

*Advanced Trigonometry - Lesson 4*

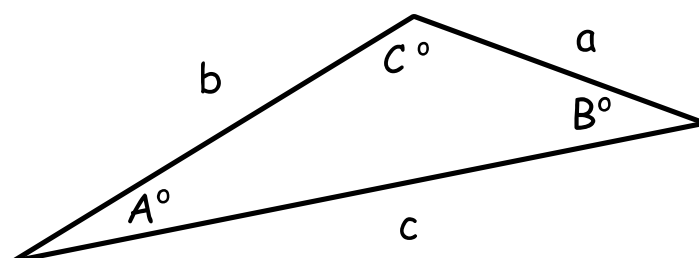
## Sine Rule (Angle)

LI

- Use the Sine Rule to find a missing angle in any triangle.

SC

- Use a calculator properly.

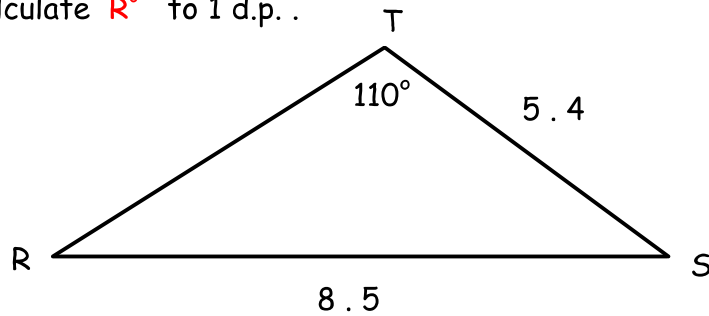
Sine Rule

For **finding angles**, better to use Sine Rule with **Sines on top** :

$$\frac{\sin A^\circ}{a} = \frac{\sin B^\circ}{b} = \frac{\sin C^\circ}{c}$$

## Strategy for Finding Missing Angle

- Sketch triangle and label **all** sides and angles
- Write down Sine Rule (with **Sines on top**)
- Tick the things you know
- Solve for missing angle

Example 1Calculate  $R^\circ$  to 1 d.p. .

$$\frac{\sin R^\circ}{r} = \frac{\sin S^\circ}{s} = \frac{\sin T^\circ}{t}$$

$R^\circ =$	,	$r = 5.4$
$S^\circ =$	,	$s =$
$T^\circ = 110^\circ$	,	$t = 8.5$

$$\frac{\sin R^\circ}{r} = \frac{\sin T^\circ}{t}$$

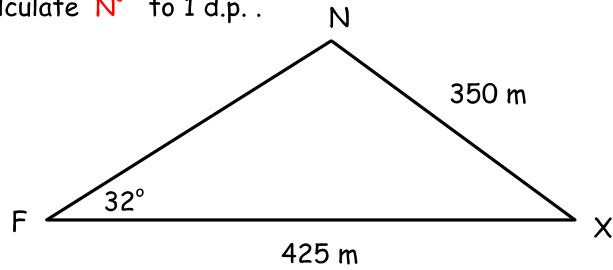
$$\frac{\sin R^\circ}{5.4} = \frac{\sin 110^\circ}{8.5}$$

$$\sin R^\circ = \frac{(5.4 \times \sin 110^\circ)}{8.5}$$

$$\sin R^\circ = 0.596 \dots$$

$$R^\circ = \sin^{-1}(0.596 \dots)$$

$$R^\circ = 36.7^\circ$$

Example 2Calculate  $N^\circ$  to 1 d.p. .

