National 5 Portfolio



Relationships 1.5 – Trig equations and Graphs

Section A - Revision

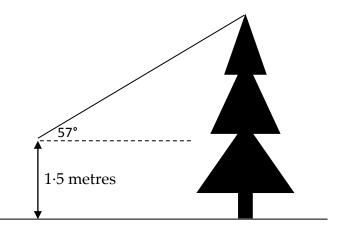
This section will help you revise previous learning which is required in this topic.

- R1 I can use Trigonometry in a right angled triangle.
- 1. John stands 10 metres from the base of a tree.

He measures the angle of elevation from his eye level to the top of the tree as 57 $^{\circ}.$

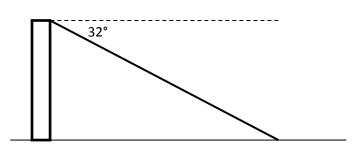
John's eye level is 1.5 metres above ground level.

Calculate the height of the tree.

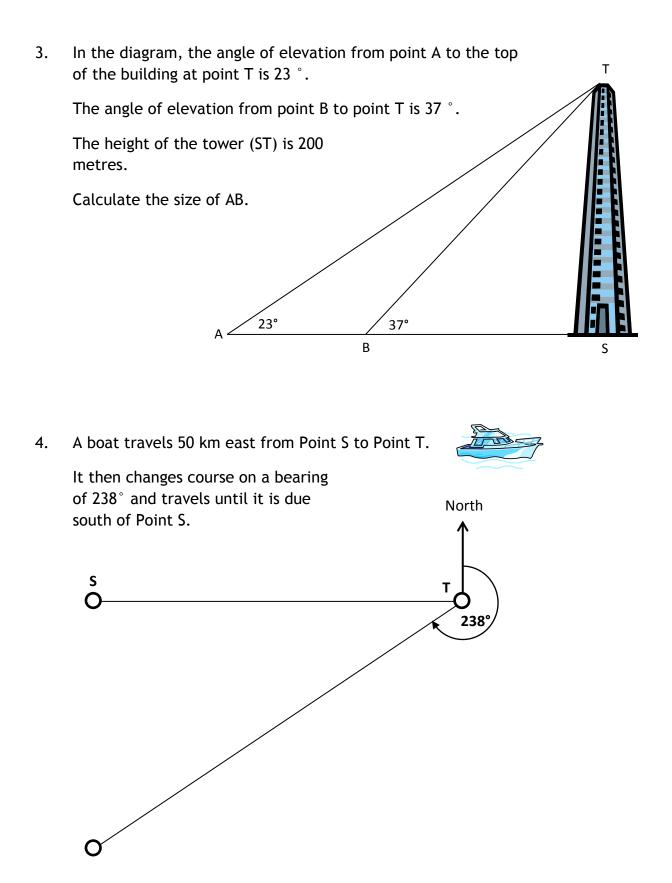


2. The army are making a death slide. The rope making the slide is 50 metres long and runs from the top of a tower to the ground.

The angle of depression at the point which attaches the rope to the top of the tower is 32 degrees.



- (a) Calculate the height of the tower.
- (b) Calculate the distance from the base of the tower to the point at which the rope is fixed to the ground.



How far has the boat travelled since leaving Point S?

Section B - Assessment Standard Section

This section will help you practise for your Assessment Standard Test for Trig Equations and Graphs. (Relationships 1.5)

Practice Assessment Standard Questions

- 1. Sketch the graph of $y = 5\sin x^{\circ}$ for $0 \le x \le 360$.
- **2.** Sketch the graph of $y = 2\sin x^{\circ}$ for $0 \le x \le 360$.
- **3.** Write down the period of the graph of the equation $y = \sin 9x^{\circ}$.
- **4.** Write down the period of the graph of the equation $y = \sin 3x^{\circ}$
- 5. Solve the equation

 $4\sin x^{\circ} + 1 = 1 \cdot 5, \ 0 \le x \le 360.$

6. Solve the equation

 $10\cos x^{\circ} - 2 = 0, \ 0 \le x \le 360.$

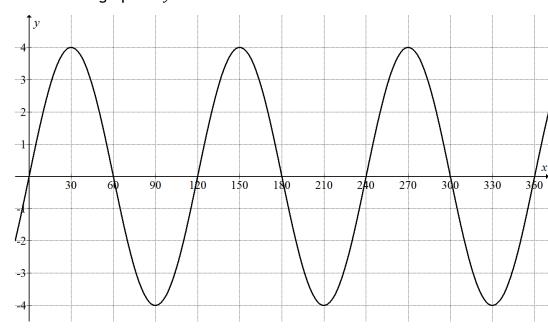
Section C - Operational Skills Section

This section provides problems with the operational skills associated with Trig Equations and Graphs.

