## Algebraic Fractions Lesson Practice

## Simplifying Basic Algebraic Fractions

Express these fractions in their simplest form:
(a) $\frac{3}{6}$
(b) $\frac{8}{12}$
(c) $\frac{30}{16}$
(d) $\frac{54}{72}$
(e) $\frac{10 a}{5}$
(f) $\frac{9 b}{6}$
(g) $\frac{18}{12 x}$
(h) $\frac{25}{15 y}$
(i) $\frac{4 c}{16 c^{2}}$
(j) $\frac{32 a}{8 a^{3}}$
(k) $\frac{13 p^{2}}{52 p^{3}}$
(l) $\left.\frac{36 a b}{6 b c} \right\rvert\,$
(m) $\frac{4 a}{2 a^{2}}$
(n) $\frac{10 x^{2}}{12 x y}$
(o) $\frac{3 v^{2} t}{9 v t^{2}}$
(p) $\frac{10 a b^{3}}{2 a^{2} b}$
(q) $\frac{30 p^{2} q}{25 p q^{2}}$
(r) $\frac{81 x^{2} y^{2}}{6 y^{2}}$
(s) $\frac{42 m n^{2}}{56 m n}$
(t) $\frac{8 d e f^{2}}{10 e^{2} f}$
(u) $\frac{3 a b^{2} c}{4 a^{2} c}$
(v) $\frac{4 k^{2} m}{28 \mathrm{~km}^{2}}$
(w) $\frac{5 e f g^{2}}{10 e^{2} f g^{3}}$
(x) $\frac{21 x y^{2}}{36 x^{3}}$

## Simplifying Algebraic Fractions by Factorising

Simplify by first finding the common factor:
(a) $\frac{3 a+6 b}{6}$
(b) $\frac{4 x+12 y}{2}$
(c) $\frac{3 a+a^{2}}{a b}$
(d) $\frac{x y+y^{2}}{2 y}$
(e) $\frac{x y+x^{2}}{6 x+x y}$
(f) $\frac{3 a b+6 b^{2}}{9 b^{2}}$
(g) $\frac{25 b^{2}+15 b^{3}}{10 b}$
(h) $\frac{14 p+10 q}{2 s}$
(i) $\frac{3 a}{2 a b-a c}$
(j) $\frac{6 x}{9 x+9 y}$
(k) $\frac{2 s t}{6 r s-2 s t}$
(I) $\frac{5 c}{10 a c+15 b c}$
(m) $\frac{14 p+28 p^{2}}{8+16 p}$
(n) $\frac{8 c+4 d}{6 a c+3 a d}$
(o) $\frac{8 n^{2}-2 n}{12 n-3}$
(p) $\frac{15 x^{2}+6 x y}{10 x+4 y}$

Simplify the following by first factorising the numerator and/or denominator:
(a) $\frac{b^{2}-4}{b+2}$
(b) $\frac{x^{2}-81}{x-9}$
(c) $\frac{a^{2}-25}{a+5}$
(d) $\frac{y^{2}-36}{y+6}$
(e) $\frac{c^{2}-49}{2 c-14}$
(f) $\frac{a^{2}-64}{2 a+16}$
(g) $\frac{p^{2}-1}{5 p-5}$
(h) $\frac{q^{2}-9}{3 q+9}$
(i) $\frac{a^{2}-b^{2}}{3 a+3 b}$
(j) $\frac{x^{2}-y^{2}}{5 x-5 y}$
(k) $\frac{2 m^{2}-18}{2 m+6}$
(l) $\frac{3 d^{2}-48}{12 d-48}$
(m) $\frac{x^{2}+3 x+2}{x+1}$
(n) $\frac{p-1}{p^{2}-2 p+1}$
(o) $\frac{a x-5 a}{x^{2}-25}$
(p) $\frac{a^{2}-1}{a^{2}+2 a+1}$
(q) $\frac{b^{2}+6 p-9}{b^{2}-9}$
(r) $\frac{c^{2}+2 c-15}{c^{2}-25}$
(s) $\frac{3 x^{2}+5 x-2}{x^{2}-4}$
(t) $\frac{y^{2}+6 y+8}{y^{2}+y-12}$
(u) $\frac{p^{2}-4 p-5}{p^{2}+2 p+1}$
(v) $\frac{c^{2}+4 c-32}{c^{2}+c-56}$
(w) $\frac{2 x^{2}+13 x+6}{x^{2}+9 x+18}$
(x) $\frac{6 a^{2}-13 a-5}{3 a^{2}-11 a-4}$
(y) $\frac{10 b^{2}-33 b-7}{10 b^{2}-37 b+7}$

## Adding and Subtracting Algebraic Fractions

Express each sum as a fraction in its simplest form:
(a) $\frac{a}{5}+\frac{a}{5}$
(b) $\frac{2 b}{5}+\frac{b}{10}$
(c) $\frac{3 x}{4}+\frac{x}{8}$
(d) $\frac{p}{6}+\frac{2 p}{3}$
(e) $\frac{y}{9}+\frac{2 y}{3}$
(f) $\frac{3}{m}+\frac{2}{m}$
(g) $\frac{5}{x}+\frac{1}{x}$
(h) $\frac{2}{a}+\frac{5}{2 a}$
(i) $\frac{4}{3 y}+\frac{3}{y}$
(j) $\frac{8}{p}+\frac{3}{5 p}$
(k) $\frac{3}{a}+\frac{2}{b}$
(I) $\frac{5}{x}+\frac{3}{y}$

