

Advanced Trigonometry - Lesson 7

Trigonometry with Bearings

LI

- Solve problems involving bearings.

SC

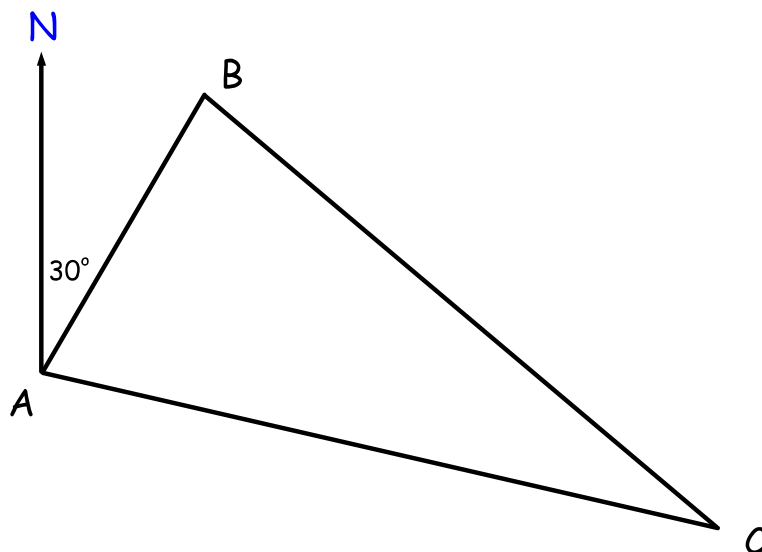
- Basic angle properties.
- Sine and Cosine Rules.

Bearings

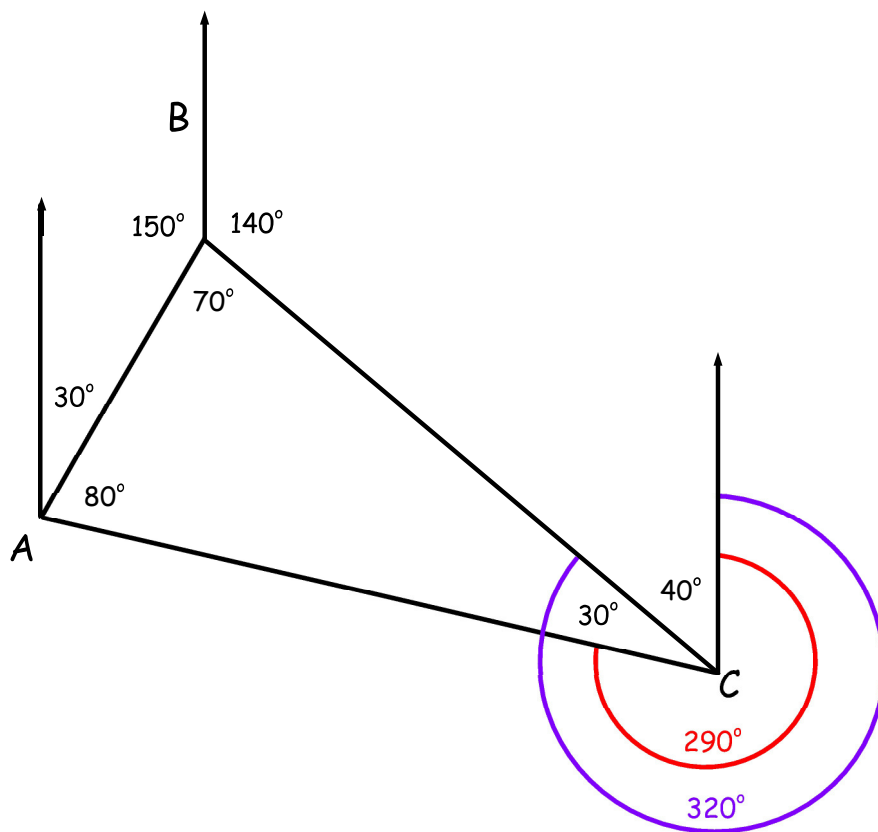
- Measured from a North line.
- Measured clockwise.
- Always written with 3 numbers.

Example 1

Point B is on a bearing of 320° from C; point A is on a bearing of 290° from C.

