Algebraic Fractions Lesson Practice

Simplifying Basic Algebraic Fractions

Express these fractions in their simplest form:

(a)
$$\frac{3}{6}$$
 (b) $\frac{8}{12}$ (c) $\frac{30}{16}$ (d) $\frac{54}{72}$

(e)
$$\frac{10a}{5}$$
 (f) $\frac{9b}{6}$ (g) $\frac{18}{12x}$ (h) $\frac{25}{15y}$

(i)
$$\frac{4c}{16c^2}$$
 (j) $\frac{32a}{8a^3}$ (k) $\frac{13p^2}{52p^3}$ (l) $\frac{36ab}{6bc}$

(m)
$$\frac{4a}{2a^2}$$
 (n) $\frac{10x^2}{12xy}$ (o) $\frac{3v^2t}{9vt^2}$ (p) $\frac{10ab^3}{2a^2b}$

(q)
$$\frac{30p^2q}{25pq^2}$$
 (r) $\frac{81x^2y^2}{6y^2}$ (s) $\frac{42mn^2}{56mn}$ (t) $\frac{8def^2}{10e^2f}$

(u)
$$\frac{3ab^2c}{4a^2c}$$
 (v) $\frac{4k^2m}{28km^2}$ (w) $\frac{5efg^2}{10e^2fg^3}$ (x) $\frac{21xy^2}{36x^3}$

Simplifying Algebraic Fractions by Factorising

Simplify by first finding the common factor:

(a)
$$\frac{3a+6b}{6}$$
 (b) $\frac{4x+12y}{2}$ (c) $\frac{3a+a^2}{ab}$ (d) $\frac{xy+y^2}{2y}$

(e)
$$\frac{xy+x^2}{6x+xy}$$
 (f) $\frac{3ab+6b^2}{9b^2}$ (g) $\frac{25b^2+15b^3}{10b}$ (h) $\frac{14p+10q}{2s}$

(i)
$$\frac{3a}{2ab-ac}$$
 (j) $\frac{6x}{9x+9y}$ (k) $\frac{2st}{6rs-2st}$ (l) $\frac{5c}{10ac+15bc}$

(m)
$$\frac{14p+28p^2}{8+16p}$$
 (n) $\frac{8c+4d}{6ac+3ad}$ (o) $\frac{8n^2-2n}{12n-3}$ (p) $\frac{15x^2+6xy}{10x+4y}$

Simplify the following by first factorising the numerator and/or denominator:

(a)
$$\frac{b^2-4}{b+2}$$
 (b) $\frac{x^2-81}{x-9}$ (c) $\frac{a^2-25}{a+5}$ (d) $\frac{y^2-36}{y+6}$

(e)
$$\frac{c^2 - 49}{2c - 14}$$
 (f) $\frac{a^2 - 64}{2a + 16}$ (g) $\frac{p^2 - 1}{5p - 5}$ (h) $\frac{q^2 - 9}{3q + 9}$

(i)
$$\frac{a^2 - b^2}{3a + 3b}$$
 (j) $\frac{x^2 - y^2}{5x - 5y}$ (k) $\frac{2m^2 - 18}{2m + 6}$ (l) $\frac{3d^2 - 48}{12d - 48}$

(m)
$$\frac{x^2+3x+2}{x+1}$$
 (n) $\frac{p-1}{p^2-2p+1}$ (o) $\frac{ax-5a}{x^2-25}$ (p) $\frac{a^2-1}{a^2+2a+1}$

(q)
$$\frac{b^2 + 6p - 9}{b^2 - 9}$$
 (r) $\frac{c^2 + 2c - 15}{c^2 - 25}$ (s) $\frac{3x^2 + 5x - 2}{x^2 - 4}$

(t)
$$\frac{y^2 + 6y + 8}{y^2 + y - 12}$$
 (u) $\frac{p^2 - 4p - 5}{p^2 + 2p + 1}$ (v) $\frac{c^2 + 4c - 32}{c^2 + c - 56}$

(w)
$$\frac{2x^2 + 13x + 6}{x^2 + 9x + 18}$$
 (x) $\frac{6a^2 - 13a - 5}{3a^2 - 11a - 4}$ (y) $\frac{10b^2 - 33b - 7}{10b^2 - 37b + 7}$

Adding and Subtracting Algebraic Fractions

Express each sum as a fraction in its simplest form:

- (a) $\frac{a}{5} + \frac{a}{5}$ (b) $\frac{2b}{5} + \frac{b}{10}$ (c) $\frac{3x}{4} + \frac{x}{8}$ (d) $\frac{p}{6} + \frac{2p}{3}$ (e) $\frac{y}{9} + \frac{2y}{3}$ (f) $\frac{3}{m} + \frac{2}{m}$ (g) $\frac{5}{x} + \frac{1}{x}$ (h) $\frac{2}{a} + \frac{5}{2a}$
- (i) $\frac{4}{3y} + \frac{3}{y}$ (j) $\frac{8}{p} + \frac{3}{5p}$ (k) $\frac{3}{a} + \frac{2}{b}$ (l) $\frac{5}{x} + \frac{3}{y}$