$$\frac{\sin X^\circ}{x} = \frac{\sin N^\circ}{n} = \frac{\sin F^\circ}{f}$$

$$X^\circ = \quad , x =$$

$$N^\circ = \quad , n = 425 \text{ m}$$

$$F^\circ = 32^\circ , f = 350 \text{ m}$$

$$\frac{\sin N^\circ}{n} = \frac{\sin F^\circ}{f}$$

$$\frac{\sin N^\circ}{425} = \frac{\sin 32^\circ}{350}$$

$$\sin N^\circ = \frac{(425 \times \sin 32^\circ)}{350}$$

$$\sin N^\circ = 0.643 \dots$$

$$N^\circ = \sin^{-1}(0.643 \dots)$$

$$N^\circ = 40.1^\circ$$

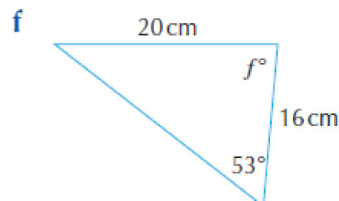
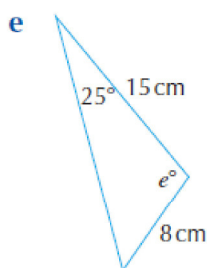
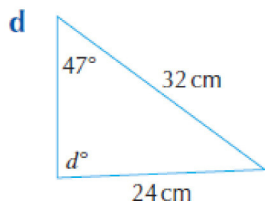
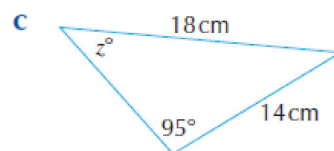
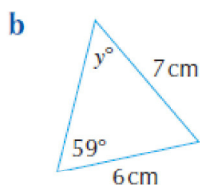
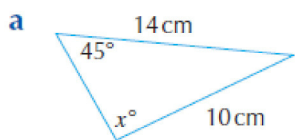
But  $N^\circ$  is obtuse, so

$$N^\circ = 180^\circ - 40.1^\circ$$

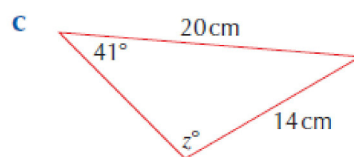
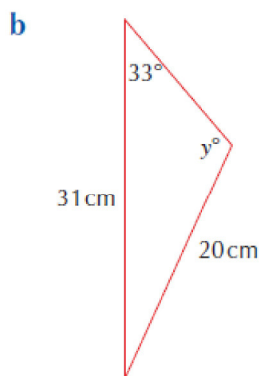
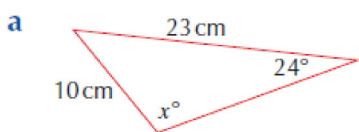
$$N^\circ = 139.9^\circ$$

Questions

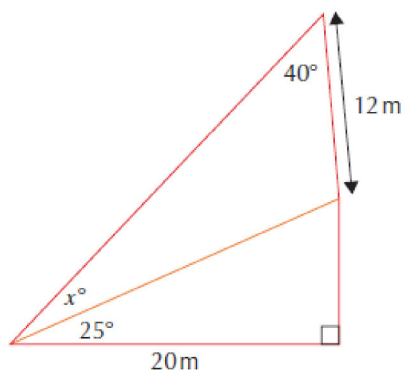
2 Find the size of the missing angles in each example. Give your answers to 1 decimal place.



3 Find the obtuse angles in each of the triangles. Give your answers to 1 decimal place.

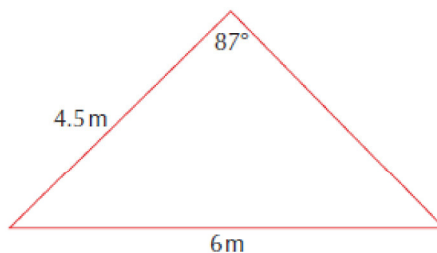


5 Calculate the size of the missing angle  $x$  in the diagram. Give your answer to 1 decimal place.



9 The cross-section of a roof truss is shown.

- a** Calculate the size of the missing angles. Give your answers to 1 decimal place.
- b** Calculate the vertical height of the roof. Give your answer to 1 decimal place.



**Answers**

<b>2</b>	<b>a</b>	$81.9^\circ$	<b>3</b>	<b>a</b>	110.7
	<b>b</b>	$47.3^\circ$		<b>b</b>	122.4
	<b>c</b>	$50.8^\circ$		<b>c</b>	110.4
	<b>d</b>	$77.2^\circ$	<b>5</b>		$20.5^\circ$
	<b>e</b>	$102.6^\circ$	<b>9</b>	<b>a</b>	$48.5^\circ, 44.5^\circ$
	<b>f</b>	$87.3^\circ$		<b>b</b>	3.2 m