#### **Glasgow Counts in our Playrooms**







Awareness of Number:

Counting and Subitising

2023/2024















#### Aims



To increase knowledge and understanding of **subitising** and the **five principles of counting.** 

To continue to explore the Glasgow Counts Framework



Identify links with key documents







'Research shows that children who have a good start in mathematical understanding in early years make better progress in school mathematics'

Aubrey and Godfrey 2003







#### Numbers

#### What do we use numbers for?





















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72

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whit down of many sizes. On a three- togged adde, after found a titly gold fory and a green bothe that and "Disprove over" which are muse fit one of the down's the sold.



















The ability to see how many without counting Comes from the Latin word meaning 'suddenly' Very young babies can tell the difference between groups of dots

# What is subitising?

Young children have powerful visual memories Subitising helps children build images for numbers, to visualise and to learn number facts

Essential part of developing number sense











#### Early Level Tracker 1



Estimation & Rounding		Knows they can check estimates by counting within 0-10			Car	n apply subitising the number of	; skills to estimate items in a set		Uses the language of estimation, including more than, less than, fewer than and the same			
	<u>No. word</u> sequences	Say short forward and backward number word sequences within 0-10			Uses e.g.	ordinal numbers I am first/secon	in real life contexts d/third in the line'		Recalls the number sequence forwards and backwards within 0-10			
Aw are nes s of Nu	<u>Numerals</u>	Recognise numerals e.g. points to the number from 0-10		Identify (name) numerals e.g. can respond to question 'what is that number?'		Explains zero is represented as 0		Orders numerals forwards and backwards within 0-10		Identifies number before, after and missing numbers in a sequence within 0-10; beginning to use the language before, after and in-between		
er – Cou ntin g, Qua	<u>Subitising</u>	Identifies 'how many?' in regular dot patterns e.g. dot arrangement/on fingers/five frames/10 frames/dice without counting up to 6			Identifies ' dot arrangen	how many?' in i nent/on fingers/ without coun	regular dot patterns e.g. ive frames/10 frames/dice ting up to 6		Represents amounts in different arrangements e.g.dot arrangement/on fingers/five frames/ 10 frames/dice without counting up to 6			
es & Nu mb er Stru ctur e	Counting	When counting objects understands the order in which we say the numbers is always the same (stable order)		Touch counts one item when each number word is said (1-to-1 correspondence)		When counting objects understands that the number name of the last object counted is the name given to the total number of objects in a set (cardinal principle)		When counting objects understands that the number of objects is not affected by position (order irrelevance)		Counts objects in a set recognising that the appearance of the objects has no effect on the overall total within 0-10 (conservation)		Counts anything e.g. objects at a distance/in a book/sounds/claps within 0-10 (abstract principle)
	<u>Place</u> <u>Value</u>	Explains that zero means there is none of				of a particular quantity		Partitions quan recognises that this does no		itities to 10 into 2 or more parts and ot affect the total e.g. 6 as 3 and 3/2 and 2 and 2		
Addition and Subtraction		Sorts & classifies objects using quantity as an attribute e.g. sets of 1, 2 within 0-10	Com dec the v	ipares 2 sets to tide which has fewest/most within 0-10		the total when 3 is added to an g amount e.g. a er line or height augmentation)	Finds the total when 2 sets are added together within 0-10 (aggregation)		Finds out how many are left when 1 or 2 are taken away within 0-10		Compares to find the difference between sets as a quantity within 0-10	Beginning to count on and back in ones to add and subtract with objects or number line within 0-10
Multiplication and Division		Shares out a group of items into 2 equ Groups objects into matching or natural sets				ual sets within 0-10. of 2 e.g. shoes within 0-10		Begin to identify halves and doubles using concrete materials within 0-10				
Fractions, Decimals and %		Identifies wholes and halves in a social context and uses appropriate language e.g. 'I have eaten half of my banana'			Sr and	olits a whole into explains that eq same s	o smaller parts ual parts are the ize		Understands that a whole can be shared equally and unequally			
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#### Early Level Tracker 1











