## Glasgow Counts in our Playrooms



Awareness of Number:
Counting and Subitising 1

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2023 / 2024
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## Aims

To increase knowledge and understanding of subitising and the five principles of counting.

To continue to explore the Glasgow Counts Framework

- Identify links with key documents
'Research shows that children who have a good start in mathematical understanding in early years make better progress in school mathematics'

Aubrey and Godfrey 2003

## Numbers

## What do we use numbers for?




## Subitising



The ability to see how many without counting

## What is subitising?

## Comes from the

 Latin word meaning 'suddenly'Very young babies can tell the difference between groups of dots

Young children have powerful visual memories

(9)THE SCOTTISH (9)ATTAINMENT () CHALLENGE - LTERACY NUMERACY

Essential part of developing number sense

Subitising helps children build images for numbers, to visualise and to learn number facts

Early Level Tracker 1

| Estimation \&Rounding |  | Knows they can check estimates by counting within 0-10 |  |  |  | Can apply subitising skills to estimate the number of items in a set |  |  |  | Uses the language of estimation, including more than, less than, fewer than and the same |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Aw are nes $s$ of Nu .... er Cou ntin g, Qua ntitit | No. word sequences | Say short forward and backward number word sequences within 0-10 |  |  |  | Uses ordinal numbers in real life contexts e.g. I am first/second/third in the line' |  |  |  | Recalls the number sequence forwards and backwards within 0-10 |  |  |
|  | Numerals | Recognise numerals e.g. points to the number from 0-10 |  | Identify (name) numerals e.g. can respond to question 'what is that number?' |  | Explains zero  <br> is represented as 0 Orders numerals forwards <br> and backwards <br> within 0-10 |  |  |  | Identifies number before, after and missing numbers in a sequence within 0-10; beginning to use the language before, aftor and in-hotwoon |  |  |
|  | Subitising | Identifies 'how many?' in regular dot patterns e.g. dot arrangement/on fingers/five frames/10 frames/dice without counting up to 6 |  |  |  | Identifies 'how many?' in irregular dot patterns e.g. dot arrangement/on fingers/five frames/10 frames/dice without counting up to 6 |  |  |  | Represents amounts in different arrangements e.g.dot arrangement/on fingers/five frames/ 10 frames/dice without counting up to 6 |  |  |
|  | Counting | When counting objects understands the order in which we say the numbers is always the same (stable order) |  | Touch coun item when number word <br> (1-to-1 correspond | one each is said <br> nce) | When counting objects understands that the number name of the last object counted is the name given to the total number of objects in a set (cardinal principle) |  | When counting objects understands that the number of objects is not affected by position (order irrelevance) |  |  | Counts odjects et recognising that the earance of the objects no effect on the overal total within 0-10 (conservation) | Counts anything e.g. objects at a distance/in a book/sounds/claps within 0-10 (abstract principle) |
|  | Place Value | Explains that zero means there is none of a particular quantity |  |  |  |  |  | Partitions quantities to 10 into 2 or more parts and recognises that this does not affect the total e.g. 6 as 3 and $3 / 2$ and 2 and 2 |  |  |  |  |
| Addition and Subtraction |  | Sorts \& classifies objects using quantity as an attribute <br> e.g. sets of 1, 2 within 0-10 | Compares 2 sets to decide which has the fewest/most within 0-10 |  | Finds the total when 1,2 or 3 is added to an existing amount e.g. a number line or height chart (augmentation) |  | Finds the total when 2 sets are added together within 0-10 (aggregation) |  | Finds out how many are left when 1 or 2 are taken away within 0-10 |  | Compares to find the difference between sets as a quantity within 0-10 | Beginning to count on and back in ones to add and subtract with objects or number line within 0-10 |


| $\frac{\text { Multiplication }}{\text { Shares out a group of items into } 2 \text { equal sets within 0-10. }}$ |  |
| :---: | :---: |
| $\underline{\text { and Division }}$ | Groups objects into matching or natural sets of 2 e.g. shoes within 0-10 |

