

FOR OFFICIAL USE



National
Qualifications
2025

Mark

X847/75/01

Mathematics
Paper 1 (Non-calculator)

WEDNESDAY, 14 MAY

9:00 AM – 10:00 AM



* X 8 4 7 7 5 0 1 *

Fill in these boxes and read what is printed below.

Full name of centre

Town

Forename(s)

Surname

Number of seat

Date of birth

Day

Month

Year

Scottish candidate number

Total marks — 40

Attempt ALL questions.

You must NOT use a calculator.

To earn full marks you must show your working in your answers.

State the units for your answer where appropriate.

Write your answers clearly in the spaces provided in this booklet. Additional space for answers is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting.

Use blue or black ink.

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* X 8 4 7 7 5 0 1 0 1 *

Total marks — 40
Attempt ALL questions

1. Evaluate $2\frac{4}{5} \times \frac{2}{7}$.

Give your answer in its simplest form.

2

$$\begin{aligned} & 2\frac{4}{5} \times \frac{2}{7} \\ &= \frac{14^2}{5} \times \frac{2}{\cancel{7}1} \\ &= \underline{\underline{\frac{4}{5}}} \end{aligned}$$

2. Expand and simplify $(x+3)(x+5)+4(x-2)$.

3

	x	$+3$
x	x^2	$+3x$
$+5$	$+5x$	$+15$

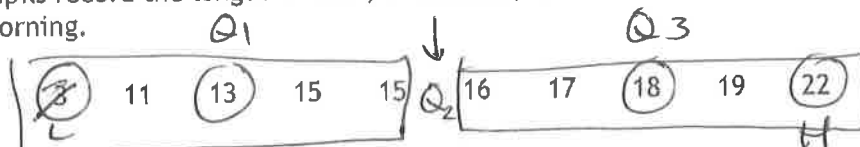
$$\begin{aligned} & (x+3)(x+5)+4(x-2) \\ &= x^2+8x+15+4x-8 \\ &= \underline{\underline{x^2+12x+7}} \end{aligned}$$

[Turn over



* X 8 4 7 7 5 0 1 0 3 *

3. Ten pupils record the length of time, in minutes, it takes them to walk to school one morning.



Calculate the interquartile range of these times.

g

$$\begin{aligned} \text{IQR} &= Q_3 - Q_1 \\ &= 18 - 13 \\ &= \underline{\underline{5}} \end{aligned}$$

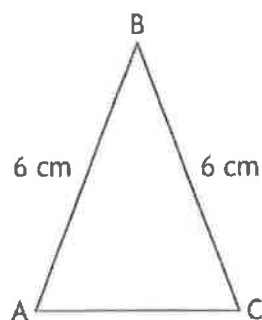
4. In a sale, the price of a wedding dress is reduced by 20%.
The sale price of the dress is £720.
Calculate the price of the dress before the sale.

%	£	
80	720	
10	90	
100	900	<u>£900</u>



* X 8 4 7 7 5 0 1 0 4 *

5. Triangle ABC is shown in the diagram.



- $AB = BC = 6$ centimetres.
- $\sin B = \frac{2}{3}$.

Calculate the area of the triangle.

2

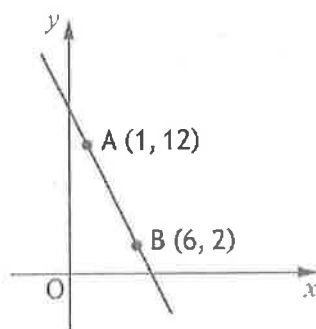
$$\begin{aligned}
 \text{Area} &= \frac{1}{2}ac \sin B \\
 &= \frac{1}{2}(6)(6)\left(\frac{2}{3}\right) \\
 &= \frac{2}{3} \text{ of } 18 \\
 &= \underline{\underline{12 \text{ cm}^2}}
 \end{aligned}$$

[Turn over



* X 8 4 7 7 5 0 1 0 5 *

6. The diagram shows the straight line passing through points A and B.



Find the equation of the line AB.

Give the equation in its simplest form.

