

*Percentages - Lesson 2*

## Original Values (Reverse Percentages)

### LI

- Work out original values when told the new value and percentage change.

### SC

- Writing percentages as decimals.
- Proportion.

### Reminders

$$100 \% = 1$$

$$73 \% = 100 \% - 27 \% = 0.73$$

$$128 \% = 100 \% + 28 \% = 1.28$$

Example 1 (Calculator)

A property is currently worth £ 154 000. This is after a 3 % increase over a year. What was the original price ?

103 % of the original cost (£  $C$ ) corresponds to 154 000

$$103 \% \text{ of } C = 154\,000$$

$$1.03 \times C = 154\,000$$

$$C = 154\,000 \div 1.03$$

$$\underline{C = 149\,514.563 \dots}$$

Original price : £ 149 514 . 56

Example 2 (Calculator)

The current world record time for the men's 400 m is 43 . 03 seconds.

If this is a decrease of 9 . 6 % of the world record set in 1924, what was the world record in 1924 ?

(100 - 9 . 6) % of 1924 time corresponds to 43 . 03

$$90 . 4 \text{ \% of } T = 43 . 03$$

$$0 . 904 \times T = 43 . 03$$

$$T = 43 . 03 \div 0 . 904$$

$$\underline{T = 47 . 599 \dots}$$

1924 record : 47 . 60 s

Example 3 (Non - Calc)

The value of a washing machine goes down by 25 %.  
If it now costs £ 144, what was the original cost ?

75 % of the original cost (£ C) corresponds to 144

$$75 \% \text{ of } C = 144$$

$$(3/4) \times C = 144$$

$$C = 144 \div (3/4)$$

$$C = 144 \times (4/3)$$

$$\underline{C = 192}$$

Original price : £ 192

Example 4 (Non - Calc)

A wise man buys a pencil. He then sells it for 20 p.  
If this amount is 1 600 % of the original price, how much did he buy it for ?

1 600 % of the original cost (£ C) corresponds to 20 p

$$1\,600\% \text{ of } C = 20$$

$$16 \times C = 20$$

$$C = \frac{20}{16}$$

$$C = \frac{5}{4}$$

$$\underline{C = 1.25}$$

Original price : 1.25 p

### Questions (Calculator PERMITTED)

- 1 A painting has increased in value by 5% since it was bought in 2005. At auction in 2013 it was sold for £13 650. How much did it cost in 2005?
- 2 The average attendance at a football ground has decreased by 10% since last year. The average attendance this year is 36 800. What was the average attendance last year?
- 3 A TV costs £900 after VAT is added at 20%. What was the cost before VAT?
- 4 A house appreciated in value by 2% over the course of a year. At the end of the year it was worth £117 300. How much was it worth at the start of the year?
- 5 A car has depreciated by 40% since it was bought. It is currently worth £1800. How much did the car originally cost?
- 6 Michael received a 3% pay rise, increasing his annual wage to £26 780. What was his wage before the increase?
- 7 A 540g cereal box claims that it has 20% extra free. What does a normal box weigh?
- 8 The value of a car has decreased by 12%. It is currently worth £7480. What was the original value?
- 9 The population of a Scottish town has risen by 3.5% over the past 10 years. If the population now stands at 22 300, what was it 10 years ago? Answer to the nearest hundred.
- 10 The rate of inflation in a particular year was 2.8%. At the end of the year a TV was priced at £635.99. If the cost had risen in line with inflation, what did it cost at the start of the year?
- 11 John put money in an account offering compound interest at 3.2% per annum. After three years it was worth £604.51. How much did he initially place in the account?

### Questions (Calculator **FORBIDDEN**)

- 1 A computer cost £240 after VAT at 20% was added. What was the cost before VAT?
- 2 Mike took his family out for dinner. He paid £132 for the meal including a 10% tip. What was the price of the meal without the tip?
- 3 A dress cost £72 in a sale where all items were reduced by 20%. What was the price of the dress before the sale?
- 4 Pensioners get 40% off of the price of a full adult train ticket. A pensioner pays £21 for a particular journey. What would be the cost of a full adult ticket for the same journey?
- 5 The population of a small village decreased by 25% last year. There are now 225 people. What was the population last year?
- 6 Jamie bought a computer last year. It depreciated by 12.5% over the course of the year and is now valued at £315. How much was it worth when he bought it?
- 7 The cost of LPG has increased by 15% since last year. This year it cost Heather £460 for a full tank of gas. How much would it have cost her last year?



**Answers**

- |                |          |
|----------------|----------|
| 1) £ 13 000    | 1) £ 200 |
| 2) 40 888      | 2) £ 120 |
| 3) £ 750       | 3) £ 90  |
| 4) £ 115 000   | 4) £ 35  |
| 5) £ 3 000     | 5) £ 300 |
| 6) £ 26 000    | 6) £ 360 |
| 7) 450 g       | 7) £ 400 |
| 8) £ 8 500     |          |
| 9) 21 500      |          |
| 10) £ 618 . 67 |          |
| 11) £ 550      |          |