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ACKNOWLEDGEMENT

This programme is extensively based on proven approaches and strategies defined within the First Steps in Mathematics resources, Maths Recovery and New Zealand programmes.

Unlike many resources that present mathematical concepts that have been logically ordered and prioritized by mathematicians or educators, First Steps in Mathematics follows a sequence derived from the mathematical development of real children. It is based on five years of research by a team of teachers from the Western Australia Department of Education and Training, and tertiary consultants led by Professor Sue Willis at Murdoch University. The First Steps in Mathematics project team conducted an extensive review of international research literature, which revealed gaps in the field of knowledge about students' learning in mathematics. Using tasks designed to replicate those in the research literature, team members interviewed hundreds of elementary school children in diverse locations. Analysis of the data obtained from these interviews identified characteristic phases in the development of students' thinking about mathematical concepts.

Maths Recovery, founded on years of research by Dr Robert Wright, Professor in Maths Education within Southern Cross University in Australia and colleagues, is now internationally renowned in responding to problems of children's failure in early numeracy and primary mathematics and has been used extensively by many nations, including New Zealand, to develop their own standards and teaching approaches in mathematics.

We are also very grateful to the work done by both Angus and Highland Council. Their input has been key in the development of this progression.



GUIDANCE

The Fife Numeracy and Mathematics Progression (Shape, Position and Movement) sets out a clear set of learning experiences and outcomes from the following Curriculum for Excellence Numeracy and Mathematics strands:

Properties of 2D Shapes and 3D Objects

Angle, Symmetry and Transformation

The purpose of this document is to provide a continuum of learning both within a level and through the Early, First, Second and Third levels. The developmental stages of learning in numeracy and mathematics are clearly documented and this will support teachers when identifying starting points for learners. The progression is intended to assist teachers as they plan their numeracy and mathematics curriculum.

The 'Points to Consider' and 'Suggested Written Recording' sections will be built up as feedback is received on this document.

Each strand is shown as a pyramid to show how learning and teaching progress within this. The skills at the base of the pyramids are required to be understood for further learning to be built upon and are not aligned to any particular year group (at First Level, statements in blue do *not* equate to Primary 2, for example). Pupils will progress through the pyramids as and when they are ready and able to do so.

The Fife Numeracy and Mathematics Progression focuses on developing increasingly sophisticated and refined mathematical understanding, fluency, logical reasoning, analytical thought and problem solving skills which can be applied in unfamiliar situations.

Early Level Experiences and Outcomes ~ Shape, Position and Movement

I enjoy investigating objects and shapes and can sort, describe and be creative with them. MTH 0-16a Pg 4

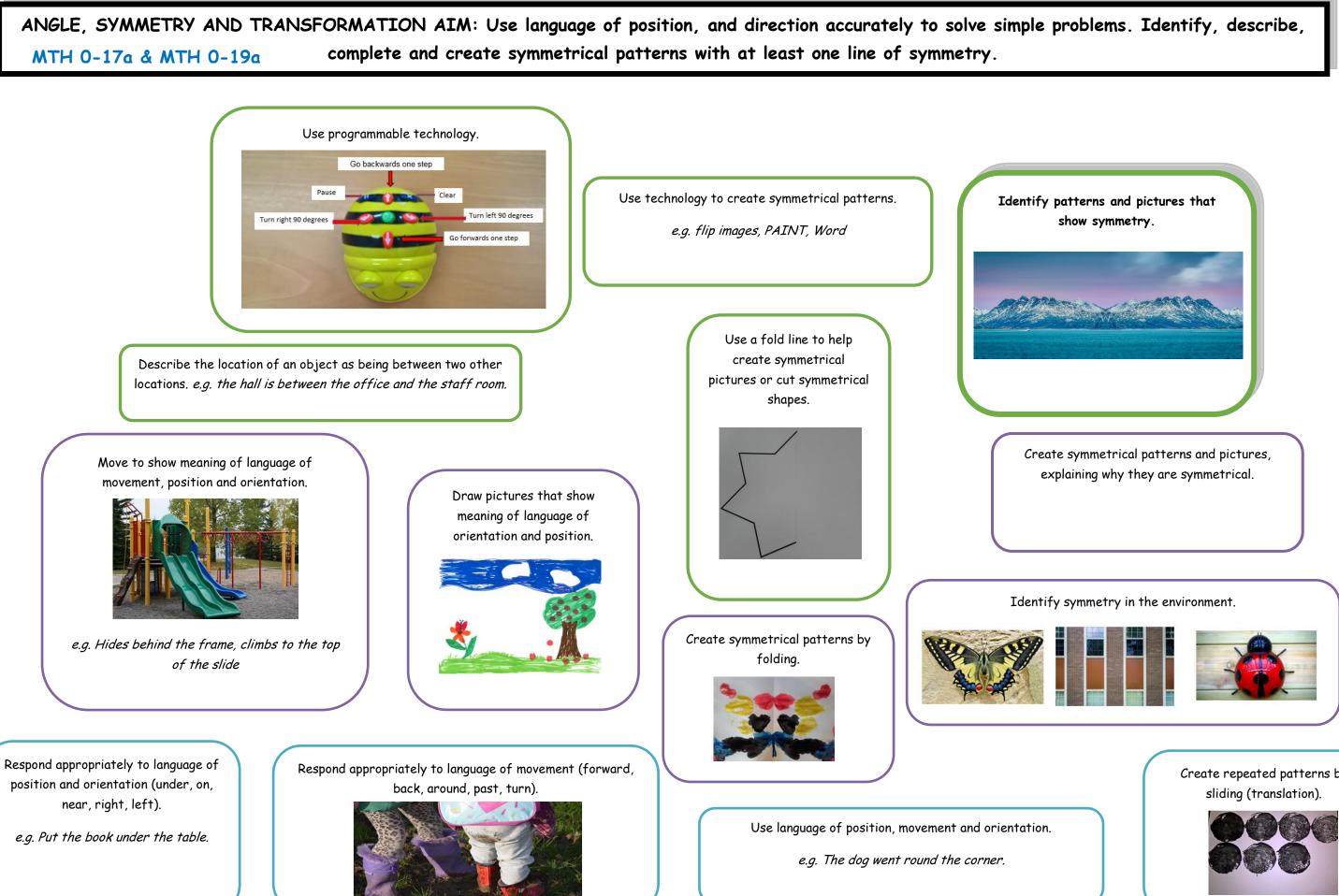
In movement, games, and using technology I can use simple directions and describe positions. MTH O-17a Pg 5

I have had fun creating a range of symmetrical pictures and patterns using a range of media. MTH 0-19a Pg 5

PROPERTIES OF 2D SHAPES AND 3D OBJECTS AIM: Recognise, sort, describe and use simple 2D shapes and 3D objects MTH 0-16a according to various criteria.



complete and create symmetrical patterns with at least one line of symmetry.



