

# Fractions

And the four operations!

# Starter Questions

05:00

1. A triangle has lengths 8.5cm, 6.4cm and 10.5cm. Is it a right angled triangle?
2. A model plane is similar to a real aircraft. The model plane is 250 times smaller. What is the volume scale factor between the planes?
3. Solve:  $5x + 3 = 2x + 7$

# Fractions of a quantity

3

5

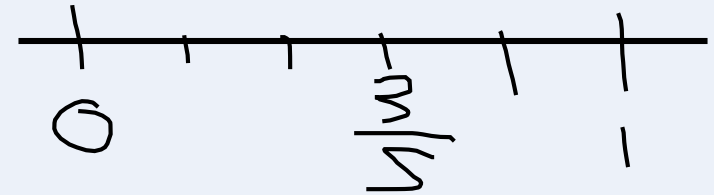
of an object



3

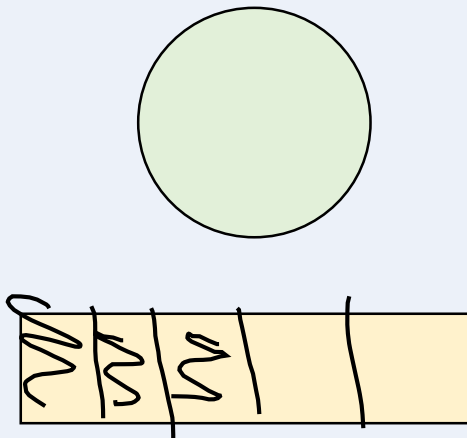
5

on number line



3

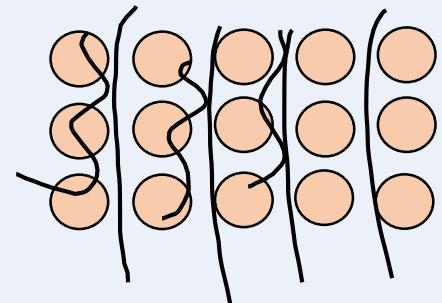
5



3

5

of a number



# Fractions of a quantity

$$\frac{5}{11} \text{ of } 66 = 66 \div 11 \times 5 = 30 \quad \frac{3}{5} \times 50 = 50 \div 5 \times 3 = 30$$

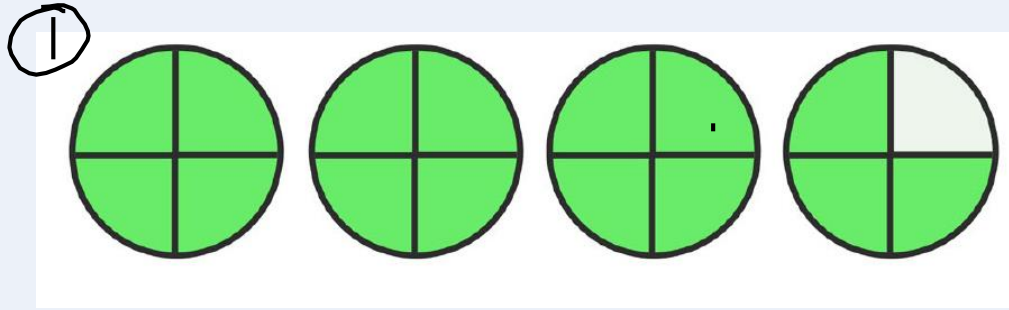
$$\frac{3}{4} \text{ of } 4 = 4 \div 4 \times 3 = 3$$

$$\frac{4}{7} \times 49 = 42$$

$$\frac{5}{6} \times 42 = 42 \div 6 \times 5 = 35 \quad \frac{7}{10} \times 110 = 77$$

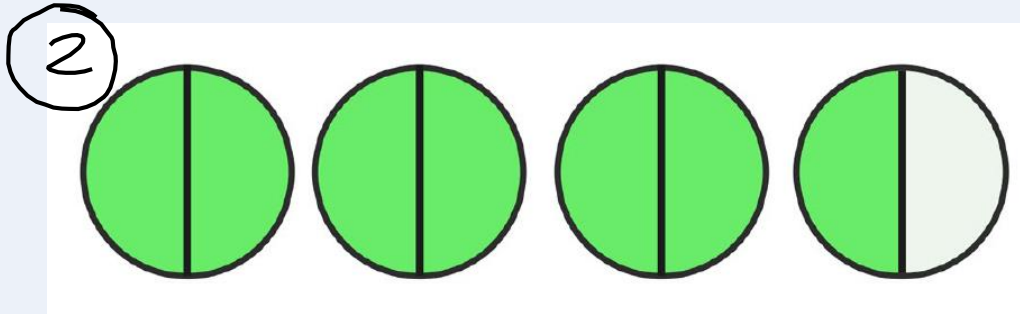
# Mixed Numbers $\leftrightarrow$ Improper Fractions