Begin to identify halves and doubles using concrete materials within 0-10

Fractions, Decimals and \%

Identifies wholes and halves in a social context and uses appropriate language e.g. 'I have eaten half of my banana'

Splits a whole into smaller parts and explains that equal parts are the same size

Understands that a whole can be shared equally and unequally

## Early Level Tracker 1

Identifies 'how many?' in regular dot patterns e.g. dot arrangement/on fingers/five frames/10 frames/dice without counting up to 6

Identifies 'how many?' in irregular dot patterns e.g. dot arrangement/on fingers/five frames/10 frames/dice without counting up to 6

Represents amounts in different arrangements e.g.dot arrangement/on fingers/five frames/ 10 frames/dice without counting up to 6

## Teaching subitising

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## Subitising

## Start with patterns In order



1

## Subitising



2


## Regular / Domino Patterns

## What do you see?

How do
you see it?

## Regular / Domino Patterns

What do
you see?


4

How do
you
see it?

## Regular / Domino Patterns

## What do <br> you see?

How do
you see it?


5

## Regular / Domino Patterns



## Random Dot Patterns



## Random Dot Patterns



3


## Random Dot Patterns



## 4


www.glasgow.gov.uk

## Random Dot Patterns



## $\square$



## Random Dot Patterns



## 6



## Subitising


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Subitising

Finger Patterns -Grow, Show, Throw


## Subitising



## Subitising

## 10 Frames - Arrays


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## Subitising

## What do you see?

10 Frames - Arrays

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## Subitising

## What do you see?

## 10 Frames - Arrays




## Subitising

## What do

10 Frames - Arrays



## Subitising

## What do

10 Frames - Arrays



## Subitising

## What do

10 Frames - Arrays


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(1) CHALLENGE

## Subitising

## What do

10 Frames - Arrays


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(2)ATAINMENT
(1) CHALLENGE

## Subitising

## 10 Frames - Arrays



## Subitising

## 10 Frames - Arrays



What do
you see?

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## Subitising


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## Subitising



## Subitising

## Games



Subitising


## Subitising



## Subitising

Games

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## Subitising

Games


## Subitising: Early Level

## Language <br> How many, dots, patterns, objects, dice, domino, five

## Strategies and Approaches

## Subitising is an essential part of developing number sense. By looking at a group of items, children can start to develop an understanding of how a number is made up <br> (https://valeriefaulknermathclub.files.wordpress.com/2017/05/faulkner_ainslie_proof.pdf)

Perceptual Subitising is the amount you can instantly recognise without counting. We do this 'naturally' from a young age. It becomes difficult to process the 'full amount' beyond 5 or 6 . Beyond 6 you will apply conceptual subitising skills to chunk what you see into smaller values.

Conceptual Subitising chunks a larger amount into smaller values. Beyond 6 your mind will process a larger amount e.g. 7 as 5 and 2 or 3 and 4 depending on the representation. This is made possible if the amounts are arranged in an organised way. Therefore effective conceptual subitisers need to be taught to organise their amounts into regular patterns, and 5/10 frames, to make subitising possible. Irregular arrangements are far harder to see and should only be used within 5 . Beyond 5 or 6 children will need to adopt regular arrangements to see the amount.

irregular arrangements

regular arrangement


10 frame

- Fingers: Use fingers everyday to represent quantities. What do you see? How do you know? Can you grow the number adding a finger at a time? Challenge children e.g. make 5 using 2 hands in different ways.
- Dot arrangements: Look for everyday opportunities for learners to see and organise regular structured representations of numbers e.g. objects or dots organised on a five frame or a ten frame, Numicon, dominos , playing cards, an abacus and dice: dice/dominoes/five/ten frames/counters Children should be familiar with all of these ways of seeing patterns of numbers for example by:
- Playing board games, dominos, cards games and snap games
- Registering attendance on a five or ten frame/ voting for preferences on the five or ten frame
- Recording who has had snack on a ten frame, ordering at the 'bakery' on a five or ten frames
- Ordering regular and irregular patterns, on a subitising washing line for example, will give learners the opportunity to show they understand the dot patterns represent increasing amounts.