Fife Numeracy & Mathematics Progression Pyramid: Early Level ~ Page 5

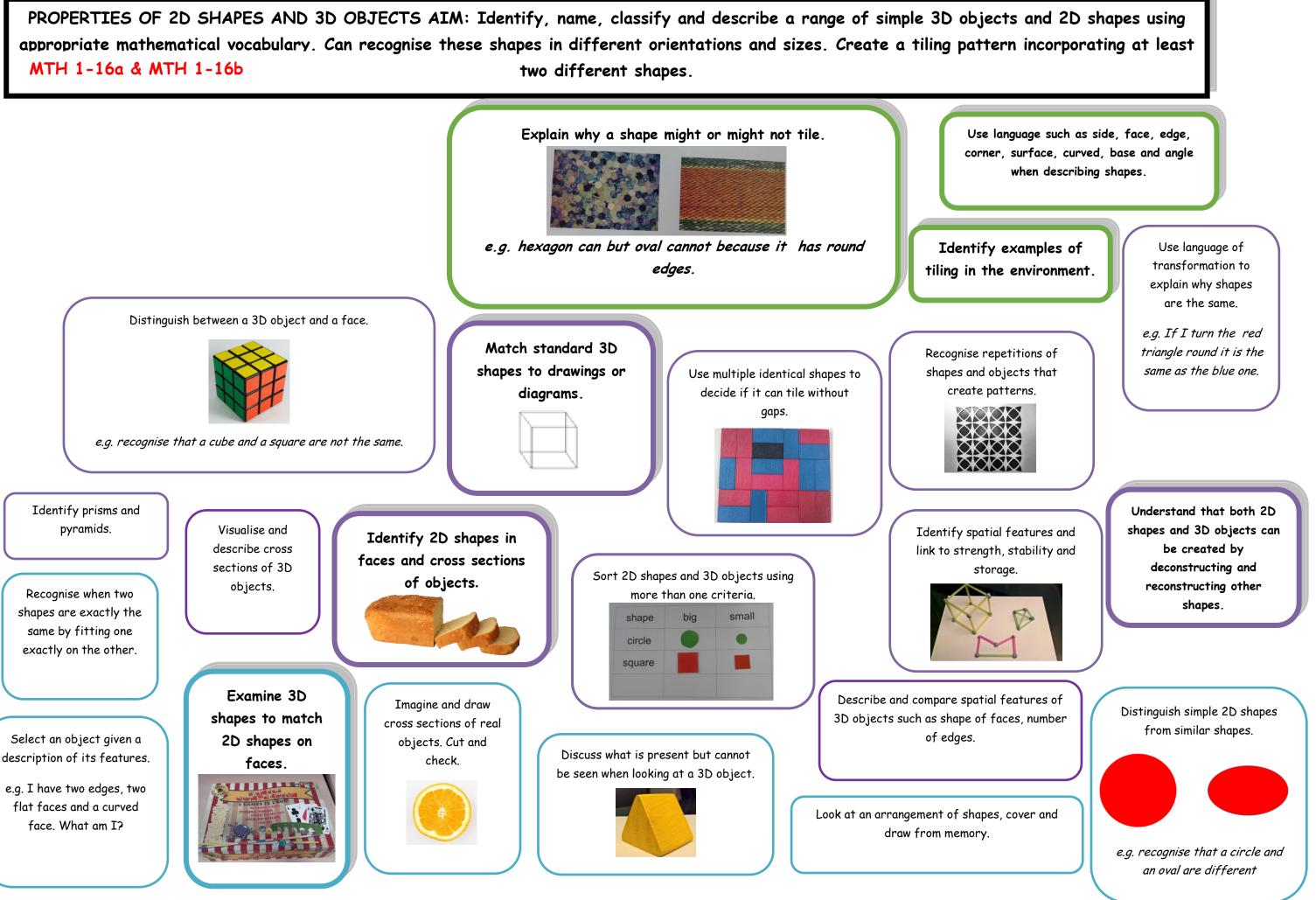
Create repeated patterns by

Early Level Overview

Key Aspect	Experiences and Outcomes	National Benchmarks
Properties of 2D Shapes and 3D Objects Pg 4	I enjoy investigating objects and shapes and can sort, describe and be creative with them. MTH 0-16a	 Recognises, describes and sorts common 2D shapes and 3D objects according to various criteria, for example, straight, round, flat and curved.
Angle, Symmetry and Transformation Pg 5	In movement, games, and using technology I can use simple directions and describe positions. MTH 0-17a	 Understands and correctly uses the language of position and direction, including in front, behind, above, below, left, right, forwards and backwards, to solve simple problems in movement games.
. 9 .	I have had fun creating a range of symmetrical pictures and patterns using a range of media. MTH 0-19a	 Identifies, describes and creates symmetrical pictures with one line of symmetry.

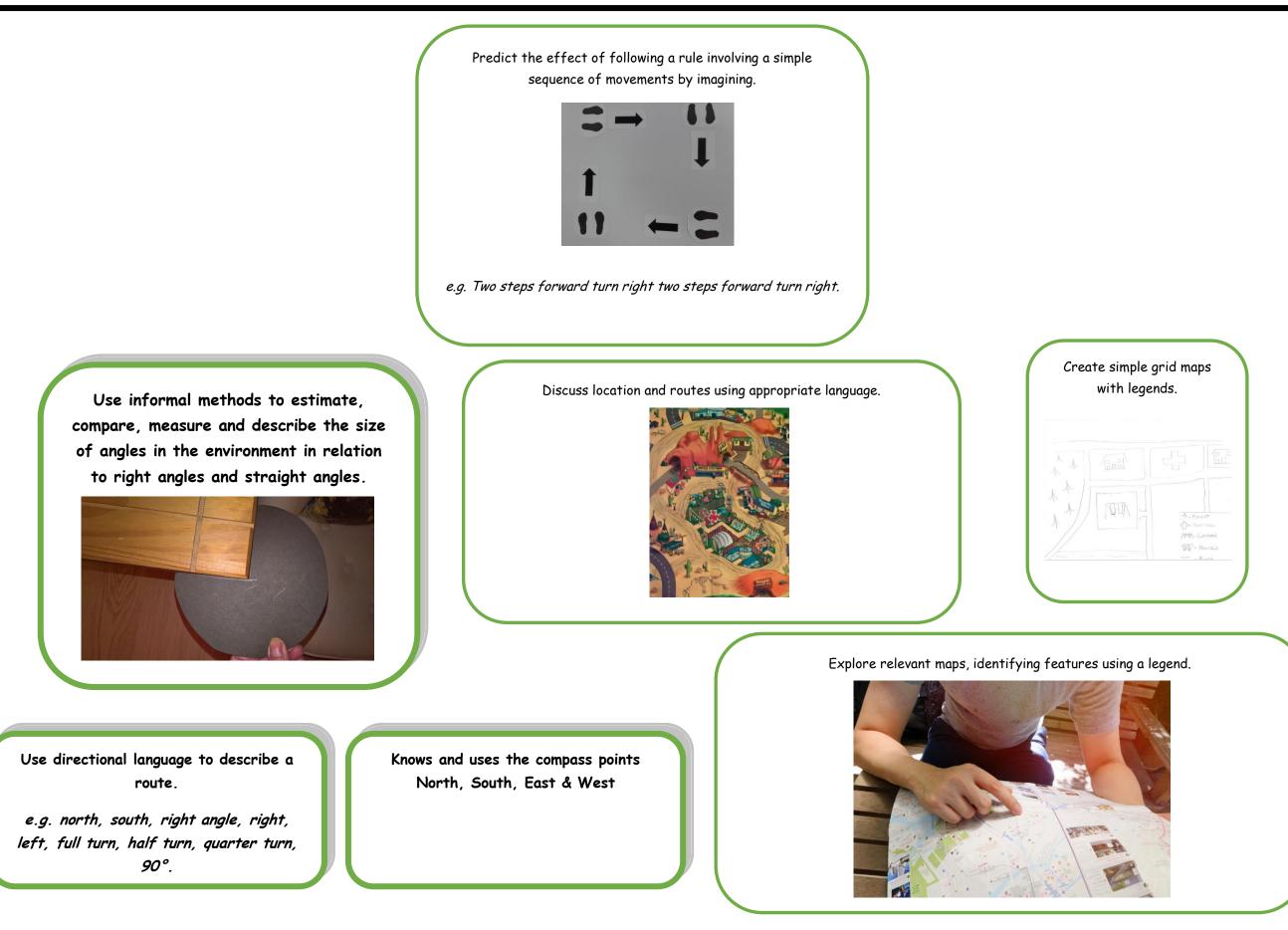
First Level Experiences and Outcomes ~ Shape, Position and Movement I have explored simple 3D objects and 2D shapes and can identify, name and describe their features using appropriate vocabulary. MTH 1-16a Pq 8 I can explore and discuss how and why different shapes fit together and create a tiling pattern with them. MTH 1-16b Pa 8 I can describe, follow and record routes and journeys using signs, words and angles associated with direction and turning. MTH 1-17a Pa's 9 & 10 I have developed an awareness of where grid reference systems are used in everyday contexts and can use them to locate and describe position. MTH 1-18a Pg's 9 & 10 I have explored symmetry in my own and the wider environment and can create and recognise symmetrical pictures, patterns and shapes. MTH 1-19a Pg's 9 & 10

