

Chain Rule

Product Rule

Quotient Rule

Parametric Differentiation
1st Derivative

Parametric Differentiation
2nd derivative

Parametric Differentiation
Speed

Derivative of an Inverse Function

$$h(x) = f(x)g(x)$$

$$h'(x) = f'(x)g(x) + f(x)g'(x)$$

$$\frac{d}{dx}(f(g(x))) = f'(g(x)) \cdot g'(x)$$

$$\frac{dy}{dx} = \frac{dy/dt}{dx/dt}$$

$$h(x) = \frac{f(x)}{g(x)}$$

$$h'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{(g(x))^2}$$

$$speed = \sqrt{\left(\frac{dx}{dt}\right)^2 + \left(\frac{dy}{dt}\right)^2}$$

$$\frac{d^2y}{dx^2} = \frac{y''x' - y'x''}{(x')^3}$$

$$\frac{d}{dx}(f^{-1}(x)) = \frac{1}{f'(f^{-1}(x))}$$

Volume of Revolution
about the x -axis
between the lines
 $x = b$ and $x = a$

Volume of Revolution
about the y -axis
between the lines
 $y = b$ and $y = a$

Integration by Parts

Rectilinear Motion
Displacement (x)

Rectilinear Motion
Velocity (v)

Rectilinear Motion
Acceleration (a)

Integration

$$\int \frac{f'(x)}{f(x)} dx =$$

Integration

$$\int f'(x)f(x)dx =$$

$$V = \int_a^b \pi x^2 dy$$

$$V = \int_a^b \pi y^2 dx$$

$$x = \int v dt$$

$$\int f g' = f g - \int f' g$$

$$a = \frac{dv}{dt}$$

$$v = \frac{ds}{dt}$$

$$v = \int a dt$$

$$\frac{1}{2} (f(x))^2 + c$$

$$\ln |f(x)| + c$$

$$\sec x =$$

$$\operatorname{cosec} x =$$

$$\cot x =$$

Matrices
INCONSISTENT

Matrices
REDUNDANT

Matrices
ILL-CONDITIONED

$$\frac{1}{\sin x}$$

$$\frac{1}{\cos x}$$

$$\frac{1}{\tan x}$$

$$\begin{pmatrix} 1 & 2 & 2 & 11 \\ 0 & -3 & 1 & -3 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

From row 3 we can see that this equations is REDUNDANT
i.e. there is an infinite number of solutions.

$$\begin{pmatrix} 1 & 2 & 2 & 11 \\ 0 & -5 & -3 & -14 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

From row 3 we can see that this equations is INCONSISTENT
i.e. there are NO solutions.

This occurs when a SMALL change
in the coefficients of the
equations leads to a LARGE
change in the solutions.

Complex Numbers

Complex Conjugate of
 $z = x + iy$

Complex Numbers

Polar Form
Modulus

Complex Numbers

Polar Form
Argument

Complex Numbers

De Moivre' Theorem

Partial Fractions

Distinct Linear Factors

Partial Fractions

Repeated Linear Factor

Partial Fractions

Irreducible Quadratic Factor

Modulus

$$r = \sqrt{x^2 + y^2}$$

$$z = x - iy$$

$$z = r(\cos \theta + i \sin \theta)$$

$$z^n = r^n(\cos n\theta + i \sin n\theta)$$

Argument

$$\theta = \tan^{-1} \frac{y}{x}$$

$$\frac{f(x)}{(x+a)(x+b)^2} = \frac{A}{(x+a)} + \frac{B}{(x+b)} + \frac{C}{(x+b)^2}$$

$$\frac{f(x)}{(x+a)(x+b)} = \frac{A}{(x+a)} + \frac{B}{(x+b)}$$

$$\frac{f(x)}{(x+a)(x^2+bx+c)} = \frac{A}{(x+a)} + \frac{Bx+C}{(x^2+bx+c)}$$

Matrices

Determinant 2×2

Matrices

Determinant 3×3

Matrices

Transpose of a Matrix

Transformation Matrix

Reflection in the x -axis

Transformation Matrix

Reflection in the y -axis

Transformation Matrix

Reflection in the *origin*

Transformation Matrix

Reflection in line $y = x$

Transformation Matrix

Reflection in the line through O which makes an angle of θ with the x -axis.