01 I can sketch Trig Graphs.

- 1. Sketch the graph of $y = -2 \sin x^\circ$, $0 \le x \le 360$.
- **2.** Sketch the graph of $y = 4 \cos 2x^\circ$, $0 \le x \le 360$.
- **3.** Sketch the graph of $y = \sin x^{\circ} + 2$, $0 \le x \le 360$.
- **4.** Sketch the graph of $y = 3 \cos x^{\circ} 1, 0 \le x \le 360$.
- 5. Sketch the graph of $y = 2 \cos x^\circ$, $0 \le x \le 360$.
- 6. Sketch the graph of $y = 2 \sin 3x^\circ$, $0 \le x \le 360$.
- 7. Sketch the graph of $y = \tan x^\circ$, $0 \le x \le 360$.
- 8. Sketch the graph of $y = 5 \sin 2x^\circ$, $0 \le x \le 360$.

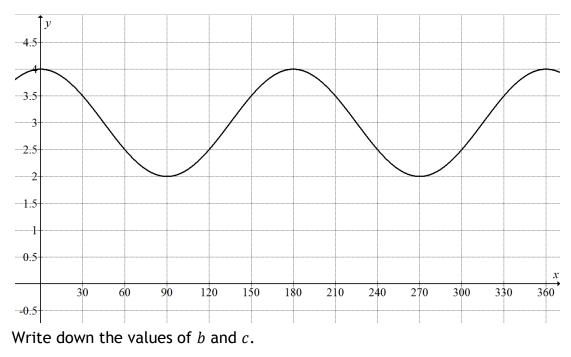
02 I can identify Trig Graphs.

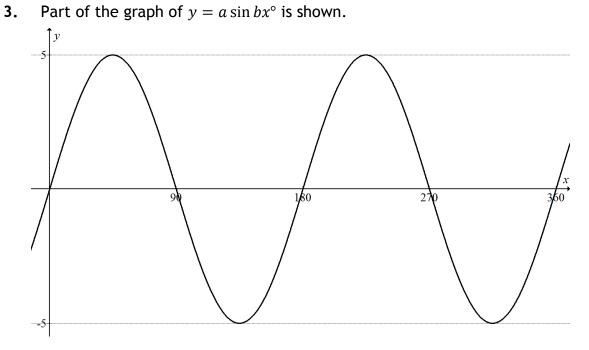


1. Part of the graph of $y = a \sin bx^{\circ}$ is shown.

Write down the values of a and b.

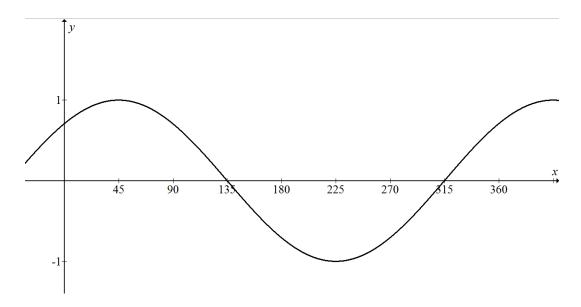
2. Part of the graph of $y = \cos bx^{\circ} + c$ is shown.



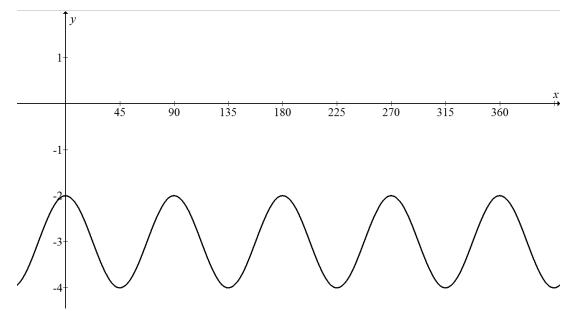


Write down the values of a and b.

