

Indices

Remember:

Anything to the power 0 is 1 i.e.

$$4^0 = 1 \quad 11^0 = 1 \quad x^0 = 1 \quad (ab)^0 = 1 \quad (\frac{1}{3})^0 = 1$$

A negative power indicates a fraction i.e.

$$4^{-1} = 1/4$$

1. Simplify

$$(1) a^4 \times a^3$$

$$(2) c^6 \times c^{-2}$$

$$(3) 3m^4 \times 2m$$

$$(4) 5d^{-3} \times 2d^{-4}$$

$$(5) e^4 \div e^2$$

$$(6) g^{-2} \div g^{-6}$$

$$(7) 20h^3 \div 4h^6$$

$$(8) 18p^{-3} \div 3p^{-7}$$

$$(9) \frac{4m^3 \times 3m^4}{2m^2}$$

$$(10) \frac{5n^{-2} \times 4n^5}{10n^{-3}}$$

$$(11) \frac{24n^9}{2n^3 \times 4n^{-1}}$$

$$(12) \frac{18p^7}{(3p^2)^2}$$

$$(13) \frac{6p^{-1} \times 3p^5}{9p^{-4}}$$

$$(14) \frac{4a \times 3a^{-5}}{6a^{-2}}$$

$$(15) \frac{(4u)^2}{8u^{-3}}$$

$$(16) \frac{(2p)^3}{8p^2}$$

$$(17) (y^4)^{-2}$$

$$(18) (a^{-4})^{-2}$$

$$(19) \frac{(c^2)^4}{c^3}$$

$$(20) \frac{(d^{-2})^4}{d^{-5}}$$

$$(21) (m^4)^{-2} \times m^4$$

$$(22) e^8 \times (e^4)^{-2}$$

$$(23) \frac{y^8}{(y^2)^3}$$

$$(24) \frac{(b^4)^2}{b \times b^3}$$

$$(25) (2v^2)^3$$

$$(26) (3n^{-3})^2$$

$$(27) (a^4)^{\frac{1}{2}}$$

$$(28) (p^{-6})^{\frac{2}{3}}$$

$$(29) 4t^{\frac{1}{2}} \times t^{\frac{1}{2}}$$

$$(30) 6u^{\frac{3}{4}} \times 3u^{\frac{1}{4}}$$

$$(31) 5w^{\frac{5}{2}} \times 2w^{\frac{3}{2}}$$

$$(32) 10x^{\frac{1}{2}} \div 2x^{\frac{1}{2}}$$

$$(33) 24y^3 \div 4y^{\frac{1}{2}}$$

$$(34) 16z^{\frac{1}{3}} \div 2z^2$$

$$(35) \frac{4a^{\frac{1}{2}} \times 5a^{\frac{1}{2}}}{10a}$$

$$(36) \frac{6c^{\frac{2}{3}} \times 3c^{\frac{4}{3}}}{9c^2}$$

$$(37) \frac{(4d^{\frac{2}{3}})^2}{8d^{\frac{1}{3}}}$$

$$(38) \frac{3e^{-3} \times 4e^{\frac{1}{2}}}{2e}$$

$$(39) \frac{5g^{\frac{1}{2}} \times g^2}{g^{\frac{1}{3}}}$$

$$(40) \frac{24h^4}{(2h^{\frac{1}{2}})^2}$$

$$(41) m^4 \times \sqrt{m}$$

$$(42) a^{-3} \times \sqrt{a}$$

$$(43) u^2 \times \sqrt[3]{u^2}$$

$$(44) \sqrt[4]{c^5} \times c$$

$$(45) e^3 \div \sqrt{e}$$

$$(46) m^{-4} \div \sqrt{m}$$

$$(47) \sqrt[3]{k^2} \div k$$

$$(48) f^{-2} \div \sqrt[4]{f}$$

$$(49) 6\sqrt{a} \times 3a^2$$

$$(50) 4p^{-2} \div 2\sqrt[3]{p}$$

2. Expand the brackets

$$(1) x(x^3 - 4)$$

$$(2) 2y^2(3y^4 + 5y^{-2})$$

$$(3) 3a^{-1}(4a^3 + 2a)$$

$$(4) 3c(4c^3 - 6c^4)$$

$$(5) m(2m^{-1} - 4m^{-4})$$

$$(6) 2u^{-5}(u + 3u^5)$$

$$(7) 5n^4(n^{-2} + \frac{2}{n^3})$$

$$(8) 2w^5\left(\frac{1}{w} + 4w^{-2}\right)$$

$$(9) p^4\left(3p^{-4} - \frac{2}{p^3}\right)$$