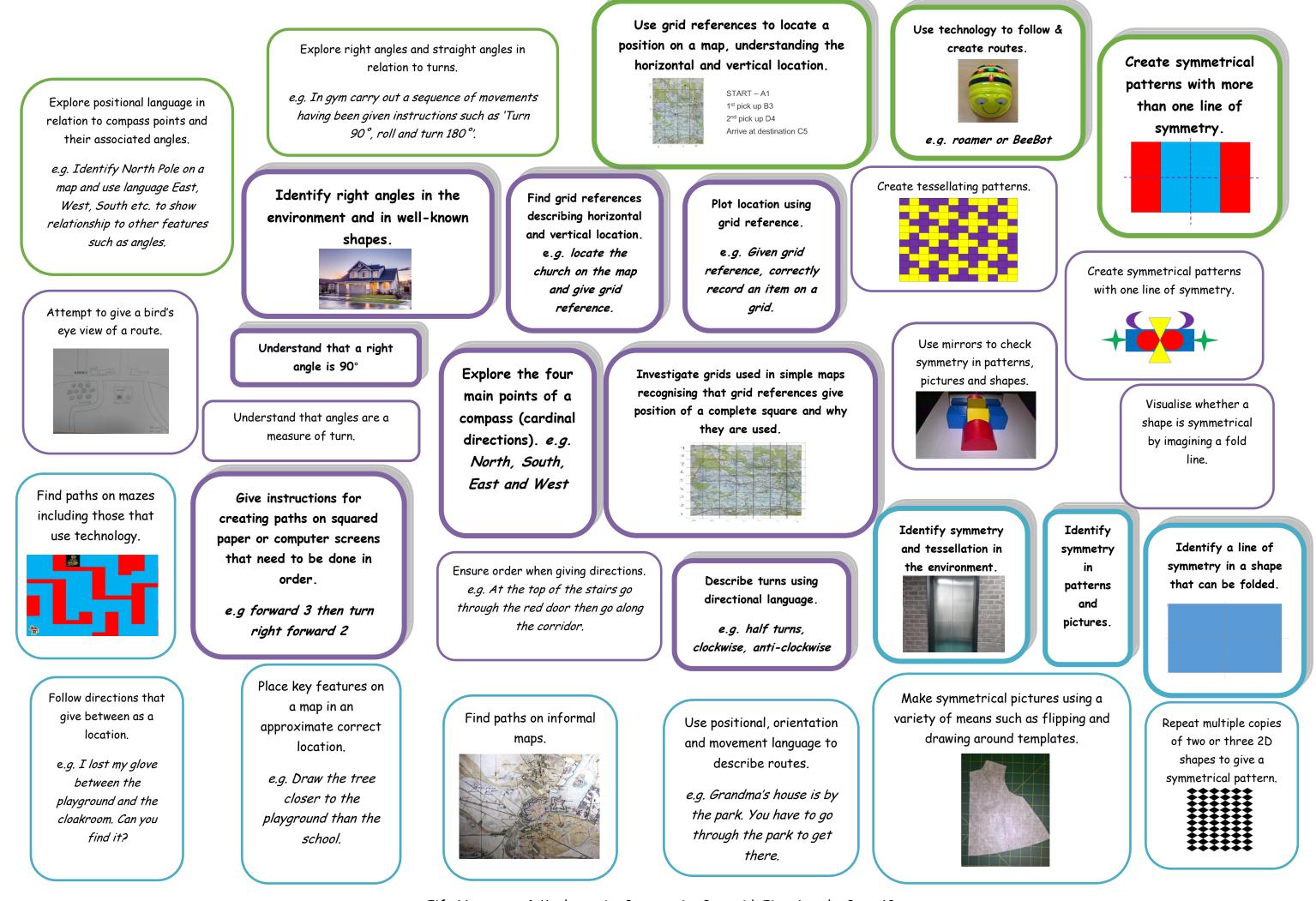
MTH 1-16a & MTH 1-16b two different shapes.



Fife Numeracy & Mathematics Progression Pyramid: First Level ~ Page 8

ANGLE, SYMMETRY AND TRANSFORMATION AIM: Use positional and directional language to describe, follow and record locations, routes and directions, including those on grids. Recognise, record and explain symmetrical patterns, pictures, nature and 2D shapes. Note: This pyramid appears over two pages. MTH 1-17a, MTH 1-18a & MTH 1-19a





First Level Overview

Key Aspect	Experiences and Outcomes	National Benchmarks
Properties of 2D Shapes and 3D Objects	I have explored simple 3D objects and 2D shapes and can identify, name and describe their features using appropriate vocabulary.	 Names, identifies and classifies a range of simple 2D shapes and 3D objects and recognises these shapes in different orientations and sizes. Uses mathematical language to describe the properties of a range of
Pg 8	MTH 1-16a I can explore and discuss how and	common 2D shapes and 3D objects including, side, face, edge, vertex, base and angle.
	why different shapes fit together and create a tiling pattern with them.	 Identifies 2D shapes within 3D objects and recognises 3D objects from 2D drawings.
	МТН 1-16Ь	 Identifies examples of tiling in the environment and applies knowledge of the features of 2D shapes to create tiling patterns incorporating two different shapes.
Angle,	I can describe, follow and record	• Uses technology and other methods to describe, follow and record
Symmetry and	routes and journeys using signs,	directions using words associated with angles, directions and turns
Transformation	words and angles associated with direction and turning.	including full turn, half turn, quarter turn, clockwise, anticlockwise, right turn, left turn, and right angle.
Pg's 9 & 10	MTH 1-17a	 Knows that a right angle is 90°.
5	I have developed an awareness of	• Knows and uses the compass points, North, South, East and West.
	where grid reference systems are	• Uses informal methods to estimate, compare and describe the size of
	used in everyday contexts and can use	angles in relation to a right angle.
	them to locate and describe position.	• Finds right angles in the environment and in well-known 2D shapes.
	MTH 1-18a	 Identifies where and why grid references are used.
	I have explored symmetry in my own	 Describes, plots and uses accurate two figure grid references,
	and the wider environment and can	demonstrating knowledge of the horizontal and vertical location.
	create and recognise symmetrical	• Identifies symmetry in patterns, pictures, nature and 2D shapes.
	pictures, patterns and shapes. MTH 1-19a	 Creates symmetrical pictures and designs with more than one line of symmetry.

Second Level Experiences and Outcomes ~ Shape, Position and Movement

Having explored a range of 3D objects and 2D shapes, I can use mathematical language to describe their properties, and through investigation can discuss where and why particular shapes are used in the environment.

MTH 2-16a Pg 13

Through practical activities, I can show my understanding of the relationship between 3D objects and their nets.

MTH 2-16b Pg 13

I can draw 2D shapes and make representations of 3D objects using an appropriate range of methods and efficient use of resources.

MTH 2-16c Pg 13

I have investigated angles in the environment, and can discuss, describe and classify angles using appropriate mathematical vocabulary.

MTH 2-17a Pg's 14 & 15

I can accurately measure and draw angles using appropriate equipment, applying my skills to problems in context.

MTH 2-17b Pg's 14 & 15

Through practical activities which include the use of technology, I have developed my understanding of the link between compass points and angles and can describe, follow and record directions, routes and journeys using appropriate vocabulary.

MTH 2-17c Pg's 14 & 15

Having investigated where, why and how scale is used and expressed, I can apply my understanding to interpret simple models, maps and plans.