4. Part of the graph of $y = \cos(x - a)^\circ$ is shown.



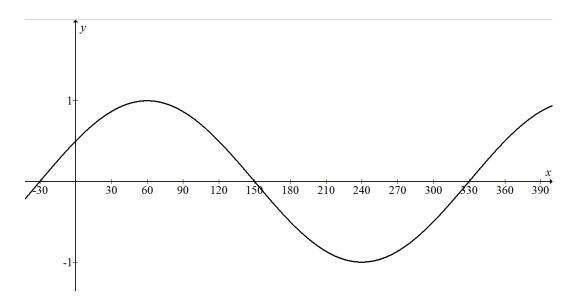
Write down the value of a.



5. Part of the graph of $y = \cos bx^{\circ} + c$ is shown.

Write down the values of b and c.

6. Part of the graph of $y = \sin(x + a)^\circ$ is shown.



Write down the value of a.

03

1. Write down the exact value of:					
(c) tan 30°					
(f) tan 60°					
(i) tan 45°					
(l) tan 0°					
(0) tan 90°					
2. Write down the exact value of:					
(c) tan 330°					
(f) tan 120°					
(i) tan 225°					
 (l) tan 0° (o) tan 90° (c) tan 330° (f) tan 120° 					

I know the common exact values in the four quadrants.

O4 I can solve Trig Equations.

1. Solve the equation

 $5 \tan x^\circ - 6 = 2$, $0 \le x < 360$.

2. Solve the equation

 $4\cos x^{\circ} + 3 = 0, \qquad 0 \le x \le 360.$

3. Solve the equation

 $7\sin x^{\circ} + 1 = -5, \qquad 0 \le x \le 360.$

4. Solve the equation

 $2 \tan x^\circ - 3 = 5$, $0 \le x \le 360$.

5. Solve the equation

 $5\cos x^{\circ} - 3 = 1$, $0 \le x \le 360$.

6. Solve the equation

 $5\cos x^\circ + 4 = 0$, $0 \le x < 360$.

05 I can manipulate Trig Identities.

1. If $\sin x^\circ = \frac{4}{5}$ and $\cos x^\circ = \frac{3}{5}$, calculate the value of $\tan x^\circ$.

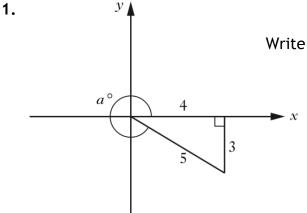
2. Simplify
$$\frac{\cos x^\circ \tan x^\circ}{\sin x^\circ}$$
.

3. Simplify
$$\frac{\cos^3 x^\circ}{1-\sin^2 x^\circ}$$
.

4. Prove that
$$\frac{\sin^2 A}{1-\sin^2 A} = \tan^2 A$$

Section D - Reasoning Skills Section

This section provides problems with Trig Equations and Graphs.



Write down the exact value of $\cos a^\circ$.

- 2. If $f(x) = 3 \sin x^\circ$, $0 \le x \le 360$
 - (a) Find *f*(270).
 - (b) $f(t) = 0 \cdot 6$.

Find two possible values of t.

- **3.** An angle, a° , can be described by the following statements.
 - a° is greater than 0 and less than 360
 - sin *a*° is negative
 - cos *a*° is positive
 - tan *a*° is negative

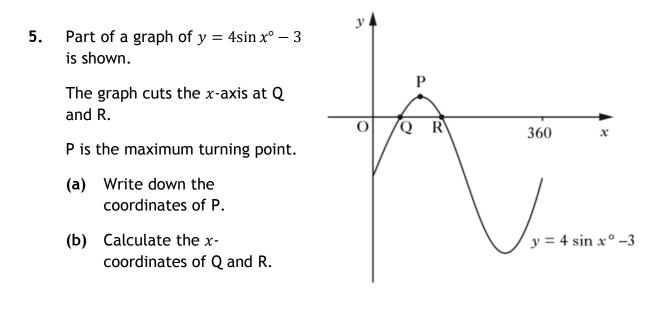
Write down a possible value for a.

4. The depth of water, D metres, in a harbour is given by the formula

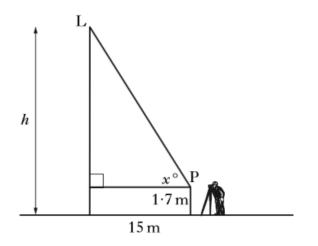
 $D = 3 + 1 \cdot 75 \sin 30h^{\circ}$

Where h is the number of hours after midnight.

- (a) Calculate the depth of water at 5am.
- (b) Calculate the maximum difference in depth of water in the harbour.



