## Answers

|  |  | Answers |
| :---: | :---: | :---: |
| 1 | Evaluate $6 \frac{1}{5}-2 \frac{1}{3}$ | $3 \frac{13}{15}$ |
| 2 | Find the equation of the line | $y=-\frac{2}{3} x+8$ |
| 3 | Express $a^{2}\left(2 a^{\frac{-1}{2}}+a\right)$ <br> in its simplest form | $2 a^{\frac{3}{2}}+a^{3}$ |
| 4 | Solve $x-2(x-1)=8$ | $x=-6$ |
| 5 | Solve $\begin{array}{r} 4 \sin x=2 \\ \text { for } 0^{\circ}<x<360^{\circ} \end{array}$ | $x=30^{\circ}, 150^{\circ}$ |

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| 6 | Find the standard deviation for $3,8,14,20$ <br> Give your answer to 3 significant figures | s.d. $=7.37$ (3 s.f.) |
| :---: | :---: | :---: |
| 7 | Factorise fully $2 x^{2}-32$ | $2(x+4)(x-4)$ |
| 8 | A house is bought for $£ 74,000$, increases in value 4.5\% every year for 3 years. <br> What is its new value? | New Value $=£ 84,446.29$ |
| 9 | A triangle has sides 83 cm , 79 cm and 19 cm . <br> Is it right angled? | $\begin{aligned} & 83^{2}=6889 \\ & 19^{2}+79^{2}=6602 \end{aligned}$ <br> Since $83^{2} \neq 19^{2}+79^{2}$ then by the Converse of Pythagoras the triangle is not right-angled. |
| 10 | Find the roots of the equation $y=x^{2}-x-6$ | $x=3, x=-2$ |

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| 11 | Evaluate $14.2+8.3 \times 40$ | 346.2 |
| 12 | Find the equation of the straight line passing through the points $(2,-3)$ and $(2,9)$ | $x=2$ |
| 13 | Simplify $\frac{\sqrt{12}}{\sqrt{60}}$ | $\frac{1}{\sqrt{5}}$ |
| 14 | Change the subject of the formula to $b$. $L=3 a-\sqrt{b}$ | $b=(3 a-L)^{2}$ |
| 15 | The graph shows <br> Find $P$ and $Q$ $y=5 \sin x-4$  | $Q\left(53.1^{\circ}, 0\right) \quad P\left(90^{\circ}, 1\right)$ |

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| 16 | Solve to one decimal place $2 x^{2}+4 x-9=0$ | $x=1.3$ or $\quad x=-3.3$ (1d.p.) |
| :---: | :---: | :---: |
| 17 | Factorise $2 x^{2}+7 x-15$ | $(2 x-3)(x+5)$ |
| 18 | John paid £297.50 for a laptop in a sale. The discount in the sale was $15 \%$. Calculate the original price. | Original Price $=£ 350$ |
| 19 | $\mathrm{LM}=1.2 \mathrm{~m}$ <br> Radius $=1.8 \mathrm{~m}$ <br> Find the depth of milk | Depth $=3.497 \mathrm{~m}$ |
| 20 | Find the roots of the equation $y=x^{2}-2 x-15$ | $x=5, \quad x=-3$ |

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| 21 | E has coordinates (5, 3, 1) Find the shortest distance between D and C | $\sqrt{35}$ |
| :---: | :---: | :---: |
| 22 | Find the equation of a straight line through $(2,-5)$ and parallel to $y=3 x-5$ | $y=3 x-11$ |
| 23 | Simplify $x^{\frac{1}{2}}\left(x^{\frac{1}{4}}+3\right)$ | $x^{\frac{3}{4}}+3 x^{\frac{1}{2}}$ |
| 24 | Solve $x-3(x-7)=9$ | $x=6$ |
| 25 | Sketch the graph of $y=4 \cos 2 x$ <br> for $0 \leq x \leq 360$ |  |