MTH 2-17d Pg's 14 & 15

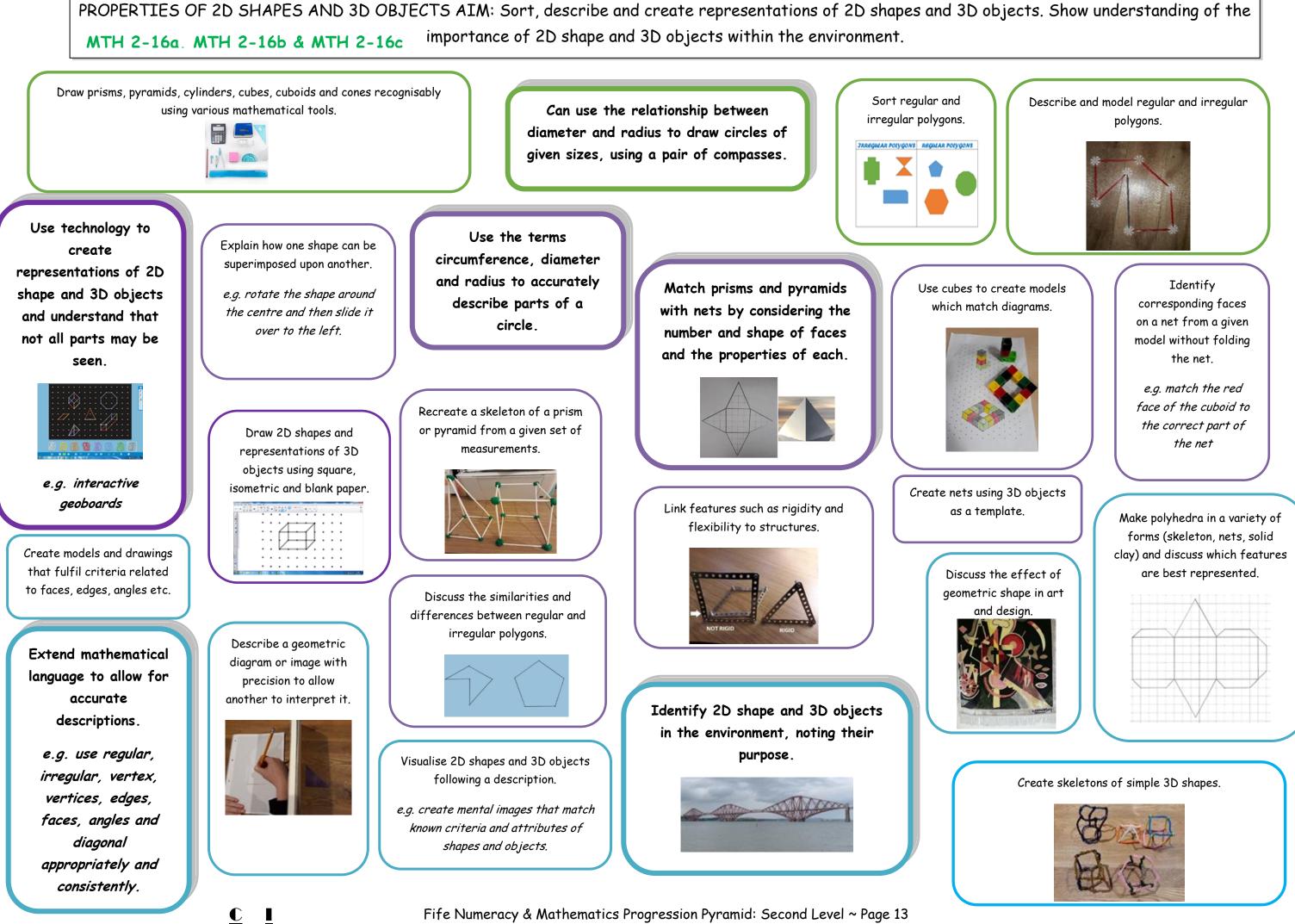
I can use my knowledge of the coordinate system to plot and describe the location of a point on a grid.