$$(10) 4d^{\frac{1}{2}}(3d^{\frac{1}{2}} - d^{\frac{1}{2}})$$

$$(11) e^{\frac{1}{2}}(e^{\frac{1}{2}} - 2e^{\frac{1}{3}})$$

$$(12) 3m^{\frac{1}{2}}(m^{\frac{1}{2}} + \frac{3}{m^{\frac{1}{2}}})$$

$$(13) n^{\frac{1}{2}}(2n^{\frac{1}{3}} - \frac{1}{\sqrt[3]{n^2}})$$

$$(14) x^{\frac{1}{2}}(2x^{\frac{1}{3}} + \frac{3}{\sqrt[3]{x}})$$

$$(15) 2a^{\frac{1}{2}}(\frac{1}{\sqrt[3]{a^2}} - 4\sqrt[3]{a^4})$$

$$(16) x^{\frac{1}{2}}(2x - 3)$$

$$(17) 3a(a^{\frac{1}{2}} + 2a^{-2})$$

$$(18) u^{\frac{1}{2}}(3u + u^3)$$

$$(19) b^{\frac{1}{3}}(b^2 + 2b^{-1})$$

$$(20) 2p^{\frac{1}{4}}(p^{\frac{1}{4}} - p)$$

3. Find the value of

$$(1) \sqrt[3]{27^2}$$

$$(2) \sqrt[4]{16^5}$$

$$(3) \sqrt[2]{100^3}$$

$$(4) \sqrt[3]{8^6}$$

$$(5) \sqrt[3]{64^{-2}}$$

$$(6) \sqrt[3]{1^5}$$

$$(7) \sqrt{4^{-5}}$$

$$(8) \sqrt[3]{1000^{-2}}$$

$$(9) \sqrt[3]{\frac{1}{8}}$$

$$(10) \sqrt[4]{\frac{1}{16}}$$

$$(11) 8^{-2}$$

$$(12) 25^{\frac{1}{2}}$$

$$(13) 32^{\frac{1}{5}}$$

$$(14) 9^{\frac{1}{2}}$$

$$(15) 16^{\frac{1}{4}}$$

$$(16) 125^{\frac{1}{3}}$$

$$(17) 1^{\frac{1}{2}}$$

$$(18) (\frac{1}{4})^{\frac{1}{2}}$$

$$(19) (\frac{8}{27})^{\frac{1}{3}}$$

$$(20) (\frac{1}{8})^{\frac{1}{3}}$$

4. Find x in each of the following

$$(1) 4^x = 32$$

$$(2) 9^x = 27$$

$$(3) 16^x = 32$$

$$(4) 4^x = \sqrt{32}$$

$$(5) 25^x = 125$$

$$(6) 4^x = 128$$

$$(7) 3^x = \sqrt{27}$$

$$(8) 9^x = \sqrt{27}$$

$$(9) 100^x = 1000$$

$$(10) 8^x = \sqrt{32}$$

$$(11) 4^x = \sqrt{8}$$

$$(12) 2^{3x} = \sqrt{64}$$

$$(13) 2^{5x} = \sqrt{64}$$

$$(14) 8^x = \sqrt{128}$$

$$(15) 4^x = \sqrt[3]{32}$$

$$(16) 9^x = \sqrt[5]{27}$$

$$(17) 25^x = \sqrt[4]{125}$$

$$(18) 8^x = \sqrt[4]{32}$$

$$(19) 9^x = \sqrt[3]{81}$$

$$(20) 1000^x = \sqrt[5]{100}$$

5. A formula is given as $P = \frac{27}{3^x}$

- (a) Calculate P when $x = 2$.
- (b) Calculate x when $P = 9$.
- (c) Calculate the maximum value of P given $x \geq 0$

6. A formula is given as $H = \frac{2^a}{4}$

- (a) Calculate H when $a = 6$.
- (b) Calculate a when $H = 8$.
- (c) Calculate the minimum value of H given $a \geq 0$

7. The intensity of light, I, emerging after passing through a liquid with concentration, c, is given the formula

$$I = \frac{20}{2^c} \quad c \geq 0$$

- (a) Find the intensity of light when the concentration is 3.
- (b) Find the concentration of the liquid when the intensity is 10.
- (c) What is the maximum possible intensity?