$$A = \begin{pmatrix} a & b & c \\ d & e & f \\ g & h & i \end{pmatrix}$$

$$\det A = a \begin{vmatrix} e & f \\ h & i \end{vmatrix} - b \begin{vmatrix} d & f \\ g & i \end{vmatrix} + c \begin{vmatrix} d & e \\ g & h \end{vmatrix}$$

$$A = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$

$$\det A = ad - bc$$

$$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

Interchange the rows and columns.

$$A = \begin{pmatrix} a & b & c \\ d & e & f \end{pmatrix}$$

$$A' = \begin{pmatrix} a & d \\ b & e \\ c & f \end{pmatrix}$$

$$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} \cos 2\theta & \sin 2\theta \\ \sin 2\theta & -\cos 2\theta \end{pmatrix}$$

$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

Transformation Matrix

Rotation through θ° in an anti-clockwise direction.

Vectors

Direction Ratios

Vectors

Direction Cosines

Vectors

Vector Product

Vectors

Scalar Triple Product

$$\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

$$\underline{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}$$

direction cosines $\frac{a_1}{|\underline{a}|} : \frac{a_2}{|\underline{a}|} : \frac{a_3}{|\underline{a}|}$

$$\underline{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix}$$

direction ratio $a_1 : a_2 : a_3$

$$\underline{a} \cdot (\underline{b} \times \underline{c}) = \begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix}$$

$$\underline{a} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} \quad \underline{b} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$$

$$\underline{a} \times \underline{b} = \begin{vmatrix} \underline{i} & \underline{j} & \underline{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix}$$

$$= \underline{i} \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix} - \underline{j} \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix} + \underline{k} \begin{vmatrix} a_1 & a_2 \\ b_1 & b_2 \end{vmatrix}$$

Differential Equations

Variable Separable

Differential Equations

First Order Linear

Second Order Differential
Equations

Auxiliary Equation
Roots - Real & Distinct

Second Order Differential
Equations

Auxiliary Equation
Roots - Real & Equal

Second Order Differential
Equations

Auxiliary Equation
Roots - Complex

Odd Functions

Even Functions

$$\frac{dy}{dx} + P(x)y = Q(x)$$

$$I(x) = e^{\int P(x)dx}$$

$$I(x)y = \int I(x) Q(x) dx$$

$$\frac{dy}{dx} = f(x)g(y)$$

$$\int \frac{dy}{g(y)} = \int f(x)dx$$

Complementary Function

$$y = Ae^{mx} + Bxe^{mx}$$

Complementary Function

$$y = Ae^{m_1x} + Be^{m_2x}$$

Complementary Function

$$y = e^{px}(A \cos qx + B \sin qx)$$

$$f(-x) = f(x)$$

$$f(-x) = -f(x)$$

Nature of Stationary Points

$$\frac{d^2y}{dx^2} < 0$$

Nature of Stationary Points

$$\frac{d^2y}{dx^2} > 0$$

Nature of Stationary Points

$$\frac{d^2y}{dx^2} = 0$$

Concavity

Concave Upwards

Concavity

Concave Downwards

Arithmetic Sequence
nth term

Arithmetic Series
sum of 1st n terms

Minimum Turning Point

Maximum Turning Point

Use a Nature Table

$$f''(x) < 0$$

$$f''(x) > 0$$

$$S_n = \frac{n}{2}(2a + (n - 1)d)$$

$$U_n = a + (n - 1)d$$

Geometric Sequence
 n^{th} term

Geometric Series
sum of 1^{st} n terms

Geometric Series
sum to infinity

Pascal's Triangle

Binomial Theorem

Binomial Coefficient

$$S_n = \frac{a(1 - r^n)}{1 - r}$$

$$U_n = ar^{(n-1)}$$

$$\begin{array}{ccccccccc} & & & & 1 & & & & \\ & & & & & 1 & & 1 & \\ & & & 1 & & 2 & & 1 & \\ & & 1 & & 3 & & 3 & & 1 \\ 1 & & 4 & & 6 & & 4 & & 1 \end{array}$$

if $-1 < r < 1$ then

$$S_\infty = \frac{a}{1 - r}$$

$${}^nC_r = \frac{n!}{r!(n-r)!} = \binom{n}{r}$$

$$(x + y)^n = \sum_{r=0}^{r=n} \binom{n}{r} x^{n-r} y^r$$

