Probability

Example.

A die (dice) has the numbers 1 2 3 4 5 6 on it.

When it is thrown.

- (a) what is the probability of throwing an odd number?
- (b) if the die is thrown 70 times, how many times would you expect an odd number ?

Answer:

- (a) There are 3 odd numbers out of 6 (1, 3 and 5) 1 2 3 4 5 6 So probability (odd number) = 3/6 = 1/2
- (b) Expect $1/2 \times 70 = 35$
- 1 (a) what is the probability of throwing an even number?
 - (b) if the die is thrown 60 times, how many times would you expect an even number ?
- 2 (a) what is the probability of throwing a prime number?
 - (b) if the die is thrown 70 times, how many times would you expect a prime number?

Clue : prime numbers 2, 3, 5, 7, 11,

- 3 (a) what is the probability of throwing a number bigger than 5?
 - (b) if the die is thrown 42 times, how many times would you expect a number bigger than 5?
- 4 (a) what is the probability of throwing a number less than 3?
 - (b) if the die is thrown 90 times, how many times would you expect a number less than 3 ?

In these questions which follow, a 10 sided dice has the numbers 1 to 10 on the sides.

- 5 (a) what is the probability of throwing an odd number?
 - (b) if the die is thrown 20 times, how many times would you expect an odd number?
- 6 (a) what is the probability of throwing a multiple of 3?
 - (b) if the die is thrown 50 times, how many times would you expect a multiple of 3?
- 7 (a) what is the probability of throwing a number less than 5?
 - (b) if the die is thrown 100 times, how many times would you expect a number less than 5 ?

Clue: multiples of 3 3, 6, 9, 12,

- 8 (a) what is the probability of throwing a multiple of 5?
 - (b) if the die is thrown 120 times, how many times would you expect a multiple of 5 ?
- 9 (a) what is the probability of throwing a square number?
 - (b) if the die is thrown 30 times, how many times would you expect a square number?

Clue; square numbers 1, 4, 9, 16, 25, ...

- 10 (a) what is the probability of throwing a factor of 16?
 - (b) if the die is thrown 3000 times, how many times would you expect an odd number ?

In a pack of Playing cards there are 52 cards (+ 2 jokers IGNORE)

There are 4 different suits: 2 RED Diamonds and Hearts

2 BLACK Spades and Clubs

There are 13 cards in each suit

In each suit: ACE, 2, 3, 4, 5, 6, 7, 8, 9, 10, JACK, QUEEN, KING

A card is chosen at random. What is the probability of choosing

- 11 An Ace
- 12 A black Queen
- 13 A red card
- 14 A red or black card
- 15 The 5 of Clubs
- 16 A Diamond or a Heart
- 17 Any King
- 18 A King or a Queen of a Jack
- 19 A BLUE suit
- 20 A card with the number 9
- 21 In a College class the colour of hair of the students is noted..

Brown	11
Black	9
Blonde	8
Brunette	2

What is the probability that if s student was chosen at random they would have Blonde hair?

Give your answer as a decimal correct to 2-decimal places.

- 22 The probability of a train arriving late is 1/5
 - (a) What is the probability of it arriving on time?
 - (b) The train arrives at the station 20 times over the weekend How many times would you expect it to be on time?

23 The ages of a group of builders were as follows:

36	19	33	25	37	33	21	34
34	47	33	18	34	32	34	35

What is the probability that a builder chosen at random will be more than 25 years old?

Give your answer as a decimal fraction.

- 24 There are 5 white, 9 green and 7 red balls in a bag.
 - (a) If a ball is taken at random from the bag what is the probability that the ball is white?
 - (b) The ball drawn was white and is not replaced in the bag.A second ball is now taken from the bag.What is the probability that this second bead is not white?Give your answer as a fraction in its simplest form.
- 25 Amazon Books offers 3 kindle book Deals for £50 as shown below:

Deal 1 : 4 Horror, 5 Romance, 7 Suspense and 4 Comedy.

Deal 2 : 3 Thriller, 4 Biography, 5 Comedy and 8 Sci-Fi

Deal 3 : 2 Suspense, 4 Comedy, 6 Horror and 8 Biography.

- (a) If Pauline chooses a Deal at random, what would be the probability of her choosing a deal with 4 Comedy books?
- (b) What is the probability of choosing a Deal containing more Thriller books than Biography books ?
- 26 A survey is taken of how 100 pupils travel to school. The results are shown in the table.
 - (i) What is the probability that a pupil chosen at random cycles to school?
 - (ii) 4 pupils who normally travel by bus are transferred. What is the probability that a pupil now chosen at random goes by car to school?

Transport	Number of pupils		
Bus	36		
Cycle	9		
Walk.	31		
Car	24		

Example.

In a box there is a mixture of milk and plain chocolates.

There are 20 plain chocolates and the remainder are milk chocolates.

The probability that a chocolate chosen at random from the box is a milk one is $\frac{3}{8}$. How many chocolates, in total, are in the box?

Answer:

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3/8 are milk
So 5/8 are plain = 20 chocolates
So 1/8 = 20 \div 5 = 4
8/8 = 4 \times 8 = 32
There are 32 chocolates in the box.
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27. In a box there is a mixture of red and green counters.

There are 40 red counters and the remainder are green counters.

The probability that a counter chosen at random from the box is a green one is $\frac{3}{8}$. How many counters, in total, are in the box?

28 On a bus there is a mixture of Scottish and English students...

There are 55 Scottish students and the remainder are English students

The probability that a student chosen at random is Scottish is $\frac{5}{6}$ How many students, in total, are on the bus?

29 In a crate of fruit there is a mixture of apples and oranges.

There are 45 apples and the remainder are oranges.

The probability that an orange is chosen at random from the crate is is $\frac{2}{5}$ How many pieces of fruit, in total, are in the box?

30 There is a mixture of magazines and comics on a library shelf..

There are 36 comics and the remainder are magazines.

The probability that a magazine is chosen at random from the shelf rather than a comic $\frac{5}{8}$

What is the total number of magazines and comics on the shelf?

Example.

A charity lottery consists of a draw from a set of 40 balls numbered from 1 to 40.

(a) What is the probability that the first ball drawn has a number greater than 30?

In the draw five numbered balls are drawn and not replaced.

(b) What is the probability of the number 7 being drawn as the fifth ball if it was not drawn in the first four?

Answer:

- (a) There are 10 balls greater than 30 So probability is $10/40 = \frac{1}{4}$
- (b) By the time you get to the fifth ball, 4 have already been removed. This leaves 36 balls.So the probability of choosing the number 7 as the fifth ball is 1/36

31.

A charity lottery consists of a draw from a set of 50 balls numbered from 1 to 50.

(a) What is the probability that the first ball drawn has a number greater than 35?

In the draw five numbered balls are drawn and not replaced.

(b) What is the probability of the number 12 being drawn as the fifth ball if it was not drawn in the first four?

32

A charity lottery consists of a draw from a set of 60 balls numbered from 1 to 60.

(a) What is the probability that the first ball drawn has a number less than 11?

In the draw three numbered balls are drawn and not replaced.

(b) What is the probability of the number 21 being drawn as the third ball if it was not drawn in the first two?