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| 26 | Find the volume of a sphere with radius 9 m , giving your answer to two significant figures | $V=3100 m^{3}(2 s . f$. |
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| 27 | Remove the brackets and simplify $(2 x+2)^{2}-2\left(x^{2}-2\right)$ | $2 x^{2}+8 x+8$ |
| 28 | John paid £20,000 for a motorbike but it depreciated $5.5 \%$ each year for 7 years. What was its value after 7 years? | Value $=£ 13,460.24$ |
| 29 | Find length $A B$ | $A B=0.78 \mathrm{~km}$ |
| 30 | Prove $\sin ^{3} x+\sin x \cos ^{2} x=\sin x$ | $\begin{aligned} \sin x\left(\sin ^{2} x+\cos ^{2} x\right) & =\sin x \\ \sin x(1) & =\sin x \\ \sin x & =\sin x \end{aligned}$ |

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| 31 | Evaluate without a calculator: $\frac{2.1+3.2 \times 5}{2^{3}}$ | 2.2625 |
| 32 | Does the point $(-2,4)$ lie on the line $y=3 x+10$ ? <br> Explain your answer. | Point lies on the line since substituting $\begin{gathered} x=-2 \text { and } y=4 \text { into } y=3 x+10 \text { gives: } \\ 4=3 \times(-2)+10 \\ 4=4 \end{gathered}$ |
| 33 | Simplify $\sqrt{40}+4 \sqrt{10}+\sqrt{90}$ | $9 \sqrt{10}$ |
| 34 | Simplify $(x-5)(3 x-2)$ | $3 x^{2}-17 x+10$ |
| 35 | Sketch the graph of $y=3 \sin (0.5 x)$ <br> for $0 \leq x \leq 360$ |  |


|  |  | Answers |
| :---: | :---: | :---: |
| 36 | Solve $3 x^{2}+3 x-7=0$ <br> giving your answer correct to 1 decimal place | $x=1.1$ or -2.1 |
| 37 | Factorise $6 x^{2}-24 x-30$ | $6(x-5)(x+1)$ |
| 38 | In a sale, a book now cost £36. What was it worth before a $20 \%$ discount? | £45 |
| 39 | Find the area of the triangle | Area $=187.45 \mathrm{~cm}^{2}$ |
| 40 | Sketch $y=(x+2)(x-3)$ <br> Label the intercepts and turning point |  |


| Answers |  |  |
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| 41 | Express $\overrightarrow{R P}$ in terms of $f, g$ and $h$ | $\overrightarrow{R P}=-f-g+h$ |
| 42 |  <br> Chose the correct equation for the above graph <br> a. $y=2 x+1$ <br> b. $y=-2 x+1$ <br> c. $y=2 x-1$ <br> d. $y=2 x^{2}-1$ | $y=2 x-1$ |
| 43 | Find the longest side of this right-angled triangle leaving your answer as a surd. | $5 \sqrt{2} \mathrm{~m}$ |
| 44 | Solve $11-2(1+3 x)<39$ | $x>-5$ |
| 45 | Solve $2 \tan x+5=-4$ for $0^{\circ}<x<180^{\circ}$ | $x=102.5^{\circ}, 282.5^{\circ}$ |


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| :---: | :---: | :---: |
| 46 | The standard deviation of $1,2,2,2,8 \text { is } \sqrt{a}$ <br> Find a | $a=8$ |
| 47 | Multiply out the brackets and simplify $(3 x+2)\left(x^{2}-4 x+3\right)$ | $3 x^{3}-10 x^{2}+x+6$ |
| 48 | The population of the UK is 64.1 million. If it increased by $3 \%$ for the next 7 years, what would it be? | 78.8 million (3 s.f.) |
| 49 | The square below has side length y . If the diagonal is 6 m . Find the exact length $y$ | $y=3 \sqrt{2} m$ |
| 50 | Show that $\frac{1-\cos ^{2} a}{\cos ^{2} a}=\tan ^{2} a$ | $\begin{gathered} \text { Use } \sin ^{2} a+\cos ^{2} a=1 \text { and } \tan x=\frac{\sin x}{\cos x} \\ \text { to prove LHS }=\text { RHS } \end{gathered}$ |