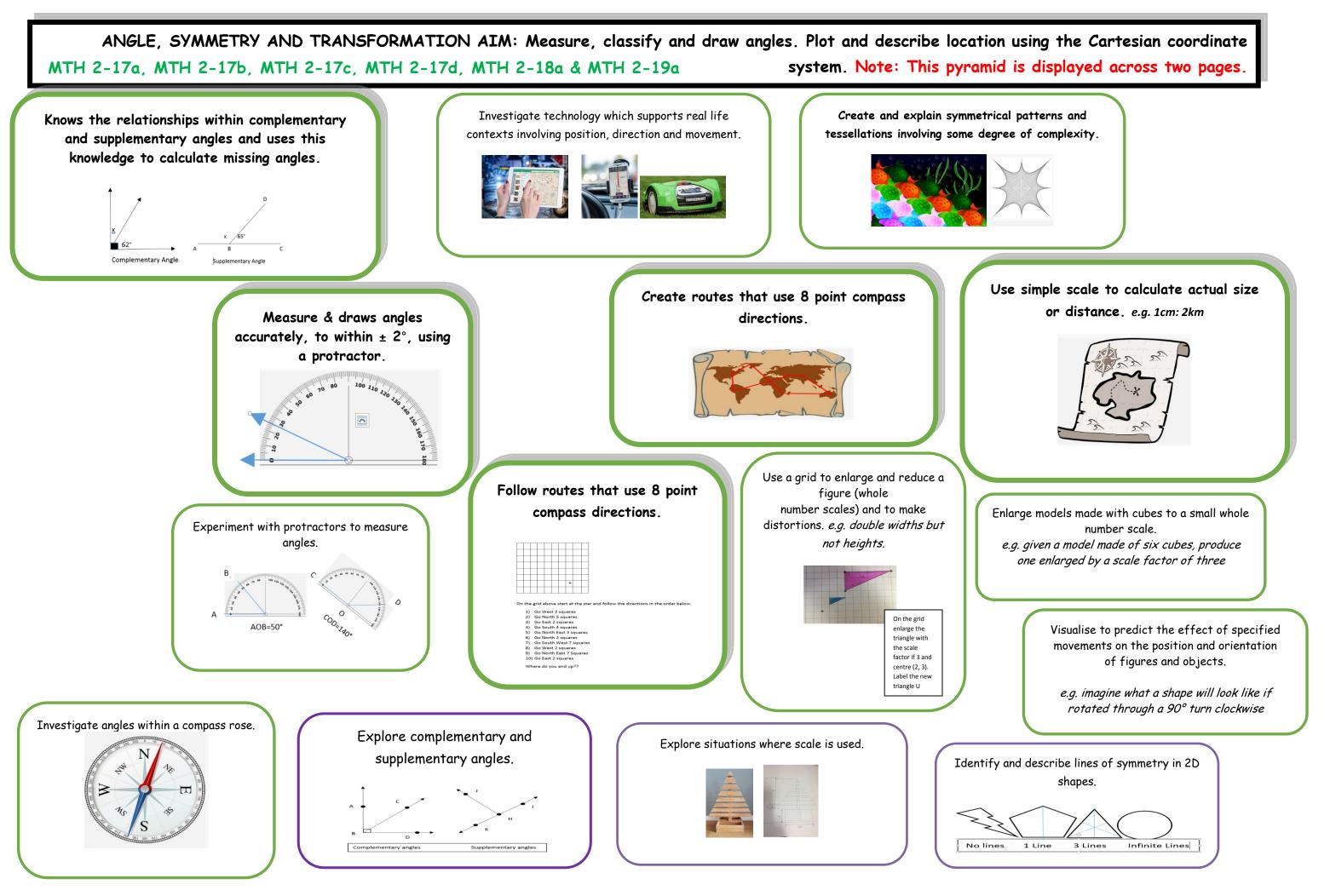
MTH 2-18a/MTH 3-18a Pg's 14 & 15

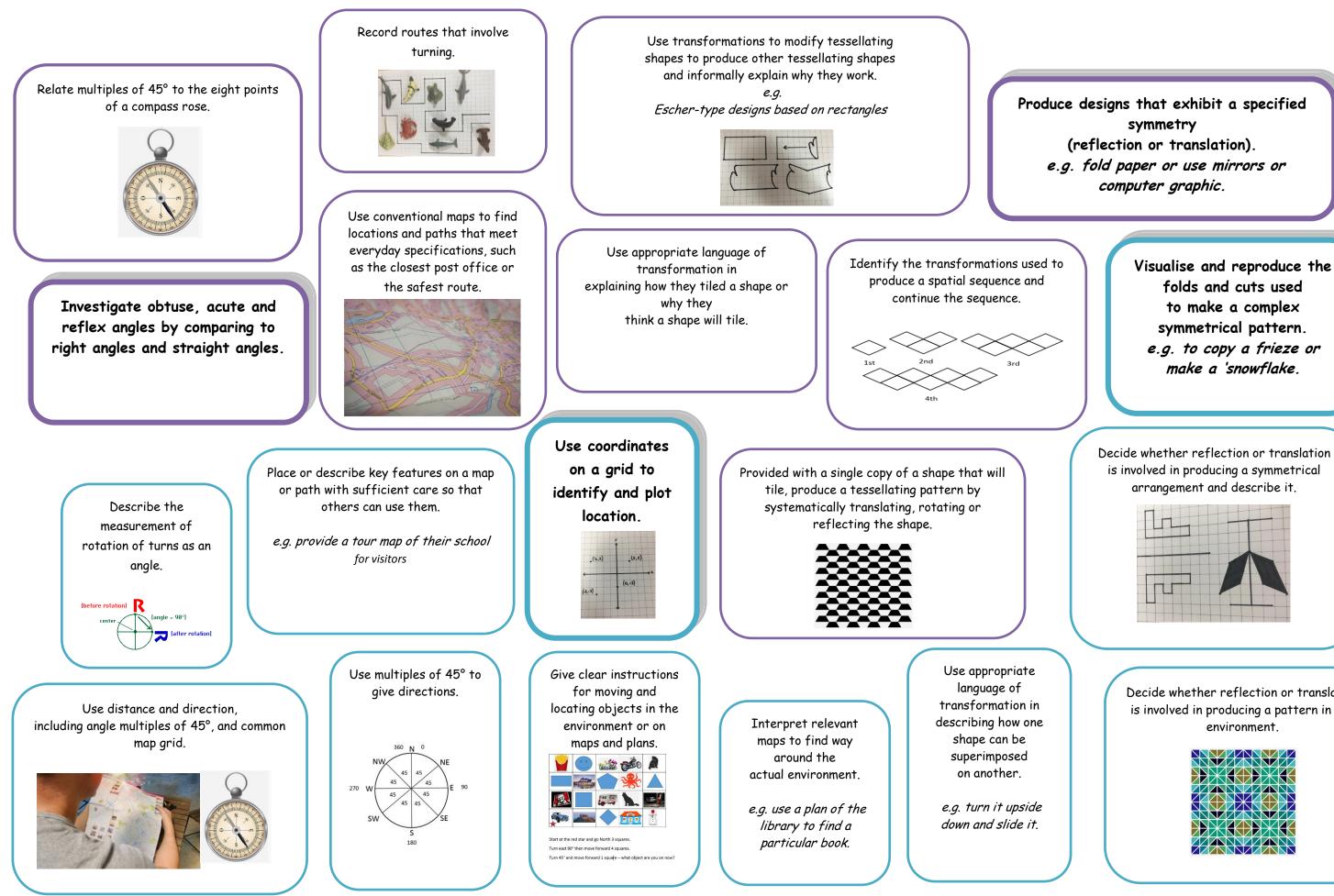
I can illustrate the lines of symmetry for a range of 2D shapes and apply my understanding to create and complete symmetrical pictures and patterns.

MTH 2-19a/MTH 3-19a Pg's 14 & 15

importance of 2D shape and 3D objects within the environment.







Fife Numeracy & Mathematics Progression Pyramid: Second Level ~ Page 15

Decide whether reflection or translation is involved in producing a pattern in the

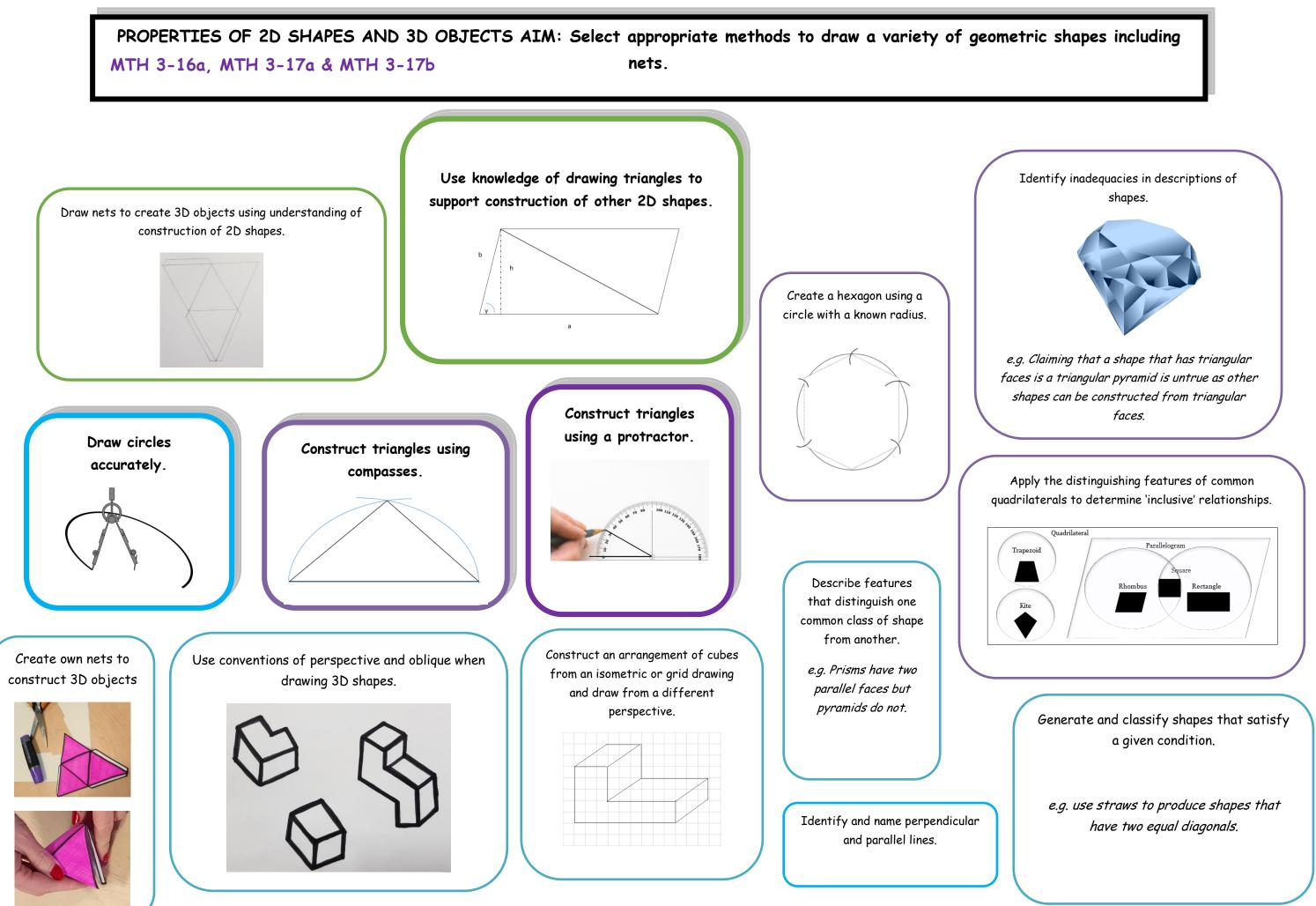
Second Level Overview

Key Aspect	Experiences and Outcomes	National Benchmarks
Pg 13 w	Having explored a range of 3D objects and 2D shapes, I can use mathematical language to describe their properties, and through investigation can discuss where and why particular shapes are used in the environment. MTH 2-16a Through practical activities, I can show my understanding of the relationship between 3D objects and their nets. MTH 2-16b	 Describes 2D shapes and 3D objects using specific vocabulary including regular, irregular, diagonal, radius, diameter and circumference. Applies this knowledge to demonstrate understanding of the relationship between 3D objects and their nets. Identifies and describes 2D shapes and 3D objects within the environment and explains why their properties match their function. Knows that the radius is half of the diameter. Uses digital technologies and mathematical instruments to draw 2D shapes and make representations of 3D objects, understanding that not all parts of the 3D object can be seen.
	I can draw 2D shapes and make representations of 3D objects using an appropriate range of methods and efficient use of resources. MTH 2-16c	

