X100/303

NATIONAL QUALIFICATIONS 2005 FRIDAY, 20 MAY 10.30 AM - 12.00 NOON MATHEMATICS HIGHER Units 1, 2 and 3 Paper 2

Read Carefully

- 1 Calculators may be used in this paper.
- 2 Full credit will be given only where the solution contains appropriate working.
- 3 Answers obtained by readings from scale drawings will not receive any credit.



ALL questions should be attempted.

1. Find
$$\int \frac{4x^3 - 1}{x^2} dx, x \neq 0.$$

- 2. Triangles ACD and BCD are right-angled at D with angles p and q and lengths as shown in the diagram.
 - (a) Show that the exact value of $\sin(p+q)$ is $\frac{84}{85}$.

(a) A chord joins the points A(1,0) and B(5,4) on

Show that the equation of the perpendicular

the circle as shown in the diagram.

bisector of chord AB is x + y = 5.

- (b) Calculate the exact values of:
 - (i) $\cos(p+q);$
 - (ii) $\tan(p+q)$.

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(b) The point C is the centre of this circle. The tangent at the point A on the circle has equation x + 3y = 1.Find the equation of the radius CA.



(c) (i) Determine the coordinates of the point C.(ii) Find the equation of the circle.

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 The sketch shows the positions of Andrew(A), Bob(B) and Tracy(T) on three hill-tops.

Relative to a suitable origin, the coordinates (in hundreds of metres) of the three people are A(23, 0, 8), B(-12, 0, 9) and T(28, -15, 7).

In the dark, Andrew and Bob locate Tracy using heat-seeking beams.

(a) Express the vectors TA and TB in component form.

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- (b) Calculate the angle between these two beams.
- 5. The curves with equations $y = x^2$ and $y = 2x^2 - 9$ intersect at K and L as shown.

Calculate the area enclosed between the curves.





6. The diagram shows the graph of $y = \frac{24}{\sqrt{x}}$, x > 0. Find the equation of the tangent at P, where x = 4.



7. Solve the equation $\log_4(5-x) - \log_4(3-x) = 2, x < 3$.

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- 8. Two functions, f and g, are defined by $f(x) = k \sin 2x$ and $g(x) = \sin x$ where k > 1. The diagram shows the graphs of y = f(x) and y = g(x) intersecting at O, A, B, C and D. Show that, at A and C, $\cos x = \frac{1}{2k}$.
- 9. The value V (in £ million) of a cruise ship t years after launch is given by the formula $V = 252e^{-0.06335t}$.
 - (a) What was its value when launched?
 - (b) The owners decide to sell the ship once its value falls below £20 million. After how many years will it be sold?
- Vectors a and c are represented by two sides of an equilateral triangle with sides of length 3 units, as shown in the diagram.

Vector **b** is 2 units long and **b** is perpendicular to both **a** and **c**. Evaluate the scalar product a.(a + b + c).

11. (a) Show that x = -1 is a solution of the cubic equation $x^3 + px^2 + px + 1 = 0$.

(b) Hence find the range of values of p for which all the roots of the cubic equation are real.

[END OF QUESTION PAPER]

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