### Teaching subitising













#### Start with patterns In order





















































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#### **Finger Patterns – Grow, Show, Throw**












































































































































































### <u>Games</u>



### **Subitising: Early Level**



#### Language

How many, dots, patterns, objects, dice, domino, five frame, ten frame, array, tell me what you see

<u>CfE</u>

<u>MNU 0-01a</u> MNU 0-02a

#### **Strategies and Approaches**

Subitising is an essential part of developing number sense. By looking at a group of items, children can start to develop an understanding of how a number is made up (https://valeriefaulknermathclub.files.wordpress.com/2017/05/faulkner\_ainslie\_proof.pdf)

**Perceptual Subitising** is the amount you can instantly recognise without counting. We do this 'naturally' from a young age. It becomes difficult to process the 'full amount' beyond 5 or 6. Beyond 6 you will apply conceptual subitising skills to chunk what you see into smaller values.

**Conceptual Subitising** chunks a larger amount into smaller values. Beyond 6 your mind will process a larger amount e.g. 7 as 5 and 2 or 3 and 4 depending on the representation. This is made possible if the amounts are arranged in an organised way. Therefore effective conceptual subitisers need to be taught to organise their amounts into regular patterns, and 5/10 frames, to make subitising possible. Irregular arrangements are far harder to see and should only be used within 5. Beyond 5 or 6 children will need to adopt regular arrangements to see the amount.



irregular arrangements

•



regular arrangement

10 frame

- **Fingers:** Use fingers everyday to represent quantities. What do you see? How do you know? Can you grow the number adding a finger at a time? Challenge children e.g. make 5 using 2 hands in different ways.
- Dot arrangements: Look for everyday opportunities for learners to see and organise regular structured representations of numbers e.g. objects or dots organised on a five frame or a ten frame, <u>Numicon</u>, dominos , playing cards, an abacus and dice: <u>dice/dominoes/five/ten frames/counters</u> Children should be familiar with all of these ways of seeing patterns of numbers for example by:
  - Playing board games, dominos , cards games and snap games
  - Registering attendance on a five or ten frame/ voting for preferences on the five or ten frame
  - Recording who has had snack on a ten frame, ordering at the 'bakery' on a five or ten frames
- Ordering regular and irregular patterns, on a subitising washing line for example, will give learners the
  opportunity to show they understand the dot patterns represent increasing amounts.

Resources

### **Questions to Enable Higher Order Thinking**

- Can you show me your age using your fingers?
- Can you show me 4 using finger patterns? Can you make it in a different way
- How many on each hand?
- How many circles did you see in the picture?
- Can you tell me without counting?
- What other groups of circles did you see?
- Tell me what you see

### **Barriers to Learning and Misconceptions**

- The spatial arrangement of sets influences how difficult they are to subitise. Children usually find rectangular arrangements easiest, followed by linear, circular, and scrambled arrangements
- If children have poor skill development with number word sequences – ability to say numbers in the correct order, they will find subitising difficult
- Inability to identify and match objects seen with associated number name
- Inability to count on when subitising more than one group

#### **On Track at Transition Statement**

 Represents amounts in different arrangements e.g.dot arrangement/on fingers/five frames/ 10 frames/dice without counting up to 6

#### **Digital Learning**



### Dominos, dice and playing cards



Irregular pattern cards and games



An open frame where children can create their own patterns



Using a five/ten frame create structured patterns



Noticing patterns in nature/real world











### **Resources – Subitising**



### **Common Learning Resources**

- Sets of counters and objects placed in different ٠ arrangements
- Dice ٠
- Dominos ٠
- Subitising cards ٠
- Subitising stones ٠



- Children's fingers ٠
- Playing cards .