3

$$\begin{aligned}
 m &= \frac{12 - 2}{1 - 6} \\
 &= \frac{10}{-5} \\
 &= -2
 \end{aligned}$$

$$\begin{aligned}
 y - 12 &= -2(x - 1) \\
 y - 12 &= -2x + 2 \\
 y &= -2x + 14
 \end{aligned}$$

7. A function is defined as $f(x) = 3x + 7$.

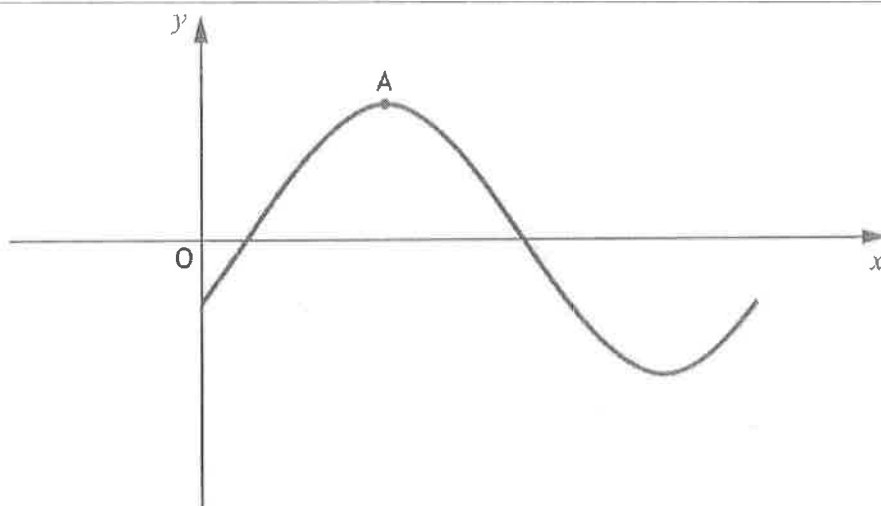
(a) Evaluate $f(6)$.

$$\begin{aligned} f(6) &= 3(6) + 7 \\ &= 18 + 7 \\ &= \underline{\underline{25}} \end{aligned}$$

(b) Given that $f(p) = 19$, find the value of p .

$$\begin{aligned} f(p) &= 3p + 7 & \therefore 3p + 7 &= 19 \\ & & 3p &= 12 \\ & & \underline{\underline{p}} &= \underline{\underline{4}} \end{aligned}$$

8. Part of the graph of $y = 2 \sin(x - 30)^\circ$ is shown in the diagram.



The graph has a maximum turning point at A.

State the coordinates of A.

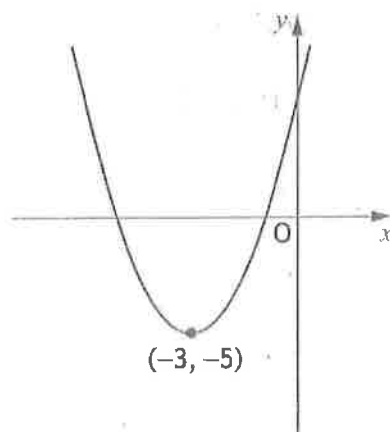
shifted 30° right.
should be $(90^\circ, 2)$
 $\therefore \underline{\underline{(120^\circ, 2)}}$

[Turn over]



* X 8 4 7 7 5 0 1 0 7 *

9. The diagram shows a parabola with equation of the form $y = (x + a)^2 + b$.



- (a) State the value of a .

1

$$a = 3$$

- (b) State the value of b .

1

$$b = -5$$

10. Simplify $\frac{n^7 \times (n^3)^2}{n^4}$.

3

$$\begin{aligned} \frac{n^7 \times (n^3)^2}{n^4} &= \frac{n^7 \times n^6}{n^4} \\ &= \frac{n^{13}}{n^4} \\ &= \underline{\underline{n^9}} \end{aligned}$$

11. Determine the nature of the roots of the function $f(x) = 3x^2 + 2x + 1$.

2

$$\begin{aligned} a &= 3 & b^2 - 4ac \\ b &= 2 & = 2^2 - 4(3)(1) \\ c &= 1 & = 4 - 12 \\ & & = -8 \\ & & b^2 - 4ac < 0 \therefore \text{no real roots.} \end{aligned}$$

12. Express $\frac{6}{\sqrt{10}}$ with a rational denominator.

Give your answer in its simplest form.