Express each difference as a fraction in its simplest form:

(a) $\frac{3a}{5} - \frac{a}{5}$ (b) $\frac{2b}{5} - \frac{b}{10}$ (c) $\frac{3x}{4} - \frac{x}{8}$ (d) $\frac{5p}{6} - \frac{2p}{3}$

(e)
$$\frac{8y}{9} - \frac{2y}{3}$$
 (f) $\frac{5}{m} - \frac{2}{m}$ (g) $\frac{7}{x} - \frac{3}{x}$ (h) $\frac{5}{a} - \frac{1}{2a}$

(i)
$$\frac{8}{3y} - \frac{2}{y}$$
 (j) $\frac{8}{p} - \frac{3}{5p}$ (k) $\frac{3}{a} - \frac{2}{b}$ (l) $\frac{5}{x} - \frac{3}{y}$

Simplify the following:

(a)
$$\frac{x+2}{3} + \frac{x+3}{6}$$
 (b) $|\frac{a+6}{4} + \frac{a-2}{3}$ (c) $\frac{d-3}{2} - \frac{d+2}{6}$
(d) $\frac{2a-1}{4} - \frac{a+2}{5}$ (e) $\frac{a+3b}{2} + \frac{a-2b}{4}$ (f) $\frac{2u+v}{3} - \frac{u-v}{4}$
(g) $\frac{2}{x+3} + \frac{3}{x+2}$ (h) $\frac{4}{x+5} + \frac{5}{x+1}$ (i) $\frac{7}{x-3} + \frac{4}{x+2}$
(j) $\frac{2}{x+4} - \frac{3}{x-3}$ (k) $\frac{1}{x-3} - \frac{5}{x-2}$ (l) $\frac{2}{x-5} - \frac{3}{x-4}$
Express as a single fraction in its simplest form
 $\frac{1}{x-2} + \frac{1}{x^2+x-6}$

Multiplying and Dividing Algebraic Fractions

Express each product as a fraction in its simplest form

(a)
$$\frac{x}{3} \times \frac{x}{6}$$
 (b) $\frac{y}{2} \times \frac{y}{4}$ (c) $\frac{a}{2} \times \frac{b}{7}$ (d) $\frac{p}{3} \times \frac{q}{8}$
(e) $\frac{c^2}{5} \times \frac{c}{6}$ (f) $\frac{6}{a} \times \frac{2}{a}$ (g) $\frac{3}{x} \times \frac{10}{y}$ (h) $\frac{3}{p} \times \frac{4}{p}$
(i) $\frac{2}{3m} \times \frac{4}{5m}$ (j) $\frac{1}{b} \times \frac{11}{3c}$ (k) $\frac{5m}{6} \times \frac{3}{2m}$ (l) $\frac{5}{7x} \times \frac{4x}{3}$
(m) $\frac{2y}{9} \times \frac{12}{5y^2}$ (n) $\frac{2}{3a} \times \frac{3}{7a^2}$ (o) $\frac{5}{3p} \times \frac{2}{p^3}$ (p) $\frac{3t^2}{5s} \times \frac{2s^2}{6t^3}$
(q) $\frac{5pq}{2} \times \frac{3}{4pq^2}$ (r) $\frac{7ab^2}{6c} \times \frac{2c^3}{3a^2}$ (s) $\frac{4}{5mn} \times \frac{2m^4}{n^2}$
(t) $\frac{4yz}{9x} \times \frac{3xz}{2y^3}$ (n) $\frac{5ab^3}{3c} \times \frac{3a}{2bc^2}$ (v) $\frac{2cd}{7a} \times \frac{3a^2}{4cd^2}$
(w) $\frac{10xy^2}{3} \times \frac{12xy}{5y^2}$ (x) $\frac{3}{8s^3} \times \frac{4st}{t^3}$ (y) $\frac{4pq^2}{3a} \times \frac{6a^2}{5p^3}$

Express as a single fraction:

(a)
$$\frac{a}{4} \div \frac{a}{2}$$
 (b) $| \frac{x}{2} \div \frac{y}{2}$ (c) $\frac{ab}{5} \div \frac{a}{2}$

(d)
$$\frac{p^2}{10} \div \frac{p}{5}$$
 (e) $\frac{2c}{3} \div \frac{c^2}{6}$ (f) $\frac{3}{t} \div \frac{6}{t}$

(g) $\frac{2}{k} \div \frac{4}{m}$ (h) $\frac{3}{y} \div \frac{9}{y^2}$ (i) $\frac{4}{bc} \div \frac{2}{c}$

(j) $\frac{3}{2x} \div \frac{12}{x^2}$ (k) $\frac{24xy}{35z} \div \frac{20xy}{21z}$ (l) $\frac{6q^2}{25p} \div \frac{9q}{20p^2}$

(m)
$$\frac{8ab}{21c} \div \frac{9b}{14ac}$$
 (n) $\frac{10m}{21n^2} \div \frac{8mn}{9}$ (o) $\frac{20ax}{33y} \div \frac{15x}{44ay^2}$