### **Online Resources**







Saying how many there are without counting

### **Stories**

- Ten Black Dots by Donald Crews ٠
- The Very Hungry Caterpillar by Eric Carle ٠
- Night Light by Nicholas Blechman ٠
- Dog's Colourful Day by Emma Dodd ٠
- My Very First Book of Numbers by Eric Carle ٠
- Ten Little Rubber Ducks by Eric Carle ٠
- ٠ How Many Snails?: A Counting Book



## Five Principles of counting











## Five Principles of counting



Order irrelevance

## Abstract









# Five Principles of counting



When counting objects understands that the number of objects is not affected by position Counts anything e.g. objects at a distance/in a book/sounds/claps within 0-10











### Early Level Tracker 1



Estimation & Rounding		Knows they can check estimates by counting within 0-10				Can apply subitising skills to estimate the number of items in a set			Uses the language of estimation, including more than, less than, fewer than and the same			
	<u>No. word</u> sequences	Say short forward and backward number word sequences within 0-10				Uses e.g.	ordinal numbers I am first/secon	; in real life contexts d/third in the line'		Recalls the number sequence forwards and backwards within 0-10		
Aw are nes s of Nu mb		Recognise numerals e.g. points to the number from 0-10 'v		Identify (name) numerals e.g. can respond to question 'what is that number?' from 0-10		Explains zero is represented as 0		Orders numerals forwards and backwards within 0-10		Identifies number before, after and missing numbers in a sequence within 0-10; beginning to use the language before, after and in-between		
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nuu es & Nu mb er Stru ctur e	Counting	When counting objects understands the order in which we say the numbers is always the same (stable order)		Touch counts one item when each number word is said (1-to-1 correspondence)		When counting objects understands that the number name of the last object counted is the name given to the total number of objects in a set (cardinal principle)		When counting objects understands that the number of objects is not affected by position (order irrelevance)		in a se appe has n	Counts objects et recognising that the earance of the objects o effect on the overall total within 0-10 (conservation)	Counts anything e.g. objects at a distance/in a book/sounds/claps within 0-10 (abstract principle)
_	<u>Place</u> <u>Value</u>	Explains that zero means there is none of a particular quantity recognises that this does not affect the total e.g									to 10 into 2 or more par ct the total e.g. 6 as 3 a	rts and nd 3/2 and 2 and 2
Addition and Subtraction		Sorts & classifies objects using quantity as an attribute e.g. sets of 1, 2 within 0-10	Com dec the	npares 2 sets to cide which has e fewest/most within 0-10		the total when 3 is added to an g amount e.g. a er line or height augmentation)	Finds the to 2 sets are adde within 0-10 (ag	tal when ed together ggregation)	Finds out how m are left when 1 are taken awa within 0-10	nany or 2 ay	Compares to find the difference between sets as a quantity within 0-10	Beginning to count on and back in ones to add and subtract with objects or number line within 0-10
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## Numbers are recited in the right order (can be forward or backwards).







## Stable-Order Principle

- Vocabulary Number words zero to five, then ten...
- Experiences Number rhymes, songs, games. Using gestures and movement along with sounds and visuals.
- Assessment Consistently recite the number words in order.
- Key questions Which number comes after (forwards)/before (backwards)?









## **Stable-Order Principle**

## Questions to Enable Higher Thinking Skills

- Can you (help me) count on/back from 0 to 10?
- Can we/you take turns counting from 0 forwards to 8, 10 backwards to 3?
- What number comes next?
- I'm going to count down from seven. Can you tell me which number comes next?
- What number comes before/after 3?
- What number is missing?
- Can you help me count as we share out the grapes?
- Do we always say the numbers in the same order? Why?
- What would happen if we counted like this 1, 3, 8 (model a mistake)?
- As we jump forwards/backwards can we count out loud together?
- As we count the dots on the dice/move our piece, can we count out loud together?









# 1:1 Correspondence



## Each object is counted only once.







## One to One Principle

- Vocabulary Number words zero to five, then to ten...
- Experiences Moving objects when counting. Matching items to a picture. Helping to set the snack table.
- Assessment Coordinates movement with the count. Can match one counting word to one action.
- Key questions-

Can you count how many?