2

$$\begin{aligned} \frac{6}{\sqrt{10}} \times \frac{\sqrt{10}}{\sqrt{10}} \\ = \frac{6\sqrt{10}}{10} \\ = \frac{3\sqrt{10}}{5} \end{aligned}$$

[Turn over



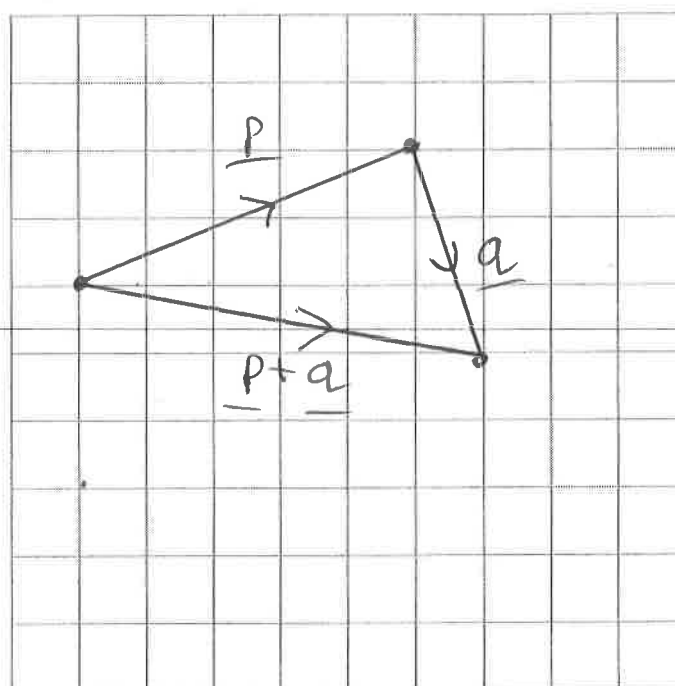
* X 8 4 7 7 5 0 1 0 9 *

13. Vectors \mathbf{p} and \mathbf{q} have components $\mathbf{p} = \begin{pmatrix} 5 \\ 2 \end{pmatrix}$ and $\mathbf{q} = \begin{pmatrix} 1 \\ -3 \end{pmatrix}$.

Draw the resultant vector $\mathbf{p} + \mathbf{q}$ on the grid.

2

(An additional grid, if required, can be found on page 14.)



14. Express

$$\frac{5}{x-1} - \frac{4}{x}, \quad x \neq 1, \quad x \neq 0$$

as a single fraction in its simplest form.

3

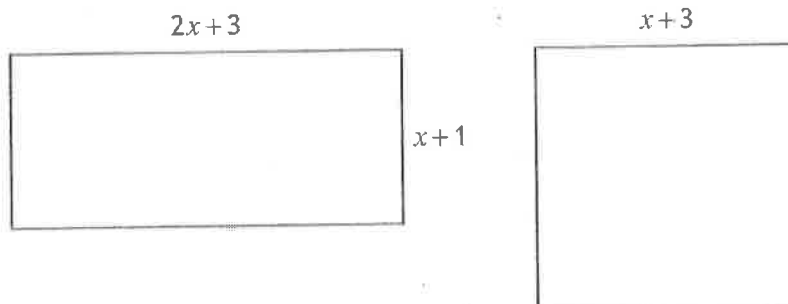
$$\begin{aligned} & \frac{5}{x-1} - \frac{4}{x} \\ &= \frac{5x - 4(x-1)}{x(x-1)} \\ &= \frac{5x - 4x + 4}{x(x-1)} \\ &= \frac{x+4}{x(x-1)} \end{aligned}$$

[Turn over



* X 8 4 7 7 5 0 1 1 1 *

15. The diagrams of a rectangle and square are shown below.
All measurements are in centimetres.



- (a) Find an expression for the area of the rectangle.