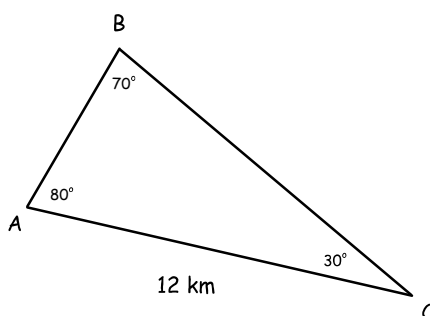
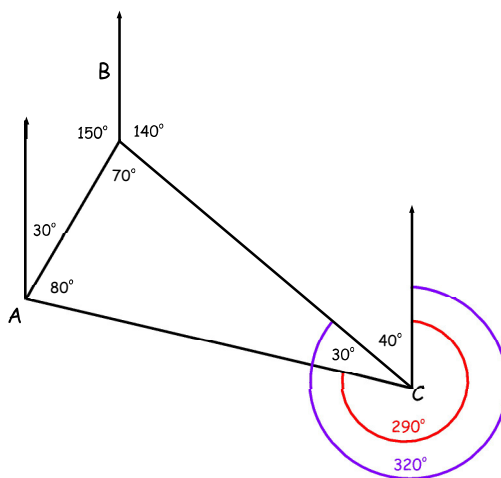


Calculate the sizes of all 3 missing angles inside the triangle.



Example 2

In Example 1, given that side $AC = 12$ km, calculate the length of AB (to 3 s.f.).



Sine Rule for length

$$\frac{a}{\sin A^\circ} = \frac{b}{\sin B^\circ} = \frac{c}{\sin C^\circ}$$

$A^\circ = 80^\circ$, $a =$ $B^\circ = 70^\circ$, $b = 12$ $C^\circ = 30^\circ$, $c =$

$$\frac{c}{\sin C^\circ} = \frac{b}{\sin B^\circ}$$

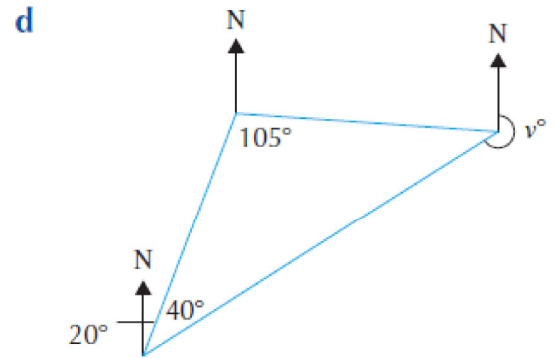
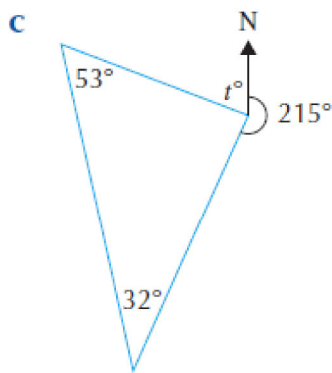
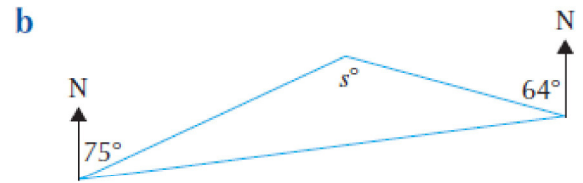
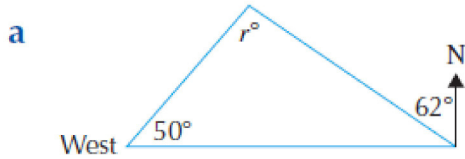
$$\frac{c}{\sin 30^\circ} = \frac{12}{\sin 70^\circ}$$

$$c = \frac{(12 \times \sin 30^\circ)}{\sin 70^\circ}$$

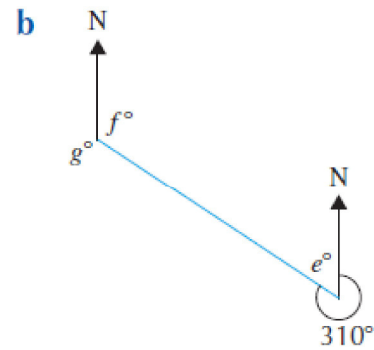
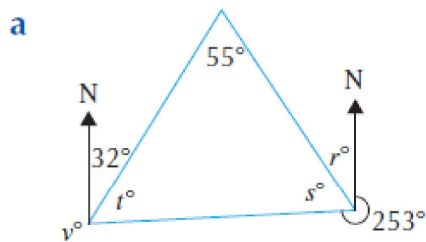
$$c = 6.39 \text{ km}$$