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| 51 | Evaluate $\frac{5}{12} \times 2 \frac{2}{9}$ <br> Give the answer in its simplest form | $\frac{25}{27}$ |
| :---: | :---: | :---: |
| 52 | A straight line has gradient 4 and it passes through the points $(2,4)$ and $(1, a)$ Find the value of $a$ | $a=0$ |
| 53 | Evaluate $2^{0}+3^{-1}$ | $1 \frac{1}{3}$ |
| 54 | Change the subject of the formula to $u$ $v^{2}=u^{2}+2 a s$ | $u=\sqrt{v^{2}-2 a s}$ |
| 55 | What is the equation of the graph below? | $y=5 \sin 3 x$ |


|  |  | Answers |
| :---: | :---: | :---: |
| 56 | Calculate the capacity of the cylindrical mug below | $V=1099 \mathrm{~cm}^{3}$ |
| 57 | Factorise $\left(100 x^{2}-500 x-2400\right)$ | $100(x-8)(x+3)$ |
| 58 | The restaurant bill included $8 \%$ tax. If the bill was $£ 324$, what was the bill before tax? | £300 |
| 59 | Calculate angle PQR | Angle PQR $=78.6^{\circ}$ |
| 60 | Write down the turning point and the equation of the axis of symmetry $y=(x-3)^{2}+4$ | $\begin{aligned} T . P . & =(3,4) \\ x & =3 \end{aligned}$ |

Step-by-step worked solutions in the N5 Maths Study Pack

| Answers |  | natio |
| :---: | :---: | :---: |
| 61 Express $\overrightarrow{A B}$ in terms of a \& b Express $\overrightarrow{O C}$ in terms of $\mathrm{a} \& \mathrm{~b}$ |  | Answers |
|  |  | $\begin{aligned} & \overrightarrow{A B}=-a+b \\ & \overrightarrow{O C}=2(b-a) \end{aligned}$ |
| 62 | Find the equation of this line | $y=2 x-5$ |
| 63 | Find $27^{\frac{2}{3}}$ | $27^{\frac{2}{3}}=9$ |
| 64 | Solve $2 x-1=\frac{x-4}{3}$ | $x=-\frac{1}{5}$ |
| 65 | What is the equation of the graph below | $y=2 \operatorname{Cos} 4 x$ |


|  |  | Answers |
| :---: | :---: | :---: |
| 66 | Show that the s.d. of $1,1,1,2,5$ is $\sqrt{3}$ and write down the s.d. of 101,101,101,102,105 | First part proof <br> Second part s.d. $=$ same $=\sqrt{3}$ |
| 67 | Multiply out and simplify $2\left(x^{2}-4 x+3\right)-x(x-3)$ | $x^{2}-5 x+6$ |
| 68 | Rob normally cycles a total distance of 56 miles per week. <br> He increases his distance by $15 \%$ each week for the next three weeks. <br> How many miles will he cycle in the third week? | Miles in $3^{\text {rd }}$ week $=85.169$ |
| 69 | Depth of water in the cylindrical tank is 5 m Calculate the radius | $r=10.6 m$ |
| 70 | Show that $\frac{\tan x}{\sin x}=\frac{1}{\cos x}$ | $\begin{aligned} & \text { Use } \tan x=\frac{\sin x}{\cos x} \\ & \text { to prove LHS }=\text { RHS } \end{aligned}$ |