$$A = (2x+3)(x+1)$$

- (b) Given that the area of the rectangle is equal to the area of the square, show that $x^2 - x - 6 = 0$.

$$(2x+3)(x+1) = (x+3)(x+3)$$

$$2x^2 + 5x + 3 = x^2 + 6x + 9$$

$$x^2 - x - 6 = 0$$

(as required)

$$\begin{array}{c|c|c} & 2x & +3 \\ \hline x & 2x^2 & +3x \\ \hline +1 & +2x & +3 \end{array}$$

$$\begin{array}{c|c|c} & x & +3 \\ \hline x & x^2 & +3x \\ \hline +3 & +3x & +9 \end{array}$$

15. (continued)

(c) Hence find, algebraically, the length and breadth of the rectangle.

3

	x	-3
x	x^2	$-3x$
$+2$	$+2x$	-6

$$\begin{array}{r} -6 \\ 1 \quad 6 \\ \hline +2 \quad -3 \end{array}$$

$$x^2 - x - 6 = 0$$

$$(x-3)(x+2) = 0$$

$$\underline{\underline{x=3}}, \quad \cancel{x=-2}$$

[END OF QUESTION PAPER]



* X 8 4 7 7 5 0 1 1 3 *



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National
Qualifications
2025

Mark

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X847/75/02**Mathematics
Paper 2**WEDNESDAY, 14 MAY
10:30 AM – 12:00 NOON

* X 8 4 7 7 5 0 2 *

Fill in these boxes and read what is printed below.

Full name of centre

--

Town

--

Forename(s)

--

Surname

--

Number of seat

--

Date of birth

Day

--	--

Month

--	--

Year

--	--

Scottish candidate number

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Total marks — 50

Attempt ALL questions.

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* X 8 4 7 7 5 0 2 0 1 *

MARKS

DO NOT
WRITE IN
THIS
MARGIN

Total marks — 50
Attempt ALL questions

1. The number of visitors to a zoo in 2024 was 118 750.

The number of visitors is expected to increase by 4% each year over the next two years.

Calculate the expected number of visitors in 2026.

3

$$+4\% \rightarrow 104\%$$

$$= 1.04$$

$$118750 \times 1.04^2$$
$$= \underline{\underline{128440}}$$

[Turn over



* X 8 4 7 7 5 0 2 0 3 *

2. A shop sells footballs in the shape of a sphere with diameter 21 centimetres.



Calculate the volume of the football.

Give your answer correct to 3 significant figures.

3

$$\begin{aligned}
 V &= \frac{4}{3} \pi r^3 \\
 &= \frac{4}{3} \pi (10.5)^3 \\
 &= 4849.048 \dots \\
 &= \underline{\underline{4850 \text{ cm}^3}} \text{ (3sf)}
 \end{aligned}$$

3. The mass of one atom of gold is 3.27×10^{-22} grams.

The mass of one atom of carbon is 6.1% of the mass of an atom of gold.

Calculate the mass of one atom of carbon.

Give your answer in scientific notation.

$$\begin{aligned} & 6.1\% \text{ of } 3.27 \times 10^{-22} \\ &= 3.27 \times 10^{-22} \times 0.061 \\ &= \underline{\underline{1.9947 \times 10^{-23} \text{ g}}} \end{aligned}$$

[Turn over



* X 8 4 7 7 5 0 2 0 5 *

4. The weights, in kilograms, of a sample of rugby players in Scotland are shown.

93 103 99 105 88 106 92

- (a) Calculate the mean and standard deviation of these weights.

4

x	$x - \bar{x}$	$(x - \bar{x})^2$
93	-5	25
103	5	25
99	1	1
105	7	49
88	-10	100
106	8	64
92	-6	36
686	0	300

$$\begin{aligned}\bar{x} &= \frac{686}{7} \\ &= \underline{\underline{98\text{kg}}}\end{aligned}$$

$$\begin{aligned}s &= \sqrt{\frac{300}{6}} \\ &= \underline{\underline{7.07\text{kg}}}\end{aligned}$$

4. (continued)

A sample of rugby players in France has a mean weight of 105 kilograms and a standard deviation of 5.9 kilograms.