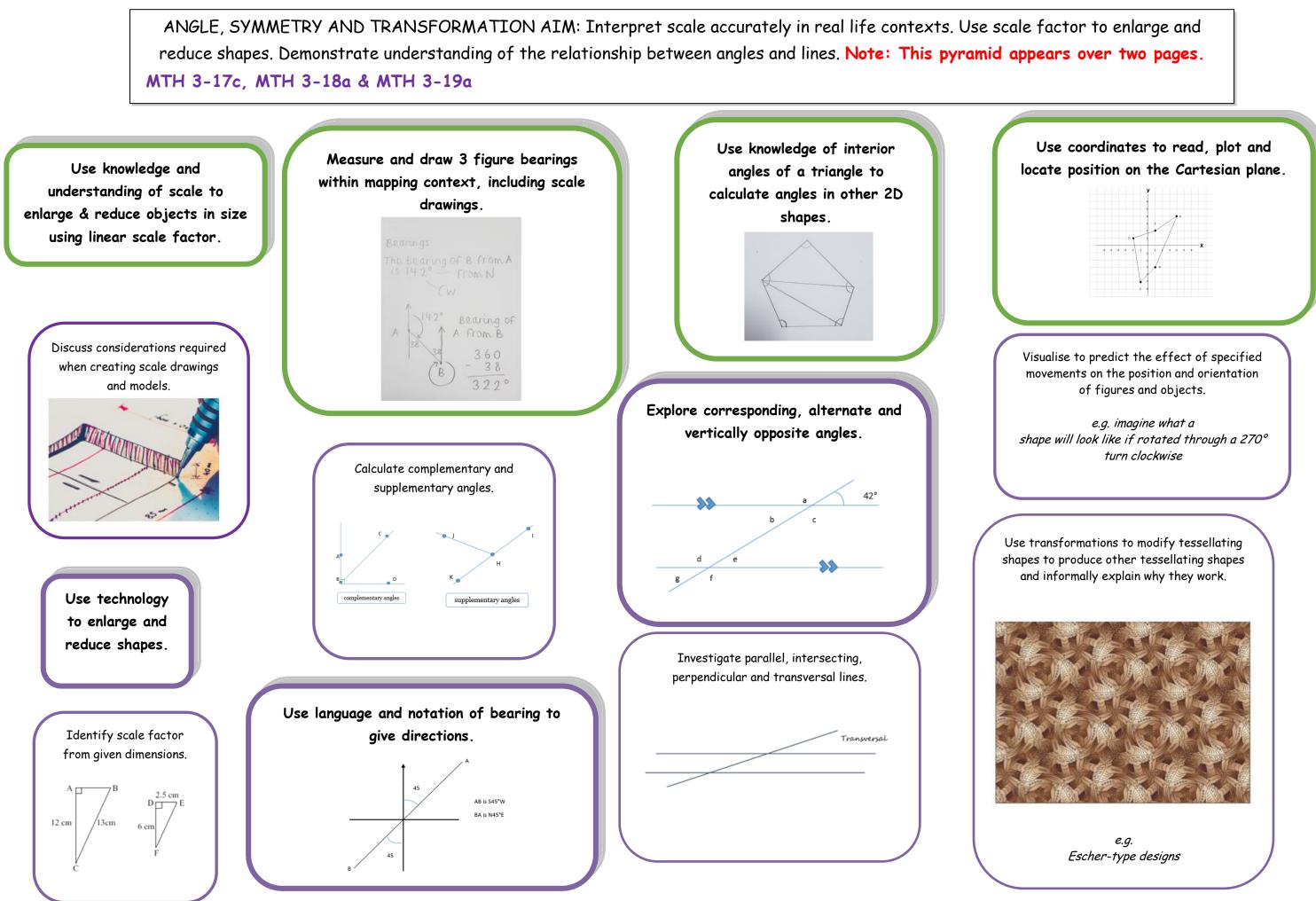
Key Aspect	Experiences and Outcomes	National Benchmarks
Angle, Symmetry and Transformation Pg's 14 & 15	I have investigated angles in the environment, and can discuss, describe and classify angles using appropriate mathematical vocabulary. MTH 2-17a I can accurately measure and draw angles using appropriate equipment, applying my skills to problems in context. MTH 2-17b Through practical activities which include the use of technology, I have developed my understanding of the link between compass points and angles and can describe, follow and record directions, routes and journeys using appropriate vocabulary. MTH 2-17c	 Uses mathematical language including acute, obtuse, straight and reflex to describe and classify a range of angles identified within shapes in the environment. Measures and draws accurately a range of angles to within ±2°. Knows that complementary angles add up to 90 degrees and supplementary angles add up to 180 degrees and uses this knowledge to calculate missing angles. Uses knowledge of the link between the eight compass points and angles to describe, follow and record directions. Interprets maps, models or plans with simple scales, for example, 1cm:2km. Describes, plots and records the location of a point, in the first quadrant, using coordinate notation. Identifies and illustrates line symmetry on a wide range of 2D shapes and applies this understanding to complete a range of symmetrical patterns, with and without the use of digital technologies.
	Having investigated where, why and how scale is used and expressed, I can apply my understanding to interpret simple models, maps and plans. MTH 2-17d	
	I can use my knowledge of the coordinate system to plot and describe the location of a point on a grid. MTH 2-18a/MTH 3-18a	
	I can illustrate the lines of symmetry for a range of 2D shapes and apply my understanding to create and complete symmetrical pictures and patterns. MTH 2-19a/MTH 3-19a	

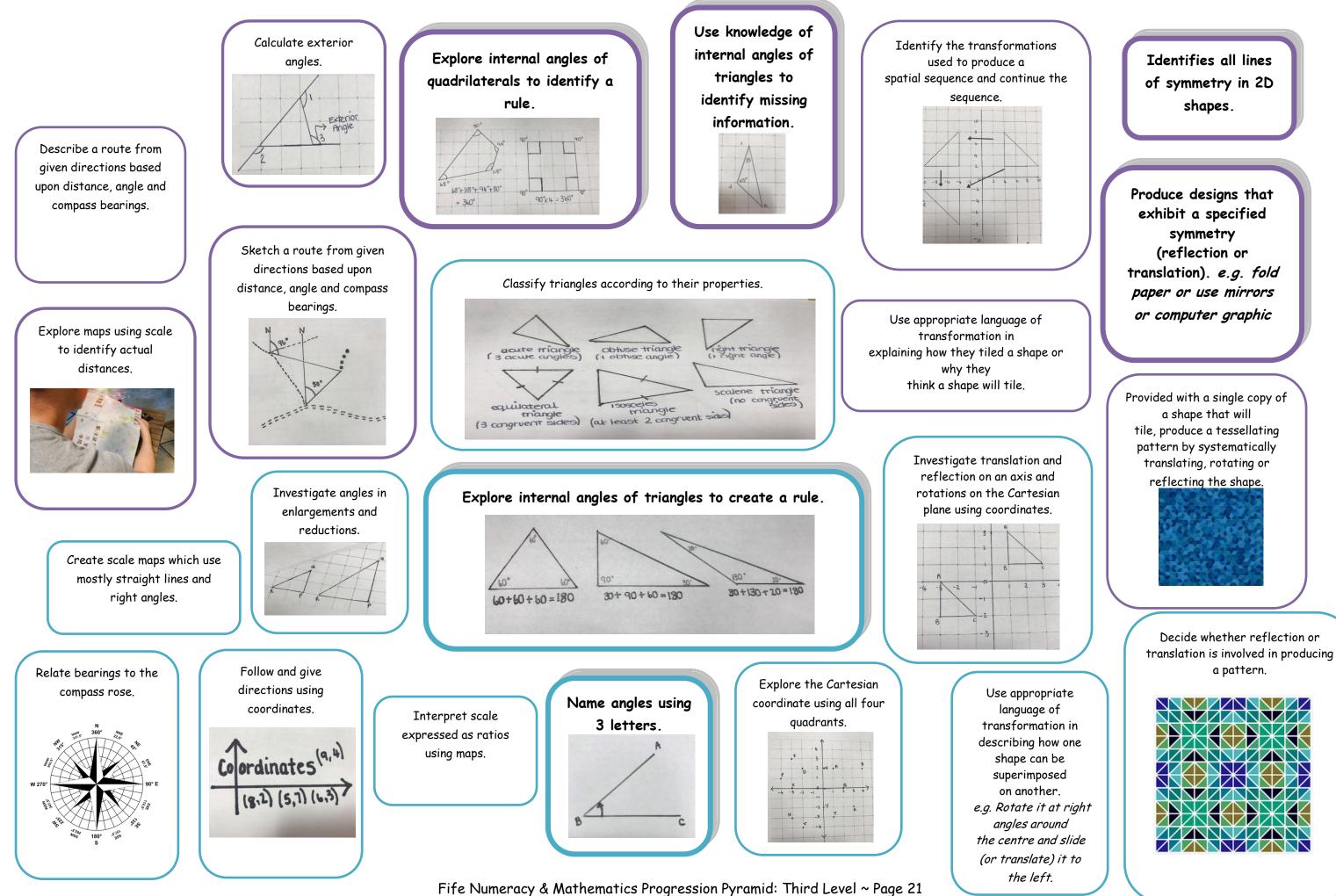
Third Level Experiences and Outcomes ~ Shape, Position and Movement Having investigated a range of methods, I can accurately draw 2D shapes using appropriate mathematical instruments and methods MTH 3-16a Pg 19 I can name angles and find their sizes using my knowledge of the properties of a range of 2D shapes and the angle properties associated with intersecting and parallel lines. MTH 3-17a Pa 19 Having investigated navigation in the world, I can apply my understanding of bearings and scale to interpret maps and plans and create accurate plans, and scale drawings of routes and journeys. MTH 3-17b Pa 19 I can apply my understanding of scale when enlarging or reducing pictures and shapes, using different methods, including technology. MTH 3-17c Pg's 20 & 21 I can use my knowledge of the coordinate system to plot and describe the location of a point on a grid. MTH 2-18a/MTH 3-18a Pg's 20 & 21 I can illustrate the lines of symmetry for a range of 2D shapes and apply my understanding to create and complete symmetrical pictures and patterns. MTH 2-19a/MTH 3-19a Pg's 20 & 21

nets.



