

Graphs

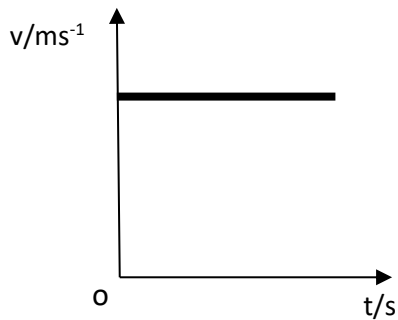
N4

Speed – Time Graphs

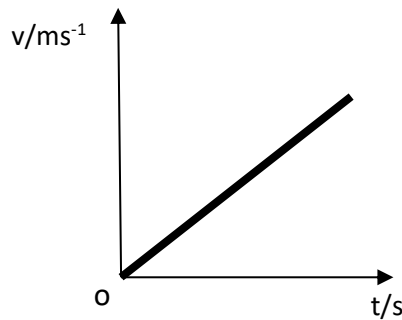
A speed-time graph is a useful way of describing the motion of an object.

Since speed is a scalar quantity, a speed-time graph considers motion in one direction only.

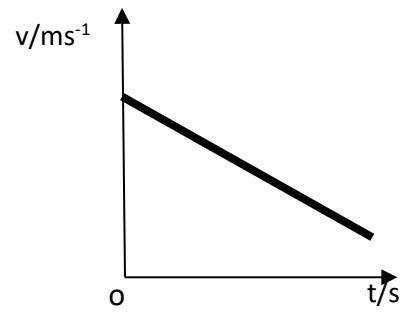
The graphs below illustrate the 3 types of motion you will study.



constant speed



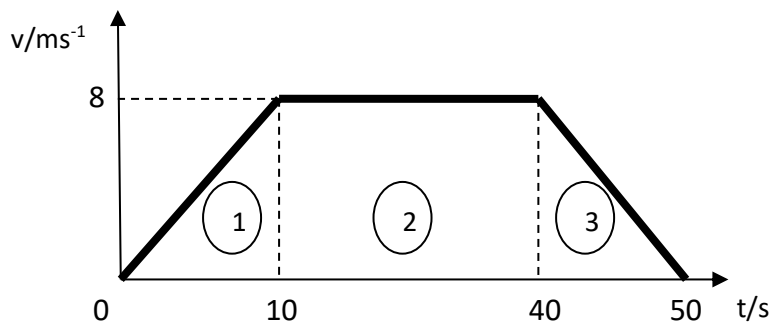
increasing speed
(constant acceleration)



decreasing speed
(constant deceleration)

The steeper the line (larger gradient) the greater the acceleration

Example: The motion of a car over 50 s is described in the speed-time graph below.



- Calculate the acceleration of the car during the first 10 s.
- Calculate the distance travelled by the car for the entire 50 s.

Solution

a) $a = ?$	$a = \frac{v - u}{t}$
$v = 8 \text{ ms}^{-1}$	
$u = 0$ (at rest)	$a = \frac{8 - 0}{10}$
$t = 10 \text{ s}$	$a = 0.8 \text{ ms}^{-2}$

- To calculate the distance travelled we cannot use $d = vt$ as the speed is not constant throughout the journey.

The distance travelled = area under the speed-time graph

Area 1 = $\frac{1}{2} (10 \times 8) = 40$ (area of right angled triangle)

Area 2 = $30 \times 8 = 240$ (area of rectangle)

Area 3 = $\frac{1}{2} (10 \times 8) = 40$ (area of right angled triangle)