6. In the diagram below, the point L represents the lift.



The height, h metres, of the lift above the ground is given by the formula

 $h = 15 \tan x^\circ + 1 \cdot 7$

Where x° is the angle of elevation from the surveyor at point P.

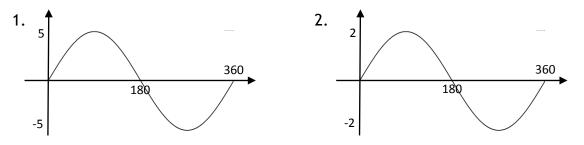
- (a) What is the height of the lift above the ground when the angle of elevation from P is 25°?
- (b) What is the angle of elevation at the point P when the height of the lift above the ground is 18.4 metres?

Answers

Section A - Revision

- 1. 16·9 m 2.(a) 26·5 m (b) 42·4 m 3. AB = 205·76 m
- 4. 108.962 km

Section B - Practice Assessment Standard Questions

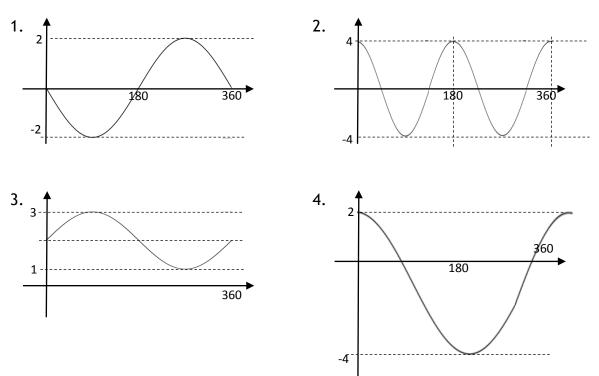


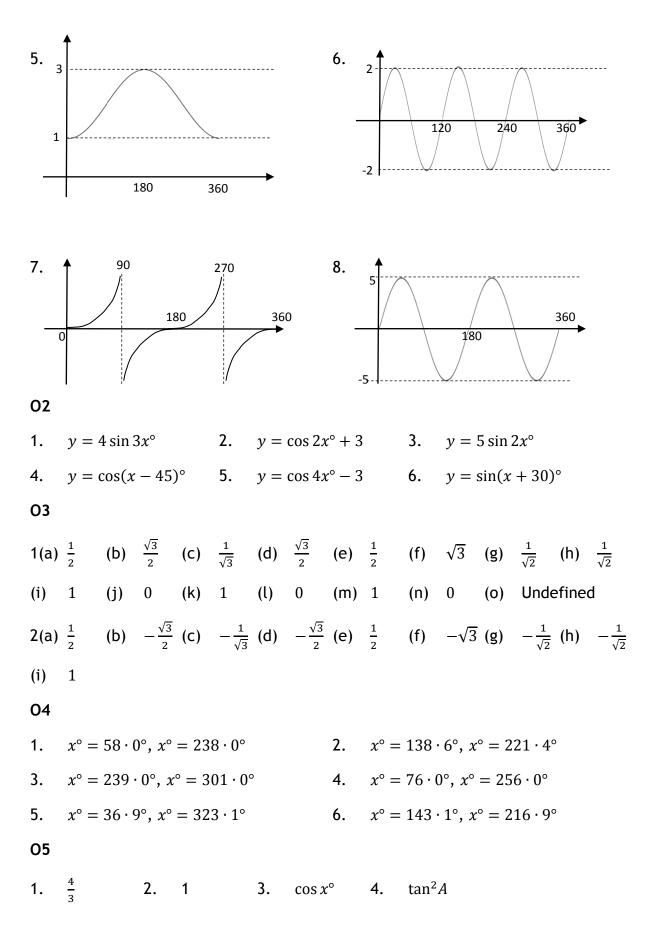
3. Period = 40° 4. Period = 120° 5. $x = 7 \cdot 2^{\circ}, x = 172 \cdot 8^{\circ}$

6.
$$x = 78 \cdot 5^{\circ}, x = 281 \cdot 5^{\circ}$$

Section C - Operational Skills

01





Section D - Reasoning Skills Section

- 1. $\frac{4}{5}$ 2. (a) -3 (b) $t = 11 \cdot 5$ and $168 \cdot 5$
- 3. Any answer 270 < a < 360 4. (a) 3.875 m (b) 3.50 m
- 5. (a) P(90, 1) (b) Q(48.6, 0) R(131.4, 0)
- 6. (a) 8.69 m (b) 48.1°