- (b) Make two valid comments comparing the weights of the rugby players in the samples from Scotland and France.

2

On average, French players are heavier
(as $105\text{ kg} > 98\text{ kg}$).
The weights of French players are more
consistent (as $5.9 < 7.07$)

5. Express $x^2 + 10x + 19$ in the form $(x+a)^2 + b$.

2

$$\begin{aligned} & (x+5)^2 + 19 - 25 \\ &= \underline{\underline{(x+5)^2 - 6}} \end{aligned}$$

[Turn over]

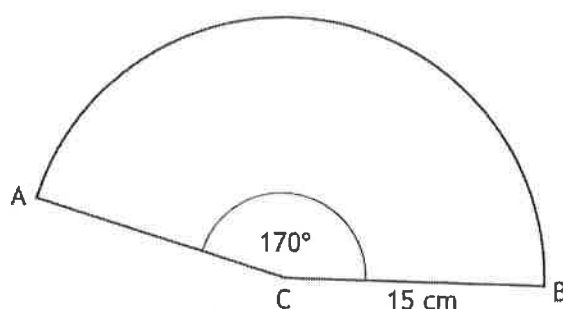


* X 8 4 7 7 5 0 2 0 7 *

6. A party hat is made in the shape of a cone, as shown.



The piece of card used for making the hat is a sector of a circle, centre C.



The radius of the circle is 15 centimetres and angle ACB is 170° .
Calculate the area of the sector.

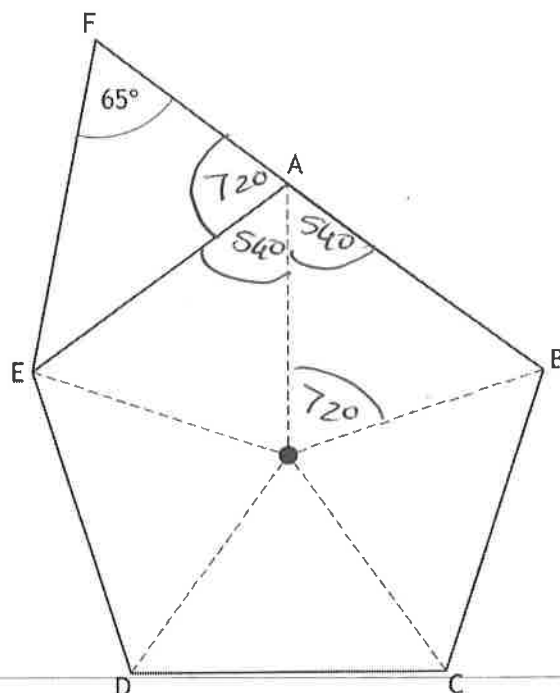
3

$$\begin{aligned} \text{Area} &= \frac{170}{360} \pi (15)^2 \\ &= \underline{\underline{333.8 \text{ cm}^2}} \end{aligned}$$



7. In the diagram, ABCDE is a regular pentagon.

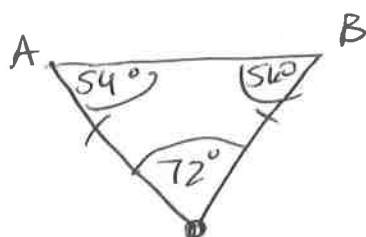
- Angle EFA is 65° .
- FAB is a straight line.



Calculate the size of angle FEA.