Total area = $40 + 240 + 40 = 320$ so distance travelled = 320m

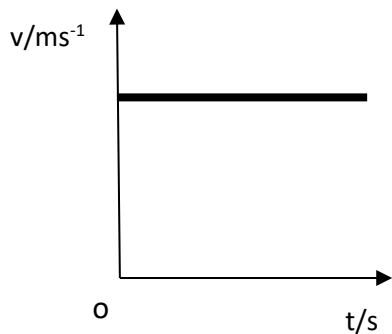
N5

Velocity – Time Graphs

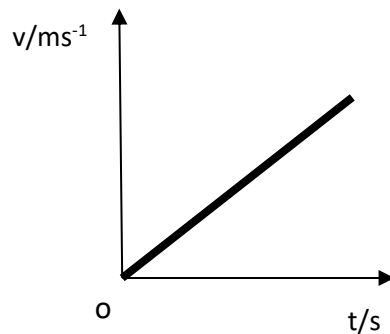
A velocity-time graph is a useful way of describing the motion of an object.

Since velocity is a vector quantity, a velocity-time graph can consider motion in two directions.

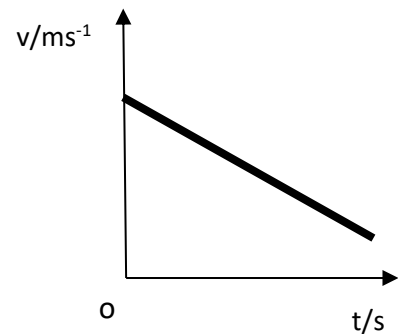
The graphs below illustrate the 3 types of motion you will study.



constant velocity



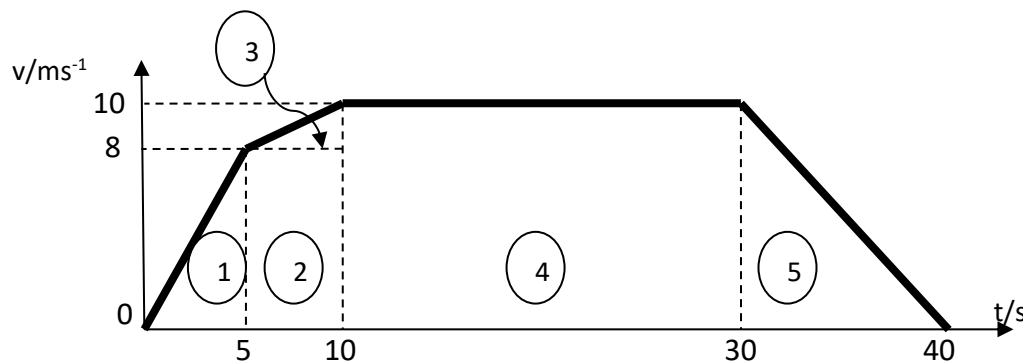
increasing velocity
(constant acceleration)



decreasing velocity
(constant deceleration)

The steeper the line (larger gradient) the greater the acceleration

Example: The motion of a car over 40 s is described in the velocity-time graph below.



- During which stage of the journey is the acceleration of the car the greatest?
- Calculate the deceleration of the car between 30 and 40 s.
- Calculate the displacement of the car for the entire 40 s.

Solution

- a) Between 0 and 5 s. (the gradient of the line is greater than 5 s to 10 s)

b) $a = ?$ $a = \frac{v - u}{t}$
 $v = 0$ $a = \frac{0 - 10}{5}$
 $u = 10 \text{ ms}^{-1}$
 $t = 10 \text{ s}$ $a = -2 \text{ ms}^{-2}$ deceleration = 2 ms^{-2}

- c) Displacement = area under the velocity-time graph

$$\text{Area 1} = \frac{1}{2} (5 \times 8) = 20$$

$$\text{Area 2} = 5 \times 8 = 40$$

$$\text{Area 3} = \frac{1}{2} (5 \times 2) = 5$$

$$\text{Area 4} = 20 \times 10 = 200$$

$$\text{Area 5} = \frac{1}{2} (10 \times 10) = 50$$

$$\text{Total area} = 20 + 40 + 5 + 200 + 50 = 315 \quad \text{so the displacement} = 315 \text{ m}$$