## One to One Principle

## **Questions to Enable Higher Order Thinking**

- Can you count the numbers on the dice?
- How can we make these stones easier to count?
- Can we line up in rows of 5 to brush our teeth?
- How many jaggy things are in the bag?







# Cardinality



## The last number you say is the total amount.







## **Cardinal Principle**

- Vocabulary Number words zero to five then 10...
- Experiences Counting groups of objects.
- Assessment Touch and count one to one.
   Use the counting names in order.
   Stop on the last number and recognise that it is the total.
- Key questions How many do you have? How many did you count?







# Order Irrelevance



The order you count the objects in does not matter (as long as you only count each object once).









## The Order Irrelevance Principle

- Vocabulary Number words zero to five then ten...
- Experiences Counting sets of items from left to right, right to left, top to bottom, bottom to top. Counting sets of different coloured items or different objects.
- Assessment Counts each item only once. Counts random arrangements.
  - Key questions How many are there? How many did you count?



















## The Abstraction Principle

- Vocabulary Number words zero to five then to ten.
- Experiences Counting sets of random objects.

- Assessment Counting things that are not objects sounds, actions, steps.
- Key questions I wonder if we can count these altogether?









# Counting Organiser-5 Principles of Counting





Each object is counted only once.



The last number you say is the amount.











# **5** Principles of Counting

**Reviewing Five Counting Principles** 



## Teaching Counting: Reviewing Five Counting Principles









# Principles of counting

In everyday contexts



How many children are in today?









# Principles of counting

In everyday contexts









## Counting

Children need:

- + a purpose for counting and motivation to count;
   + meaningful contexts that make sense;
- to understand how numbers relate to each other;
  to make connections;
- to develop positive attitudes and confidence;
  to use the language...

Adapted from Early Mathematics: A Guide for Improving and Teaching and Learning 2016









Resources

<u>Language</u> Count, set, items, collection, row, group, add, more, make, altogether

<u>MNU 0-01a</u> MNU 0-02a

#### **Strategies and Approaches**

All children are working towards understanding and using the 5 principles of counting (see <u>https://blogs.glowscotland.org.uk/gc/gccleadersofearlylearning/files/2018/11/counting\_a\_dec</u> <u>eptively\_simple\_skill.pdf</u>)

**Counting walks:** take a walk to spot (make predictions beforehand) number of birds (including types), (blue) cars, post boxes, shops, dogs, buses, traffic lights, conkers, things with 4 wheels, pieces of litter, street signs etc. Make time to review how many things were spotted on return to the playroom.

**Board games:** encourage and model: predicting what number will be rolled, counting the dots on the dice once rolled and comparing with the prediction; counting aloud when moving the counter; thinking about what number is needed to get to a desired spot on the board; thinking aloud e.g. 'what do I need to get to the pig'; creating own board games; creating own dice with various arrangements e.g. only 1-5 or a mix of dots and numbers

**Block Play/Water/Sand/Construction:** encourage predicting and counting when building and creating. Model thinking aloud 'how many do I need' as well as actions of counting one-to-one

**Making collections and sorting sets** – how many do you have that are smooth, jaggy, round, noisy? Asking questions about how many...encouraging children to notice and count. Encourage children to think about how they can arrange their sets to make them easier to count e.g. items in rows or regular arrangements (dice, dominos, <u>Numicon</u>)

**Role play** always thinking about meaningful mathematical possibilities for counting e.g. in the bakery have 5 different options of cake displayed with numerals, 5 labelled chairs, purses and coins up to the value of  $\pounds 2$ , an order form which is a 5 frame to colour in

**Counting ourselves:** snack time, lunch time, lining up, as part of singing (children represent the 10 green bottles); using our fingers throughout the day to show amounts

Counting and clapping songs, games , rhymes, syllables every day

**Digital Learning** 

#### **Questions to Enable Higher Order Thinking**

CfE

- How many magpies will we see on our walk today? Can you show me how many you think you will see on your fingers?
- Can you count the numbers on the dice?
- What number do you need to get to the cow?
- How can we make these stones easier to count?
- Can we line up in rows of 5 to brush our teeth?
- How many jaggy things are in the bag?

