

*Surds - Lesson 3*

## Simplifying Surds 3 - Multiplying Brackets

### LI

- Simplify surds using the 1<sup>st</sup> and 2<sup>nd</sup> Rules of Surds.

### SC

- 1<sup>st</sup> and 2<sup>nd</sup> Rules of Surds.
- Expanding Brackets (Foil).

Example 1

Multiply the brackets and simplify :

$$\sqrt{3} (7 - \sqrt{3})$$

$$= \sqrt{3} \times 7 - \sqrt{3} \times \sqrt{3}$$

$$= 7\sqrt{3} - 3$$

Example 2

Multiply the brackets and simplify :

$$\begin{aligned} & \sqrt{18} (\sqrt{2} - \sqrt{3}) \\ = & \sqrt{9 \times 2} (\sqrt{2} - \sqrt{3}) \\ = & 3\sqrt{2} (\sqrt{2} - \sqrt{3}) \\ = & 3\sqrt{2} \times \sqrt{2} - 3\sqrt{2} \times \sqrt{3} \\ = & 3 \times 2 - 3\sqrt{6} \\ = & \boxed{6 - 3\sqrt{6}} \end{aligned}$$

Example 3

Multiply the brackets and simplify :

$$\begin{aligned} & (\sqrt{5} - 2)(\sqrt{5} + 6) \\ &= \sqrt{5} \times \sqrt{5} + 6 \times \sqrt{5} - 2 \times \sqrt{5} - 12 \\ &= 5 + 6\sqrt{5} - 2\sqrt{5} - 12 \\ &= 4\sqrt{5} - 7 \end{aligned}$$

1) Multiply the brackets and simplify.

**a**  $\sqrt{2}(3 + \sqrt{2})$       **b**  $\sqrt{5}(\sqrt{5} - 1)$       **c**  $\sqrt{7}(5 - \sqrt{7})$       **d**  $2\sqrt{3}(6 - \sqrt{3})$   
**e**  $3(\sqrt{2} - \sqrt{5})$       **f**  $7(\sqrt{3} - 8)$       **g**  $\sqrt{8}(\sqrt{2} - \sqrt{3})$       **h**  $\sqrt{6}(3 - 2\sqrt{2})$

2) Multiply the brackets and simplify.

**a**  $(\sqrt{2} + 1)(\sqrt{2} - 3)$       **b**  $(\sqrt{3} - 2)(\sqrt{3} + 4)$       **c**  $(\sqrt{3} - 5)(\sqrt{3} + 5)$   
**d**  $(\sqrt{2} - \sqrt{7})(\sqrt{2} + \sqrt{7})$       **e**  $(\sqrt{5} + 1)^2$       **f**  $(\sqrt{3} - \sqrt{2})^2$   
**g**  $(\sqrt{7} - 5)^2$       **h**  $3(\sqrt{5} + 1)(\sqrt{5} + 4)$

3) A rectangle has sides of length  $(3 + \sqrt{2})$  cm and  $(3 - \sqrt{2})$  cm.

Calculate:

**a** the area of the rectangle      **b** the length of a diagonal.

**Answers**

<b>1 a</b>	$3\sqrt{2} + 2$	<b>2 a</b>	$-1 - 2\sqrt{2}$	<b>3 a</b>	$7 \text{ cm}^2$
<b>b</b>	$5 - \sqrt{5}$	<b>b</b>	$2\sqrt{3} - 5$	<b>b</b>	$\sqrt{22} \text{ cm}$
<b>c</b>	$5\sqrt{7} - 7$	<b>c</b>	$-22$		
<b>d</b>	$12\sqrt{3} - 6$	<b>d</b>	$-5$		
<b>e</b>	$3\sqrt{2} - 3\sqrt{5}$	<b>e</b>	$6 + 2\sqrt{5}$		
<b>f</b>	$7\sqrt{3} - 56$	<b>f</b>	$5 - 2\sqrt{6}$		
<b>g</b>	$4 - 2\sqrt{6}$	<b>g</b>	$32 - 10\sqrt{7}$		
<b>h</b>	$3\sqrt{6} - 4\sqrt{3}$	<b>h</b>	$27 + 15\sqrt{5}$		