

$$f(x) = a \sin x + b \cos x$$

compare to required
trigonometric identities

$$f(x) = k \sin(x + \beta)$$
$$= k \sin x \cos \beta + k \cos x \sin \beta$$

Compare coefficients

$$a = k \cos \beta$$

$$b = k \sin \beta$$

Square and add then
square root gives

$$k = \sqrt{a^2 + b^2}$$

Divide and inverse tan gives

$$\beta = \tan^{-1} \frac{b}{a}$$

Process
example

Wave Function

a and b values
decide which
quadrant

Write out required form

$$f(x) = k \sin(x \pm \beta)$$

transforms

$$f(x) = a \sin x + b \cos x$$

into the form

$$f(x) = k \sin(x \pm \beta)$$

OR

$$f(x) = k \cos(x \pm \beta)$$

Related topic
Solving trig equations