### Potential Barriers / Misconceptions

- Children may not touch, point to or move each counter/item alongside saying the number name; this will require lots of modelling (one-to-one principle).
- Children may not realise that, when counting, the last number word is the answer to 'How many?' Some may think that the answer to 'How many?' is answered simply by pointing to each counter and counting from 1. It is important for the adult to model identifying the quantity of the collection is the last one counted, and that this stays the same regardless of where we start counting (cardinality and order irrelevance).

### **On Track at Transition Statement**

- Counts objects in a set recognising that the appearance of the objects has no effect on the overall total within 0-10 (conservation)
- Counts anything e.g. objects at a distance/in a book/sounds/claps within 0-10 (abstract principle)











### **Counting on/back**

Counting on/back- use actions, puppets and objects to illustrate counting rhymes and songs

- How many claps, taps, barks, clicks...
- Counting on from various numbers
- Counting back from various numbers
- How many more to make 5, 10...?
- Can you clap five times and count aloud at the same time?



### **Regular and Irregular Patterns**

### Match to appropriate number/number name



Songs

- Ten Green Bottles
- One, two, three, four, five once I caught a fish alive
- One, Two, Buckle My Shoe
- One for Sorrow
- Five Little Speckled Frogs
- One Potato, Two Potato
- There were 10 in a bed
- 5 green speckled frogs
- 5 little ducks
- Johnny works with one hammer

Song planning sheet for intentional interaction

### **Observation of Counting Skills**

When counting objects watch carefully as the child decides how many there are. Does he/she:

- Give an instantaneous response?
- Was it correct/incorrect? Why
- Can the child explain how they worked it out?
- Did they touch each object as they count?
- Move each object as they count?
- Track the objects with their eyes whilst counting in their head?
- Subitise ('just knows')?



### **Resources – Counting**





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Counting Cows by Michelle Medlock Adams

Butterfly Colors and Counting by Jerry Pallotta

One is a Snail, Ten is a Crab by April Pulley Sayre

Chicka Chicka 1, 2, 3 by Bill Martin Jr.

Over in the Meadow by Jill McDonald

On The Launch Pad By Michael Dahl

10 Little Rubber Ducks by Eric Carle

Centipedes 100 Shoes by Tony Ross 1, 2, 3 Little Donkey Rindert Kromhout

Ten Red Apples by Pat Hutchins

One Gorilla by Anthony Browne

How Many Legs By Kes Gray

Feast for 10 by Cathryn Falwell

### **Puddle Play**





### Sets of objects



## Notice and Name!

• Using the tracker, can you observe and identify significant learning in these pictures?









### Linthaugh Nursery













## Meiklewood Nursery



## Lyoncross Nursery



## Meiklewood Nursery




### Glasgow City Mission Children and Family Centre



#### Meiklewood Nursery



#### Meiklewood Nursery





#### Linthaugh Nursery

















#### High Quality Provision













## Meiklewood Nursery







#### Lyoncross Nursery







## Counting and Subitising RtA

Numeracy and mathematical thinking encompasses many different elements including recognition of numerical symbols, verbalising numbers and being able to recognise patterns and shapes.

It involves many different skills such as understanding numbers, counting, problem solving, measuring, sorting and patterning. However, numeracy is not only about developing these skills.

It is also about having the ability to apply these concepts in all areas of life. Therefore, numeracy should be embedded throughout the curriculum and the environment and should not simply be seen as an area on its own.







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# Counting and Subitising HGIOELC



Assessment is an integral part of the learning and teaching and is used effectively to plan high quality learning experiences for all children.

Tracking and monitoring of children's progress is well-understood and used effectively to secure improved outcomes for all children.







Scotland

How good is our early learning and childcare? 'The same part of the brain is used to subitise small quantities as to process symbolic number and so it is an important aspect of number development'

Cantlon et al. 200







# **Glasgow Counts in our Playrooms**







Awareness of Number:

Counting and Subitising

2023/2024













