## Expressions \& Formulae

 1.4:Calculate the length of an arc or the area of a sector of a circle

## Exercise 1: The Length of an Arc

1. Calculate the length of the arc in each diagram below, giving your answer correct to 1d.p.
(a)

(b)


2. Calculate the perimeter of each sector in Question 1. Giving your answers correct to 1 d.p.
3. Find the length of the minor arc $A B$ in each of the following circles, giving your answers correct to 1 d.p.
(a)

(b)
(f)

(c)

(d)
(h)



4. Calculate the length of the major arc in the circles shown in Question 3, giving your answers correct to 1 d.p.

## Exercise 2: The Area of a Sector

1. Calculate the area of the sector in each diagram below, giving your answer correct to 3 significant figures
(a)

(b)

(c)

2. Calculate the area of minor sector OAB in the circles shown below, giving your answers correct to 3 significant figures.
(a)

(e)
(f)
(b)

(c)
(g)

(d)
(h)



3. Calculate the area of the major sector for the circles in Question 2, giving your answers correct to 3 significant figures.
4. The length of minor arc $C D$ is 7.33 cm .

Calculate the area of the circle.


## Exercise 3: Problem Solving with Arcs and Sectors

1. Calculate the area of the sector shown in the diagram, given that it has radius 6.8 cm .
2. A table is in the shape of a sector of a circle with radius $1 \cdot 6$ ।.


Calculate the perimeter of the table, given that the angle at the centre is $130^{\circ}$
3. The door into a restaurant kitchen swings backwards and forwards through $110^{\circ}$.


The width of the door is 90 cm .

Calculate the area swept out by the door as it swings back and forth.
4. The YUMMY ICE CREAM Co uses a logo in the shape of an ice-cream cone.

It is made up from an isosceles triangle and a sector of a circle as shown in the diagram.

- The equal sides of the triangle are 6 cm
- The radius of the sector is 3.3 cm .

Calculate the perimeter of the logo.

5. A sensor on a security system covers a horizontal area in the shape of a sector

of a circle of radius $3 \cdot 5 \mathrm{~m}$.
The sensor detects movement in an area with an angle of $105^{\circ}$.
Calculate the area covered by the sensor.
6. A sector of a circle with radius 6 cm is shown opposite.

Angle $\mathrm{AOB}=x^{\circ}$
If the exact area of the sector is $4 \pi$ square centimetres, calculate the size of the angle marked $x$.

7. A hand fan is made of wooden slats with material on the outer edge.

(a) Calculate the area of material needed for the hand fan.
(b) Calculate the perimeter of the shaded area in the diagram above.
8. The area of the shaded sector $O P Q$ is $5.024 \mathrm{~cm}^{2}$.

Calculate the area of the circle.
9. The area sector $O B C$ is $78.5 \mathrm{~cm}^{2}$. Calculate the size of angle $x^{\circ}$.


## ANSWERS

## Exercise 1, Page 2

| 1. | (a) | $12 \cdot 6 \mathrm{~cm}$ | (b) | $34 \cdot 2 \mathrm{~mm}$ | (c) | $1 \cdot 2 \mathrm{~m}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2. | (a) | $28 \cdot 6 \mathrm{~cm}$ | (b) | $62 \cdot 2 \mathrm{~mm}$ | (c) | $5 \cdot 2 \mathrm{~m}$ |  |
| 3. | (a) | $7 \cdot 85 \mathrm{~cm}$ | (b) | $4 \cdot 7 \mathrm{~cm}$ | (c) | $18 \cdot 8 \mathrm{~cm}$ | (d) |
|  | (e) | $4 \cdot 9 \mathrm{~cm}$ | (f) | $16 \cdot 7 \mathrm{~cm}$ | (g) | $20 \cdot 9 \mathrm{~cm}$ | (h) |
| 4. | (a) | $23 \cdot 6 \mathrm{~cm}$ | (b) | $14 \cdot 1 \mathrm{~cm}$ | (c) | $37 \cdot 7 \mathrm{~cm}$ | (d) |
|  | (e) | $7 \cdot 7 \mathrm{~cm}$ | (f) | $58 \cdot 6 \mathrm{~cm}$ | (g) | $29 \cdot 3 \mathrm{~cm}$ | 3 cm |
|  |  |  |  |  | (h) | $50 \cdot 2 \mathrm{~cm}$ |  |

## Exercise 2, Page 3

1. (a) $50 \cdot 2 \mathrm{~cm}^{2}$
2. (a) $19.6 \mathrm{~cm}^{2}$
(e) $4 \cdot 88 \mathrm{~cm}^{2}$
(b) $239 \mathrm{~mm}^{2}$
(c) $1 \cdot 22 \mathrm{~m}^{2}$
(b) $\quad 7 \cdot 07 \mathrm{~cm}^{2}$
(c) $84 \cdot 8 \mathrm{~cm}^{2}$
(d) $12 \cdot 8 \mathrm{~cm}^{2}$
(f) $100 \mathrm{~cm}^{2}$
(g) $\quad 83 \cdot 7 \mathrm{~cm}^{2}$
(h) $\quad 62 \cdot 8 \mathrm{~cm}^{2}$
3. (a) $58.9 \mathrm{~cm}^{2}$
(b) $21 \cdot 2 \mathrm{~cm}^{2}$
(c) $170 \mathrm{~cm}^{2}$
(d) $141 \mathrm{~cm}^{2}$
(g) $\quad 117 \mathrm{~cm}^{2}$
(h) $251 \mathrm{~cm}^{2}$
4. $12 \cdot 8 \mathrm{~cm}^{2}$

## Exercise 3, Page 3

1. $54 \cdot 4 \mathrm{~cm}^{2}$
2. $6 \cdot 83 \mathrm{~m}$
3. 

$7770 \mathrm{~cm}^{2}$
6. $\quad 40^{\circ}$
8. $25 \cdot 1 \mathrm{~cm}^{2}$
7. $\quad(a) \quad 173 \mathrm{~cm}^{2}$
(b) $56 \cdot 5 \mathrm{~cm}$
9. $90^{\circ}$
4. 27 cm
5.