Express each difference as a fraction in its simplest form:
(a) $\frac{3 a}{5}-\frac{a}{5}$
(b) $\frac{2 b}{5}-\frac{b}{10}$
(c) $\frac{3 x}{4}-\frac{x}{8}$
(d) $\frac{5 p}{6}-\frac{2 p}{3}$
(e) $\frac{8 y}{9}-\frac{2 y}{3}$
(f) $\frac{5}{m}-\frac{2}{m}$
(g) $\frac{7}{x}-\frac{3}{x}$
(h) $\frac{5}{a}-\frac{1}{2 a}$
(i) $\frac{8}{3 y}-\frac{2}{y}$
(i) $\frac{8}{p}-\frac{3}{5 p}$
(k) $\frac{3}{a}-\frac{2}{b}$
(I) $\frac{5}{x}-\frac{3}{y}$

Simplify the following:
(a) $\frac{x+2}{3}+\frac{x+3}{6}$
(b) $\frac{a+6}{4}+\frac{a-2}{3}$
(c) $\frac{d-3}{2}-\frac{d+2}{6}$
(d) $\frac{2 a-1}{4}-\frac{a+2}{5}$
(e) $\frac{a+3 b}{2}+\frac{a-2 b}{4}$
(f) $\frac{2 u+v}{3}-\frac{u-v}{4}$
(g) $\frac{2}{x+3}+\frac{3}{x+2}$
(h) $\frac{4}{x+5}+\frac{5}{x+1}$
(i) $\frac{7}{x-3}+\frac{4}{x+2}$
(j) $\frac{2}{x+4}-\frac{3}{x-3}$
(k) $\frac{1}{x-3}-\frac{5}{x-2}$
(I) $\frac{2}{x-5}-\frac{3}{x-4}$
Express as a single fraction in its simplest form

$$
\frac{1}{x-2}+\frac{1}{x^{2}+x-6}
$$

## Multiplying and Dividing Algebraic Fractions

Express each product as a fraction in its simplest form
(a) $\frac{x}{3} \times \frac{x}{6}$
(b) $\frac{y}{2} \times \frac{y}{4}$
(c) $\frac{a}{2} \times \frac{b}{7}$
(d) $\frac{p}{3} \times \frac{q}{8}$
(e) $\frac{c^{2}}{5} \times \frac{c}{6}$
(f) $\frac{6}{a} \times \frac{2}{a}$
(g) $\frac{3}{x} \times \frac{10}{y}$
(h) $\frac{3}{p} \times \frac{4}{p}$
(i) $\frac{2}{3 m} \times \frac{4}{5 m}$
(i) $\frac{1}{b} \times \frac{11}{3 c}$
(k) $\frac{5 m}{6} \times \frac{3}{2 m}$
(l) $\frac{5}{7 x} \times \frac{4 x}{3}$
(m) $\frac{2 y}{9} \times \frac{12}{5 y^{2}}$
(n) $\frac{2}{3 a} \times \frac{3}{7 a^{2}}$
(o) $\frac{5}{3 p} \times \frac{2}{p^{3}}$
(p) $\frac{3 t^{2}}{5 s} \times \frac{2 s^{2}}{6 t^{3}}$
(q) $\frac{5 p q}{2} \times \frac{3}{4 p q^{2}}$
(r) $\frac{7 a b^{2}}{6 c} \times \frac{2 c^{3}}{3 a^{2}}$
(s) $\frac{4}{5 m n} \times \frac{2 m^{4}}{n^{2}}$
(t) $\frac{4 y z}{9 x} \times \frac{3 x z}{2 y^{3}}$
(u) $\frac{5 a b^{3}}{3 c} \times \frac{3 a}{2 b c^{2}}$
(v) $\frac{2 c d}{7 a} \times \frac{3 a^{2}}{4 c d^{2}}$
(w) $\frac{10 x y^{2}}{3} \times \frac{12 x y}{5 y^{2}}$
(x) $\frac{3}{8 s^{3}} \times \frac{4 s t}{t^{3}}$
(y) $\frac{4 p q^{2}}{3 a} \times \frac{6 a^{2}}{5 p^{3}}$

Express as a single fraction:
(a) $\frac{a}{4} \div \frac{a}{2}$
(b) $\quad \frac{x}{2} \div \frac{y}{2}$
(c) $\frac{a b}{5} \div \frac{a}{2}$
(d) $\frac{p^{2}}{10} \div \frac{p}{5}$
(e) $\frac{2 c}{3} \div \frac{c^{2}}{6}$
(f) $\frac{3}{t} \div \frac{6}{t}$
(g) $\frac{2}{k} \div \frac{4}{m}$
(h) $\frac{3}{y} \div \frac{9}{y^{2}}$
(i) $\frac{4}{b c} \div \frac{2}{c}$
(j) $\frac{3}{2 x} \div \frac{12}{x^{2}}$
(k) $\frac{24 x y}{35 z} \div \frac{20 x y}{21 z}$
(l) $\frac{6 q^{2}}{25 p} \div \frac{9 q}{20 p^{2}}$
(m) $\frac{8 a b}{21 c} \div \frac{9 b}{14 a c}$
(n) $\frac{10 m}{21 n^{2}} \div \frac{8 m n}{9}$
(o) $\frac{20 a x}{33 y} \div \frac{15 x}{44 a y^{2}}$