## Resources

## Digital Learning

## Questions to Enable Higher Order Thinking

- Can you show me your age using your fingers?
- Can you show me 4 using finger patterns? Can you make it in a different way
- How many on each hand?
- How many circles did you see in the picture?
- Can you tell me without counting?
- What other groups of circles did you see?
- Tell me what you see


## Barriers to Learning and Misconceptions

- The spatial arrangement of sets influences how difficult they are to subitise. Children usually find rectangular arrangements easiest, followed by linear, circular, and scrambled arrangements
- If children have poor skill development with number word sequences - ability to say numbers in the correct order, they will find subitising difficult
- Inability to identify and match objects seen with associated number name
- Inability to count on - when subitising more than one group


## On Track at Transition Statement

- Represents amounts in different arrangements e.g.dot arrangement/on fingers/five frames/ 10 frames/dice without counting up to 6

Dominos, dice and playing cards


Irregular pattern cards and games


An open frame where children can create their own patterns


Using a five/ten frame create structured patterns


How many children are here today?


## Resources - Subitising

## Common Learning Resources

- Sets of counters and objects placed in different arrangements
- Dice
- Dominos
- Subitising cards
- Subitising stones
- Rekenrek
- Children's fingers
- Playing cards



Who has seven?


## Online Resources



Hidden Jewels
Age 3 to 5
Saying how many there are without counting

## Stories

- Ten Black Dots by Donald Crews
- The Very Hungry Caterpillar by Eric Carle

- Night Light by Nicholas Blechman
- Dog's Colourful Day by Emma Dodd
- My Very First Book of Numbers by Eric Carle
- Ten Little Rubber Ducks by Eric Carle
- How Many Snails?: A Counting Book


## Five Principles of counting



## Five Principles of counting

## Stable Order

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1-\text { to }-1
$$

correspondence

## Cardinal

## irrelevance



## Five Principles of counting

Stable Order
When counting objects
understands the order
in which we say
the numbers
is always the same


Early Level Tracker 1


| $\frac{\text { Multiplication }}{\text { and Division }}$ | Shares out a group of items into 2 equal sets within 0-10. <br> Groups objects into matching or natural sets of 2 e.g. shoes within 0-10 |
| :---: | :---: |

Begin to identify halves and doubles using concrete materials within 0-10

Fractions, Decimals and \%

Identifies wholes and halves in a social context and uses appropriate language e.g. 'I have eaten half of my banana'

Splits a whole into smaller parts and explains that equal parts are the same size

Understands that a whole can be shared equally and unequally

## Stable Order

## $0,1,2,3,4,5 \ldots \ldots$.

Numbers are recited in the right order (can be forward or backwards).

## Stable-Order Principle

- Vocabulary Number words zero to five, then ten...
- Experiences - Number rhymes, songs, games. Using gestures and movement along with sounds and visuals.
- Assessment - Consistently recite the number words in order.
- Key questions - Which number comes after
 (forwards)/before (backwards)?


## Stable-Order Principle

## - Questions to Enable Higher Thinking Skills

- Can you (help me) count on/back from 0 to 10 ?
- Can we/you take turns counting from 0 forwards to 8,10 backwards to 3 ?
- What number comes next?
- I'm going to count down from seven. Can you tell me which number comes next?
- What number comes before/after 3?
- What number is missing?
- Can you help me count as we share out the grapes?
- Do we always say the numbers in the same order? Why?
- What would happen if we counted like this $1,3,8$ (model a mistake)?
- As we jump forwards/backwards can we count out loud together?

- As we count the dots on the dice/move our piece, can we count out loud together?