Fife Numeracy & Mathematics Progression Pyramid: Third Level ~ Page 19





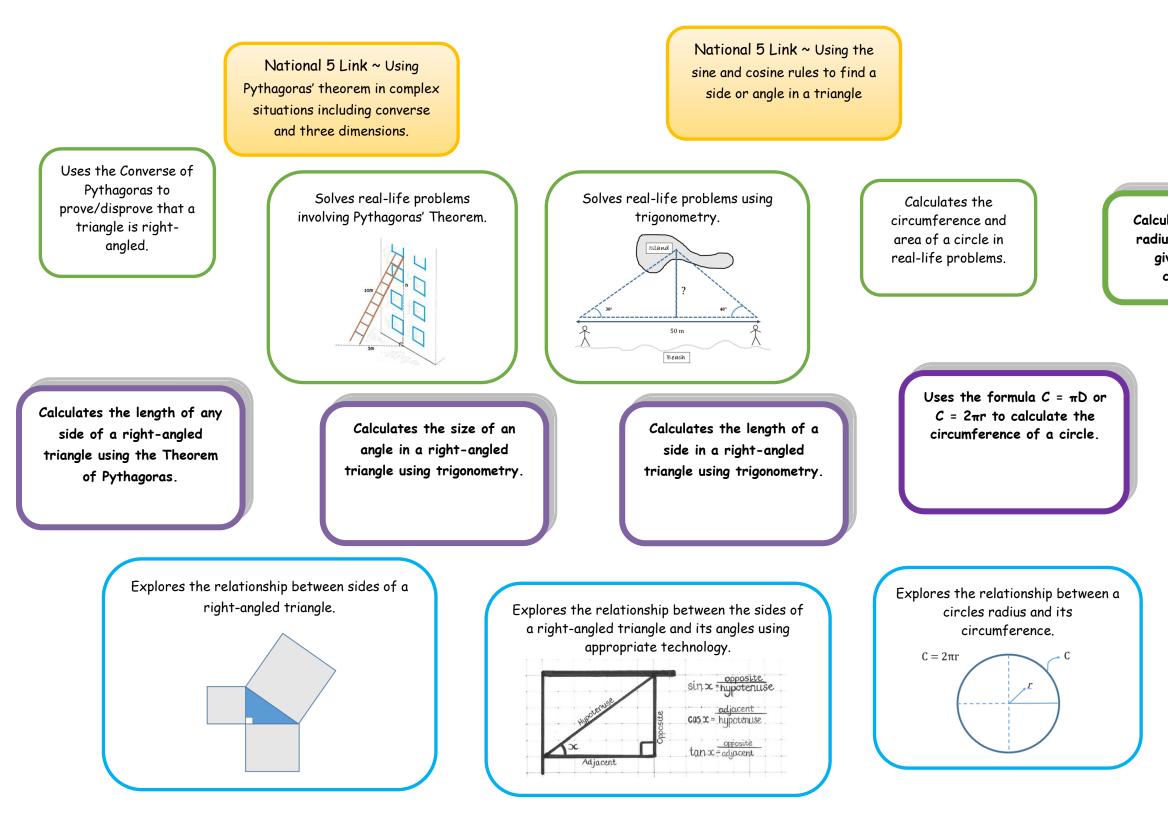
Third Level Overview

Key Aspect	Experiences and Outcomes		National Benchmarks
Properties of	Having investigated a range of methods,	•	Demonstrates a variety of methods to accurately draw 2D shapes, including
2D Shapes and	I can accurately draw 2D shapes using		triangles and regular polygons (given the interior angle), using mathematical
3D Objects	appropriate mathematical instruments		instruments.
	and methods.		
Pg 19	MTH 3-16a		
	I can name angles and find their sizes		
	using my knowledge of the properties of		
	a range of 2D shapes and the angle		
	properties associated with intersecting		
	and parallel lines.		
	MTH 3-17a		
	Having investigated navigation in the		
	world, I can apply my understanding of		
	bearings and scale to interpret maps and		
	plans and create accurate plans, and		
	scale drawings of routes and journeys.		
	MTH 3-17b		

Key Aspect	Experiences and Outcomes	National Benchmarks
Angle, Symmetry and Transformation Pg's 20 & 21	I can apply my understanding of scale when enlarging or reducing pictures and shapes, using different methods, including technology. MTH 3-17c I can use my knowledge of the coordinate system to plot and describe the location of a point on a grid. MTH 2-18a/MTH 3-18a	 Names angles using mathematical notation, for example, ∠ ABC Identifies corresponding, alternate and vertically opposite angles and uses this knowledge to calculate missing angles. Uses the angle properties of triangles and quadrilaterals to find missing angles. Applies knowledge and understanding of scale to enlarge and reduce objects in size showing understanding of linear scale factor. Uses bearings in a navigational context including creating scale drawings. Identifies all lines of symmetry in 2D shapes. Creates symmetrical patterns and pictures.
	I can illustrate the lines of symmetry for a range of 2D shapes and apply my understanding to create and complete symmetrical pictures and patterns. MTH 2-19a/MTH 3-19a	

Founth Laval Expani	ences and Outcomes
I have explored the relationships that exist between the sides, or sides and angles, in right-angled triangles and can select and use an appropriate strategy to solve related problems, interpreting my answer for the context.	I can apply my understanding of the properties of similar figures to solve problems involving length and area. MTH 4-17b Pgs 26 & 27
MTH 4-16a Pg 25	I can plot and describe the position of a point on a 4-quadrant coordinate grid.
Having investigated the relationships between the radius, diameter, circumference and area of a circle, I can apply my knowledge to solve related problems.	MTH 4-18a Pgs 26 & 27
MTH 4-16b Pg 25	I can apply my understanding of the 4-quadrant coordinate system to move, and describe the transformation of, a point or shape on a grid.
Having investigated the relationship between a radius and a tangent and explored the size of the angle in a semi-circle, I can use the facts	MTH 4-18b Pgs 26 & 27
I have established to solve related problems. MTH 4-17a Pgs 26 & 27	Having investigated patterns in the environment, I can use appropriate mathematical vocabulary to discuss the rotational properties of shapes, pictures and patterns and can apply my understanding when completing or creating designs.
	MTH 4-19a Pgs 26 & 27

PROPERTIES OF 2D SHAPES & 3D OBJECTS AIM: Use Pythagoras' Theorem and Trigonometry to carry out calculations with right-angled triangles and use formulae to carry out calculations with circles. MTH 4-16a, MTH 4-16b



National 5 Link ~ Calculating the length of an arc and the area of a sector.

Calculates diameter and radius of a circle when given the area or circumference.

> Uses the formula $A = \pi r^2$ to calculate the area of a circle.