2

$$360 \div 5 = 72^\circ$$



$$\begin{aligned} 180 - 72 \\ = 108 \\ 108 \div 2 = 54^\circ \end{aligned}$$

$$\begin{aligned} \angle FAE &= 180 - (54^\circ + 72^\circ) \\ &= 72^\circ \end{aligned}$$

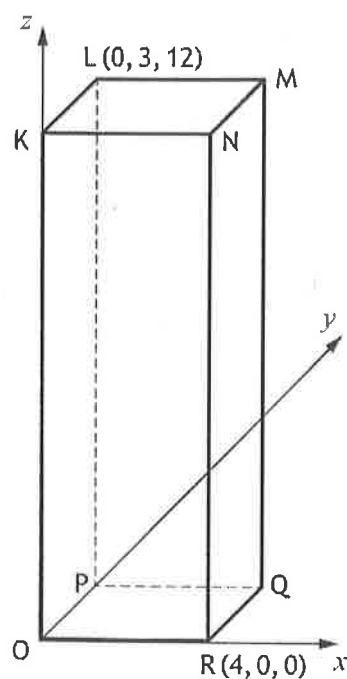
$$\begin{aligned} \angle FEA &= 180 - (65 + 72) \\ &= \underline{\underline{43^\circ}} \end{aligned}$$

[Turn over]



* X 8 4 7 7 5 0 2 0 9 *

8. The diagram shows a cuboid, KLMNOPQR, relative to the coordinate axes.



L has coordinates (0, 3, 12).

R has coordinates (4, 0, 0).

- (a) Write down the coordinates of M.

$$M = (4, 3, 12)$$

- (b) Calculate the length of the space diagonal OM.

$$\begin{aligned} \vec{OM} &= \begin{pmatrix} 4 \\ 3 \\ 12 \end{pmatrix} & |\vec{OM}| &= \sqrt{4^2 + 3^2 + 12^2} \\ & & &= \sqrt{16 + 9 + 144} \\ & & &= \sqrt{169} \\ & & &= \underline{\underline{13 \text{ units}}} \end{aligned}$$



* X 8 4 7 7 5 0 2 1 0 *

9. Change the subject of the formula $B = \frac{1}{4}kc^2 - 3c$ to k .

3

$$\begin{aligned}\frac{1}{4}kc^2 - 3c &= B \\ \frac{1}{4}kc^2 &= B + 3c \\ kc^2 &= 4(B + 3c) \\ k &= \frac{4(B + 3c)}{c^2}\end{aligned}$$

[Turn over



* X 8 4 7 7 5 0 2 1 1 *

10. On Bob's lorry there are 7 stacks of paving slabs and 3 stacks of edging blocks. The total weight of these stacks is 2400 kilograms.

Let p be the weight of a stack of paving slabs and e be the weight of a stack of edging blocks.

- (a) Write down an equation in p and e to illustrate this information.

1

$$7p + 3e = 2400 \quad (1)$$

Imran has 3 stacks of paving slabs and 4 stacks of edging blocks on his lorry. The total weight of these stacks is 1300 kilograms.

- (b) Write down an equation in p and e to illustrate this information.

1

$$3p + 4e = 1300 \quad (2)$$

Beth has 6 stacks of paving slabs and 5 stacks of edging blocks on her lorry.

- (c) Calculate the total weight of the stacks of paving slabs and edging blocks on Beth's lorry.

4

$$(1) \times 4 \rightarrow 28p + 12e = 9600 \quad (3)$$

$$(2) \times 3 \rightarrow 9p + 12e = 3900 \quad (4)$$

$$(3) - (4) \quad 19p = 5700$$

$$p = 300$$

\therefore Paving slabs = 300kg

Sub 300 for p in (1)