## 1:1 Correspondence



Each object is counted only once.

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## One to One Principle

- Vocabulary - Number words zero to five, then to ten...
- Experiences - Moving objects when counting. Matching items to a picture. Helping to set the snack table.
- Assessment - Coordinates movement with the count. Can match one counting word to one action.
- Key questions-

Can you count how many?


## One to One Principle

## Questions to Enable Higher Order Thinking

- Can you count the numbers on the dice?
- How can we make these stones easier to count?
- Can we line up in rows of 5 to brush our teeth?
- How many jaggy things are in the bag?



## Cardinality

## 10



The last number you say is the total amount.


## Cardinal Principle

- Vocabulary Number words zero to five then 10...
- Experiences - Counting groups of objects.
- Assessment -

Touch and count one to one.
Use the counting names in order. Stop on the last number and recognise that it is the total.

- Key questions - How many do you have? How many did you count?


## Order Irrelevance



The order you count the objects in does not matter (as long as you only count each object once).


## The Order Irrelevance Principle

- Vocabulary - Number words zero to five then ten...
- Experiences - Counting sets of items from left to right, right to left, top to bottom, bottom to top. Counting sets of different coloured items or different objects.
- Assessment - Counts each item only once. Counts random arrangements.

How many are there?

- Key questions - How many did you count?


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## The Abstraction Principle

- Vocabulary -

Number words zero to five then to ten.

- Experiences - Counting sets of random objects.
- Assessment - Counting things that are not objects sounds, actions, steps.
- Key questions - I wonder if we can count these altogether?



# Counting Organiser5 Principles of Counting 

## Stable Order



The order you count the objects in does not matter.
(As long as you only count (As long as you only count each object once!)

1:1 Correspondence


## Each object is counted only once.



Literacy numeracy

## 5 Principles of Counting

## Teaching Counting: Reviewing Five Counting Principles

more videos al Center on<br>- IINTENSIVE INTERVENTION



# Principles of counting 

In everyday contexts


> How many children are in today?


1 - to -1 correspondence


## Order Irrelevance

## Abstract

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# Principles of counting 

## In everyday contexts

5 Little Monkeys



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1 \text { - to }-1 \text { correspondence }
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Cardinal

## Order Irrelevance

## Abstract

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- CHALLENGE
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## Counting

## Children need:

+ a purpose for counting and motivation to count;
+ meaningful contexts that make sense;
+ to understand how numbers relate to each other;
+ to make connections;
+ to develop positive attitudes and confidence;
+ to use the language...

Adapted from Early Mathematics: A Guide for Improving and Teaching and Learning 2016

## Counting : Early Level

Language Count, set, items, collection, row, group, add, more, make, altogether $\quad$| CfE | $\frac{\text { MNU 0-01a }}{\text { MNU 0-02a }}$ |
| :--- | :--- |

## Strategies and Approaches

## All children are working towards understanding and using the 5 principles of counting (see

 https://blogs.glowscotland.org.uk/gc/gccleadersofearlylearning/files/2018/11/counting a dec eptively_simple_skill.pdf)Counting walks: take a walk to spot (make predictions beforehand) number of birds (including types), (blue) cars, post boxes, shops, dogs, buses, traffic lights, conkers, things with 4 wheels, pieces of litter, street signs etc. Make time to review how many things were spotted on return to the playroom.

Board games: encourage and model: predicting what number will be rolled, counting the dots on the dice once rolled and comparing with the prediction; counting aloud when moving the counter; thinking about what number is needed to get to a desired spot on the board; thinking aloud e.g. 'what do I need to get to the pig'; creating own board games; creating own dice with various arrangements e.g. only 1-5 or a mix of dots and numbers

Block Play/Water/Sand/Construction: encourage predicting and counting when building and creating. Model thinking aloud 'how many do I need' as well as actions of counting one-to-one