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| 71 | Without using a calculator find $17.5 \% \text { of } £ 90$ | £15.75 |
| 72 | For the straight-line equation $y=m x+c$ <br> When $m>0$ and $c<0$ sketch a possible graph |  |
| 73 | Simplify $\frac{6 x y^{3}}{8 x^{4} y^{2}}$ | $\frac{3 y}{4 x^{3}}$ |
| 74 | Write as a single fraction $\frac{2}{x}+\frac{4}{x-2}$ | $\frac{6 x-4}{x(x-2)}$ |
| 75 | Solve the equation $\begin{aligned} & 11 \cos x^{\circ}-2=3 \\ & \text { for }\left(0 \leq x \leq 360^{\circ}\right) \end{aligned}$ | $x=62.96^{\circ}, 297.04^{\circ}$ |


|  |  | Answers |
| :---: | :---: | :---: |
| 76 | Find volume to 2 s.f. | $V=870 \mathrm{~cm}^{3}$ |
| 77 | Factorise $16 x^{2}-1$ | $(4 x+1)(4 x-1)$ |
| 78 | A 900g box has 20\% extra washing powder. How much washing powder was in a standard size box? | 750g |
| 79 | $\begin{aligned} & \mathrm{EF}=18 \mathrm{~m} \\ & \mathrm{OF}=\text { radius }=15 \mathrm{~m} \\ & \text { Find } \mathrm{h} \end{aligned}$ | $h=27 m$ |
| 70 | Describe the nature of the roots $y=x^{2}-3 x+3$ | There are no real roots |

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| 81 | Evaluate $3 \frac{2}{5}-2 \frac{1}{3}$ | $1 \frac{1}{15}$ |
| 82 | Find the gradient and $y$ intercept for the straight line: $3 x-17=15 y$ | $m=\frac{1}{5}, \quad c=-\frac{17}{15}$ |
| 83 | Express the below with a rational denominator in its simplest form $\frac{8}{\sqrt{8}}$ | $2 \sqrt{2}$ |
| 84 | Change the subject of the formula to $R$ $P=R^{3} b-5$ | $R=\sqrt[3]{\frac{P+5}{b}}$ |
| 85 | State the equation of the graph below | $y=4 \sin 3 x$ |

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| 86 | Make two valid comparisons for the two maths scores: <br> Class A: Mean $=65 \%$, s.d. $=12 \%$ <br> Class B: Mean $=59 \%$, s.d. $=10 \%$ | - On average Class A have higher maths scores <br> - Class A have less consistent marks |
| 87 | Factorise $4 a^{2}-60 a-136$ | $4(a-17)(a+2)$ |
| 88 | A new car cost $£ 25000$. Its value was expected to decrease every year by 20\%. <br> Find its expected value after 7 years. | Value = £5248.88 |
| 89 | Find the length $A B$ | $A B=42.66 \mathrm{~cm}$ |
| 90 | Below is a graph of $y=(x-a)^{2}+b$ <br> Find coordinates of c | $C(0,5)$ |

## N5 Self Check Ten

|  |  | Answers |
| :---: | :---: | :---: |
| 91 | Find $\|u\|$, the magnitude of $u=\left[\begin{array}{c} 6 \\ -13 \\ 18 \end{array}\right]$ | $\|u\|=23$ |
| 92 | Find the equation of a straight line between $(-7,4)$ and $(-3,5)$ | $4 y-x=23$ |
| 93 | Express in its simplest form $y^{8} \times\left(y^{3}\right)^{-2}$ | $y^{2}$ |
| 94 | Solve for $y$ $\frac{2(y-3)}{4}=\frac{y+5}{3}$ | $y=19$ |
| 95 | Solve algebraically the equation $\sqrt{3} \sin x^{\circ}-1=0$ <br> for $0 \leq x \leq 360$ | $x=35.5^{\circ}, 144.7^{\circ}$ |


|  |  | Answers |
| :---: | :---: | :---: |
| 96 | Find the total volume of the shape below. | $V=30.75 m^{3}$ |
| 97 | Multiply out and simplify $(y-2)^{3}$ | $y^{3}-6 y^{2}+12 y-8$ |
| 98 | I bought a new racing bike for £1500. This included VAT at $20 \%$. What was the cost before VAT was added? | Cost $=£ 1250$ |
| 99 | Find the length SW | $S W=6.6 \mathrm{~cm}$ |
| 100 | Express $x^{2}-14 x+44$ <br> in the form $(x-a)^{2}+b$ | $(x-7)^{2}-5$ |