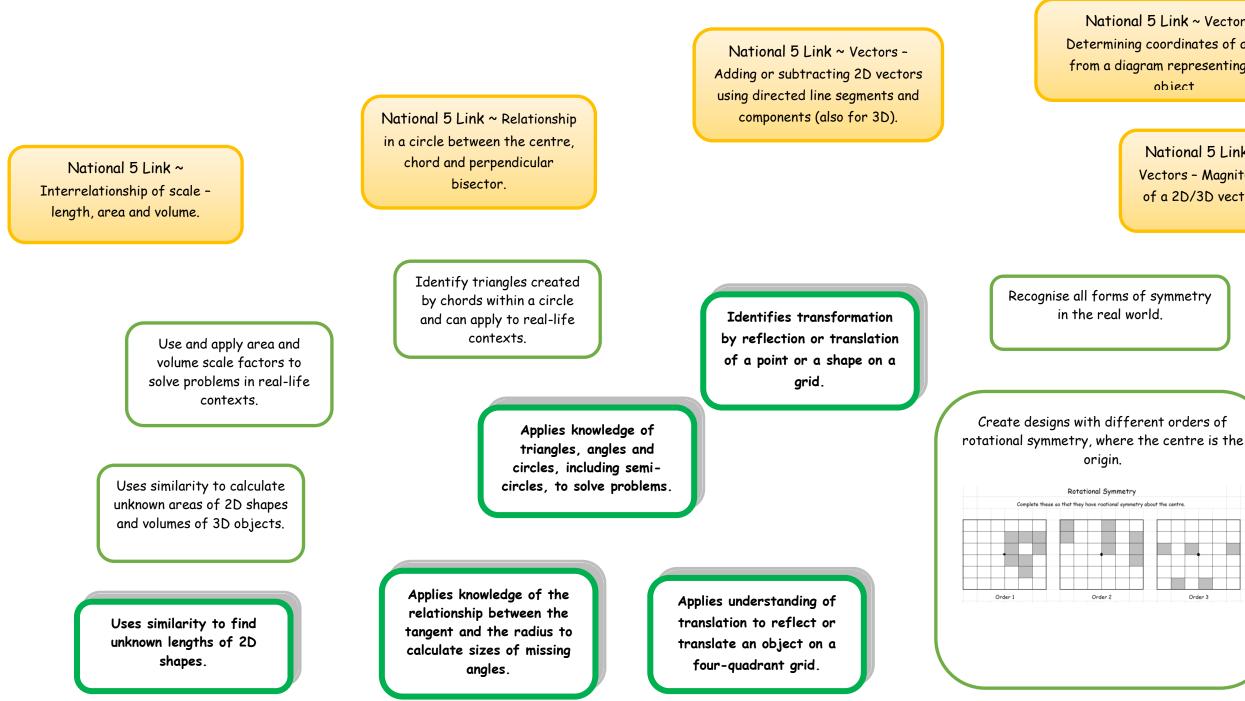
Explores the relationship between a circles radius and its area.

 $A = \pi r$

ANGLE, SYMMETRY & TRANSFORMATION AIM: Note: This pyramid appears across two pages

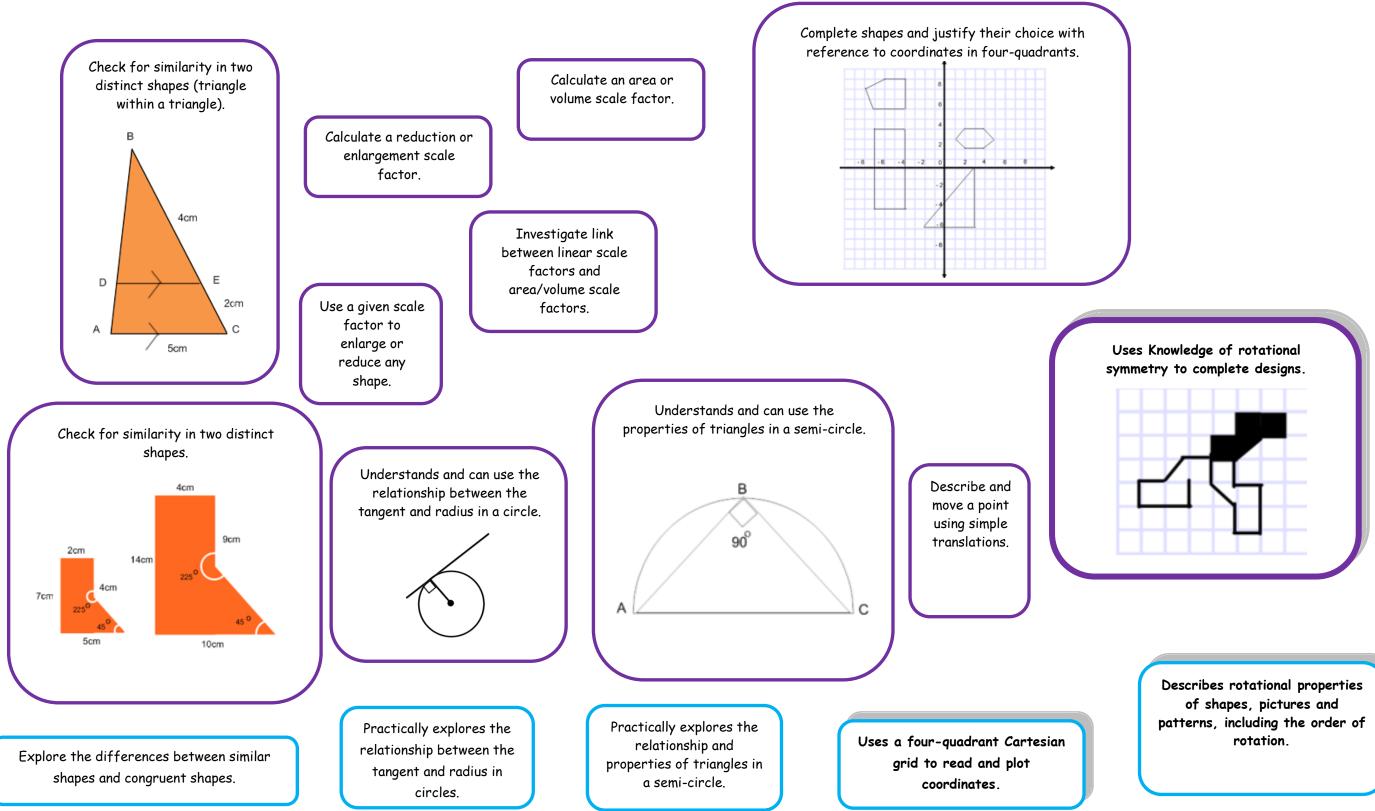
Interpret symmetry in real life contexts. Use knowledge of similar shapes to find unknown lengths of 2D shapes. Demonstrate understanding of the relationship between angles, lines and triangles in circles

MTH 4-17a, MTH 4-17b, MTH 4-18a, MTH 4-18b, MTH 4-19a



National 5 Link ~ Vectors -Determining coordinates of a point from a diagram representing a 3D object National 5 Link ~ Vectors - Magnitude of a 2D/3D vector.

Order 3



Fourth Level Overview

Key Aspect	Experiences and Outcomes	National Benchmarks
Properties of 2D Shapes and 3D Objects Pg 25	I have explored the relationships that exist between the sides, or sides and angles, in right-angled triangles and can select and use an appropriate strategy to solve related problems, interpreting my answer for the context. MTH 4-16a	 Calculates the length of any side of a right-angled triangle using the Theorem of Pythagoras. Calculates the size of an angle in a right-angled triangle using trigonometry. Calculates the length of a side in a right-angled triangle using trigonometry. Uses the formula C = πD or C = 2πr to calculate the circumference of a circle. Uses the formula A = πr² to calculate the area of a circle. Calculates diameter and radius of a circle when given the area or circumference.
	Having investigated the relationships between the radius, diameter, circumference and area of a circle, I can apply my knowledge to solve related problems. MTH 4-16b	

Key Aspect	Experiences and Outcomes	National Benchmarks
Angle, Symmetry and Transformation Pgs 26 & 27	Having investigated the relationship between a radius and a tangent and explored the size of the angle in a semi-circle, I can use the facts I have established to solve related problems. MTH 4-17a I can apply my understanding of the properties of similar figures to solve problems involving length and area. MTH 4-17b I can plot and describe the position of a point on a 4- quadrant coordinate grid. MTH 4-18a	 Describes rotational properties of shapes, pictures and patterns, including the order of rotation. Uses knowledge of rotational symmetry to complete designs. Uses a four-quadrant Cartesian grid to read and plot coordinates. Applies understanding of translation to reflect or translate an object on a four-quadrant grid. Uses similarity to find unknown lengths of 2D shapes. Applies knowledge of the relationship between the tangent and radius to calculate sizes of missing angles. Applies knowledge of triangles, angles and circles, including semi-circles, to solve problems. Identifies transformation by reflection or translation of a point or shape on a grid.

Key Aspect	Experiences and Outcomes	National Benchmarks
	I can apply my understanding of	
	the 4-quadrant coordinate	
	system to move, and describe	
	the transformation of, a point or	
	shape on a grid.	
	MTH 4-18b	
	Having investigated patterns in the environment, I can use appropriate mathematical vocabulary to discuss the rotational properties of shapes, pictures and patterns and can apply my understanding when completing or creating designs.	

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