$$7(300) + 3e = 2400$$

$$2100 + 3e = 2400$$

$$3e = 300$$

$$e = 100$$

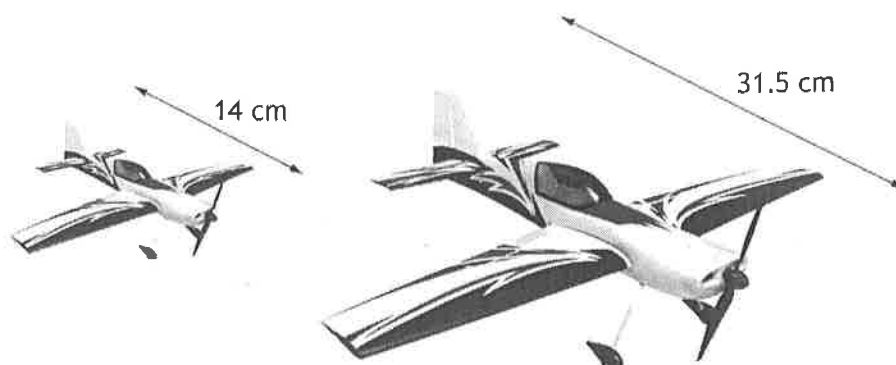
\therefore Edging slabs = 100kg

$$6p + 5e = 6(300) + 5(100) = 2300\text{kg}$$



* X 8 4 7 7 5 0 2 1 2 *

11. Two model aircraft are mathematically similar.



The small model is 14 centimetres long, and the area of one wing is 24 square centimetres.

The large model is 31.5 centimetres long.

Calculate the area of one wing of the large model.

3

$$sf = \frac{31.5}{14}$$

$$= \frac{9}{4}$$

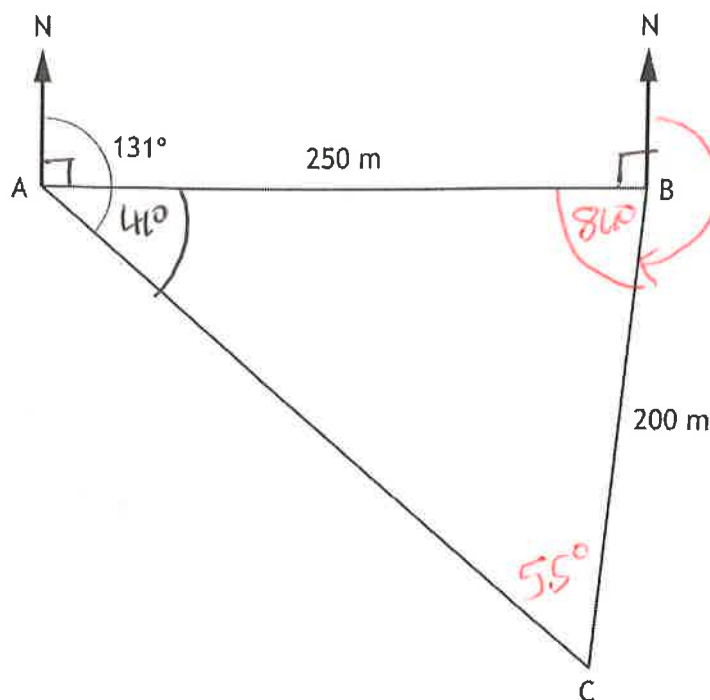
$$\text{Area} = 24 \times sf^2$$

$$= 24 \times \left(\frac{9}{4}\right)^2$$

$$= \underline{\underline{121.5 \text{ cm}^2}}$$

[Turn over

12. In the diagram A, B and C represent the positions of three checkpoints in an orienteering course.



- B is 250 metres east of A.
- The bearing of C from A is 131° .
- C is 200 metres from B.

Calculate the bearing of C from B.
Do not use a scale drawing.

\therefore Find $\angle ABC$
(need $\angle ACB$ first!)

4

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\angle ABC = 180 - (41 + 55) = 84^\circ$$