Questions

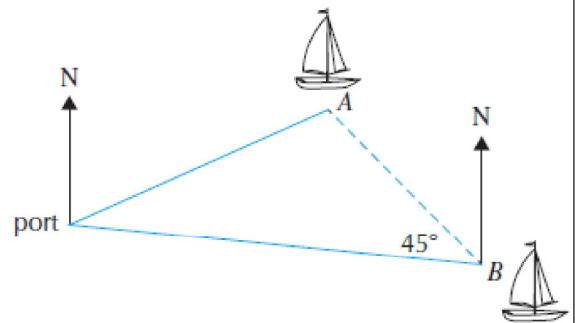
1 In each triangle shown find the missing angles labelled.



2 Calculate the missing angle shown in each diagram.



3 Boat A is on a bearing of 076° from port, boat B is on a bearing of 099° . Calculate the bearing of boat A from boat B.

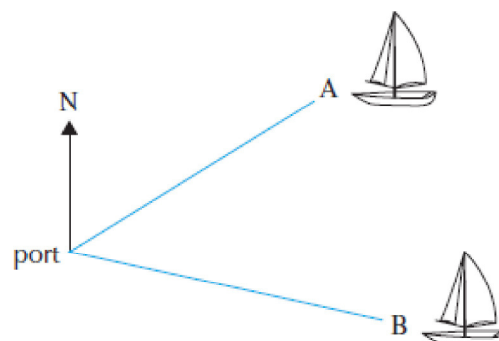


Questions

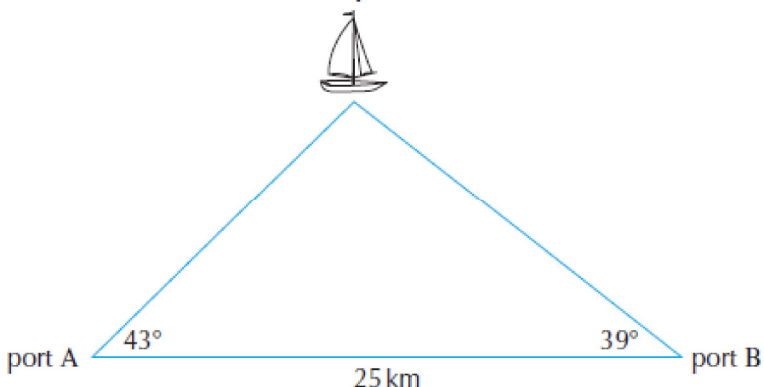
For each question, give your answer to 2 decimal places.

- 2 A ship sails east for 14.5 km then on a bearing of 130° for 11 km. Calculate the distance the boat has sailed.

- 3 Two yachts set off from the same port as shown in the diagram. Yacht A sails 10.7 km on a bearing of 053° , while yacht B sails 11.2 km on a bearing of 112° . Calculate the distance between the two yachts.



- 4 Port B is 25 km east of port A.



- a Calculate the distance of the ship to the nearer port.
- b Find the bearing the ship must sail to reach this port.

- 5 An airplane flies 170 miles from point X at a bearing of 125° , and then turns and flies at a bearing of 230° for 90 miles. How far is the plane from point X?

- 6 A ship is being followed by two submarines, A and B, 3.8 km apart, with A due east of B. If A is on a bearing of 165° from the ship and B is on the bearing of 205° from the ship, find the distance from the ship to both submarines.

Answers

1 a 102°

b 139°

c 50°

d 240°

2 a **r** 23° , **s** 84° , **t** 41° , **v** 287°

b **e** 50° , **f** 130° , **g** 230°

3 324°

2 23.99 km

3 10.79 km

4 a 15.89 km

b 227°

5 170.53 miles

6 5.36 km, 5.71 km