Making collections and sorting sets - how many do you have that are smooth, jaggy, round, noisy? Asking questions about how many...encouraging children to notice and count. Encourage children to think about how they can arrange their sets to make them easier to count e.g. items in rows or regular arrangements (dice, dominos, Numicon)

Role play always thinking about meaningful mathematical possibilities for counting e.g. in the bakery have 5 different options of cake displayed with numerals, 5 labelled chairs, purses and coins up to the value of $£ 2$, an order form which is a 5 frame to colour in

Counting ourselves: snack time, lunch time, lining up, as part of singing (children represent the 10 green bottles); using our fingers throughout the day to show amounts

Counting and clapping songs, games, rhymes, syllables every day
Digital Learning

## Questions to Enable Higher Order Thinking

- How many magpies will we see on our walk today? Can you show me how many you think you will see on your fingers?
- Can you count the numbers on the dice?
- What number do you need to get to the cow?
- How can we make these stones easier to count?
- Can we line up in rows of 5 to brush our teeth?
- How many jaggy things are in the bag?


## Potential Barriers / Misconceptions

- Children may not touch, point to or move each counter/item alongside saying the number name; this will require lots of modelling (one-to-one principle).
- Children may not realise that, when counting, the last number word is the answer to 'How many?' Some may think that the answer to 'How many?' is answered simply by pointing to each counter and counting from 1 . It is important for the adult to model identifying the quantity of the collection is the last one counted, and that this stays the same regardless of where we start counting (cardinality and order irrelevance).


## On Track at Transition Statement

- Counts objects in a set recognising that the appearance of the objects has no effect on the overall total within 0-10 (conservation)
- Counts anything e.g. objects at a distance/in a book/sounds/claps within 0-10 (abstract principle)



## Numicon Number Line



## Counting on/back

Counting on/back- use actions, puppets and objects to illustrate counting rhymes and songs

- How many claps, taps, barks, clicks...
- Counting on from various numbers
- Counting back from various numbers
- How many more to make 5,10 ...?
- Can you clap five times and count aloud at the same time?
?



## Songs

- Ten Green Bottles
- One, two, three, four, five once I caught a fish alive
- One, Two, Buckle My Shoe
- One for Sorrow
- Five Little Speckled Frogs
- One Potato, Two Potato
- There were 10 in a bed
- 5 green speckled frogs
- 5 little ducks
- Johnny works with one hammer

Song planning sheet for intentional interaction

## Regular and Irregular Patterns

Match to appropriate number/number name


Observation of Counting Skills

When counting objects watch carefully as the child decides how many there are. Does he/she:

- Give an instantaneous response?
- Was it correct/incorrect? Why
- Can the child explain how they worked it out?
- Did they touch each object as they count?
- Move each object as they count?
- Track the objects with their eyes whilst counting in their head?
- Subitise ('just knows')?


## Resources - Counting



## Notice and Name!

- Using the tracker, can you observe and identify significant learning in these pictures?


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Meiklewood Nursery



Meiklewood Nursery


## Meiklewood Nursery




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High Quality Provision


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## Meiklewood Nursery



Lyoncross Nursery


## Counting and Subitising RtA

Numeracy and mathematical thinking encompasses many different elements including recognition of numerical symbols, verbalising numbers and being able to recognise patterns and shapes.
It involves many different skills such as understanding numbers, counting, problem solving, measuring, sorting and patterning. However, numeracy is not only about developing these skills.

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It is also about having the ability to apply these concepts in all areas of life. Therefore, numeracy should be embedded throughout the curriculum and the environment and should not simply be seen as an area on its own.
'The same part of the brain is used to subitise small quantities as to process symbolic number and so it is an important aspect of number development'

Cantlon et al. 200

## Contacts

Ana Nikolaidis Gould: gw22gouldanastasia@glow.sch.uk


- Twitter: @GlasgowLEL
- Blog: Google Leaders of Early Learning https://blogs.glowscotland.org.uk/gc/gccleadersofearlylearning/


## Glasgow Counts in our Playrooms