$$\therefore \frac{200}{\sin 41} = \frac{250}{\sin C}$$

$$200 \sin C = 250 \sin 41$$

$$\sin C = \frac{250 \sin 41}{200}$$

$$C = \sin^{-1} \left(\frac{250 \sin 41}{200} \right) = 55^\circ$$

$$\therefore \text{Bearing} = 360 - (90 + 84) = 186^\circ$$



* X 8 4 7 7 5 0 2 1 4 *

13. Solve the equation $\frac{5x+1}{2} = \frac{4x}{3} + 1$.

Method 1

$$\frac{5x+1}{2} - \frac{4x}{3} = 1$$

$$\frac{3(5x+1) - 2(4x)}{6} = 1$$

$$\frac{15x+3-8x}{6} = 1$$

$$\frac{7x+3}{6} = 1$$

$$7x+3 = 6(1)$$

$$7x+3 = 6$$

$$7x = 3$$

$$x = \frac{3}{7}$$

Method 2

$$2\left(\frac{5x+1}{2}\right) = 2\left(\frac{4x}{3} + 1\right)$$

$$5x+1 = \frac{8x}{3} + 2$$

$$3(5x+1) = 3\left(\frac{8x}{3} + 2\right)$$

$$15x+3 = 8x+6$$

$$15x-8x = 6-3$$

$$7x = 3$$

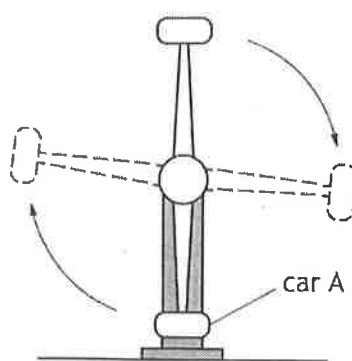
$$x = \frac{3}{7}$$

[Turn over

14. A ride at a theme park has a car attached to each end of a rotating arm.



The starting position of car A is shown in the diagram.



As the arm rotates clockwise, the height, h metres, of car A above the ground in each rotation is given by

$$h = 10 - 8 \cos x^\circ, \quad 0 \leq x < 360$$

where x° is the angle the arm has turned from car A's starting position.

Calculate the two values of x for which the height of car A is 13 metres above the ground.

4

$$13 = 10 - 8 \cos x$$

$$8 \cos x + 13 = 10$$

$$8 \cos x = -3$$

$$\cos x = -\frac{3}{8}$$

$$x = \cos^{-1}\left(-\frac{3}{8}\right)$$

$$x = 68^\circ$$

180 -	(5)	*
180 +	(1)	*

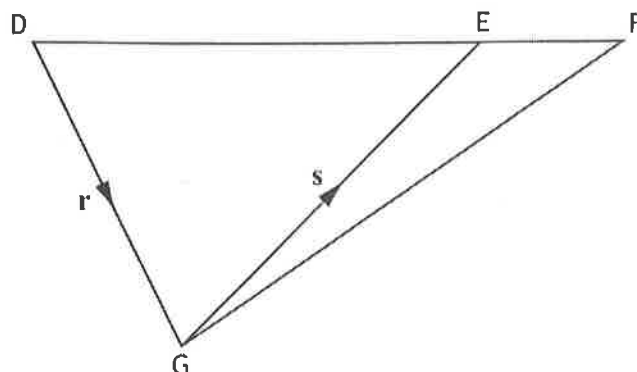
$$180 - 68 = 112^\circ$$

$$180 + 68 = 248^\circ$$

$$\therefore x = 112^\circ, 248^\circ$$



15. In the diagram, \vec{DG} and \vec{GE} are represented by the vectors \mathbf{r} and \mathbf{s} respectively, and $\vec{DE} = 3\vec{EF}$.



Express \vec{GF} in terms of \mathbf{r} and \mathbf{s} .

Give your answer in its simplest form.

2

$$\begin{aligned}\vec{DE} &= 3\vec{EF} \\ \therefore \vec{EF} &= \frac{1}{3}\vec{DE} \\ \vec{DE} &= \underline{\mathbf{r}} + \underline{\mathbf{s}}\end{aligned}$$

$$\begin{aligned}\vec{DF} &= \vec{DE} + \vec{EF} \\ &= \vec{DE} + \frac{1}{3}\vec{DE} \\ &= \underline{\frac{4}{3}\vec{DE}} \\ \vec{GF} &= \vec{GD} + \vec{DF} \\ &= -\vec{DG} + \vec{DF} \\ &= -\underline{\mathbf{r}} + \frac{4}{3}(\underline{\mathbf{r}} + \underline{\mathbf{s}}) \\ &= -\underline{\mathbf{r}} + \frac{4}{3}\underline{\mathbf{r}} + \frac{4}{3}\underline{\mathbf{s}} \\ &= \underline{\underline{\frac{1}{3}\mathbf{r} + \frac{4}{3}\mathbf{s}}}\end{aligned}$$

[END OF QUESTION PAPER]



* X 8 4 7 7 5 0 2 1 7 *