## Applying Algebraic skills

## AH Mathematics HW

to Number Theory

## Essential knowledge:

1. Use the Euclidean algorithm to find the greatest common divisor of:
(a) 679 and 388
(b) 174 and 319
(c) 3066 and 713
2. Which pair of values in question 1 are co-prime?
3. Use the Euclidean algorithm to find integers $x$ and $y$ such that

$$
149 x+139 y=1
$$

4. Convert 238 , to base 10 .
5. Convert 59 to base 3 .

## Unit level:

6. Use the Euclidean algorithm to obtain the greatest common divisor of 1448 and 328

## Assessment level:

7. Use the Euclidean algorithm to show that $(231,17)=1$.
8. Use the Euclidean algorithm to obtain the greatest common divisor of 1204 and 833, expressing it in the form $1204 a+833 b$, where $a$ and $b$ are integers.
9. Change $712_{8}$ to base 5 .

## Challenge Questions (optional)

1. The numbers $5,6,7,8,9,10$ are to be placed in the diagram, so that the sum of the numbers in each pair of touching circles is a prime number. The number 5 is placed in the top circle. What number is placed in the
 shaded circle?
A 6
B 7
C 8
D 9
E 10
2. The number 3 can be expressed as the sum of one or more positive integers in four different ways:

$$
3 ; \quad 1+2 ; \quad 2+1 ; \quad 1+1+1
$$

In how many ways can the number 5 be so expressed?
A 8
B 10
C 12
D 14
E 16