$$3 \frac{3}{4}$$



$$\frac{15}{4}$$

$$3 \frac{1}{2}$$



$$3 \frac{1}{2}$$

$$10$$

④

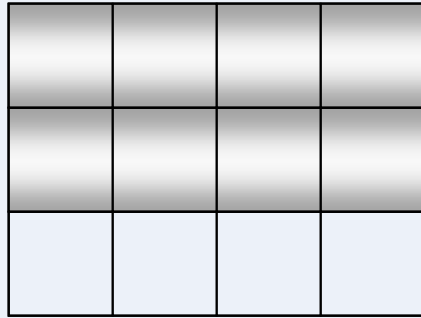
$$10 \frac{2}{5}$$

$$10 \frac{2}{5} = \frac{10 \times 5 + 2}{5}$$

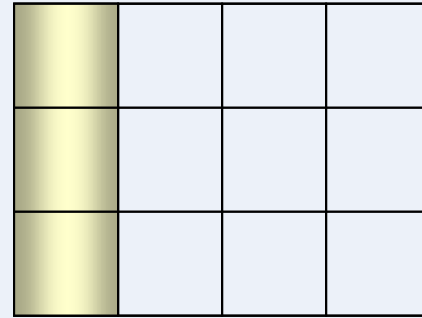
⑤

$$\frac{15}{3}$$
$$5 \frac{2}{5}$$

$$\frac{2}{3}$$



+



$$\frac{1}{4}$$

Equivalent

$$\frac{8}{12}$$

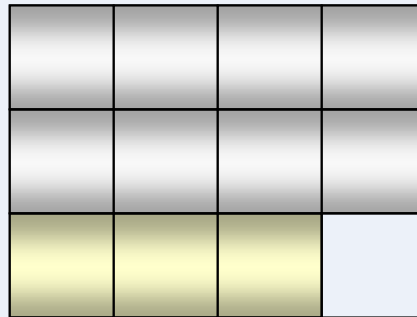
+

$$\frac{3}{12}$$

Equivalent

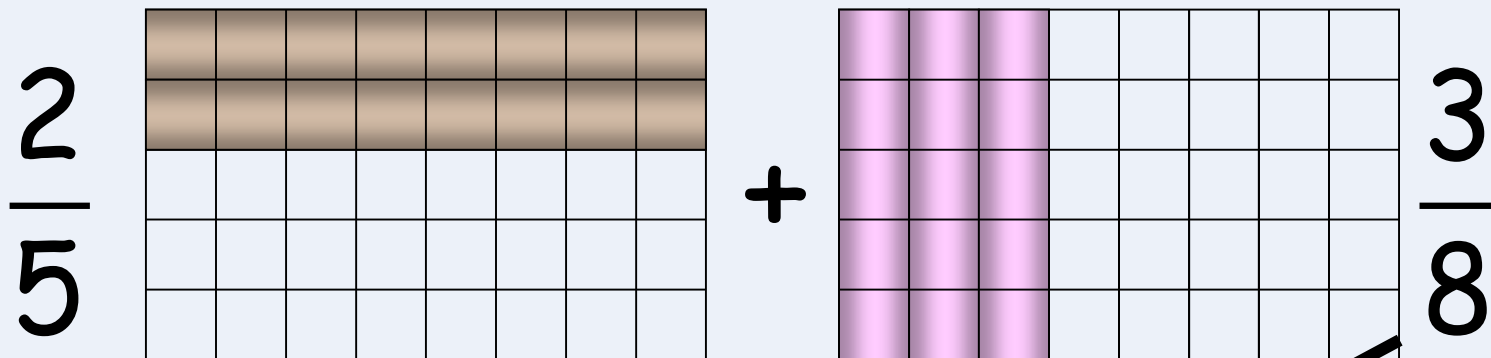
+ Diagram  
1

=



$$\frac{11}{12}$$

Multiples of 3 and 4	
3	4
6	8
9	12
12	16
15	20
12 is the LCM	



Equivalent

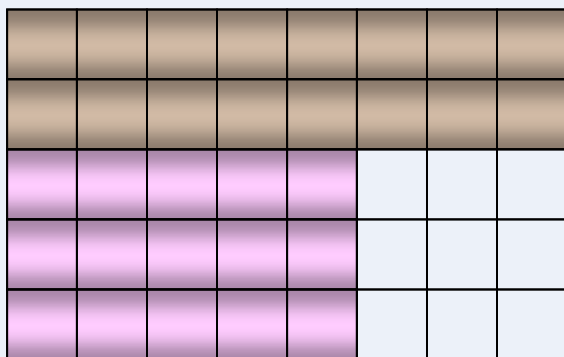
$$\frac{16}{40}$$

+

$$\frac{15}{40}$$

Equivalent

=



$$\frac{31}{40}$$

+ Diagram 2

Multiples of 5 and 8	
5	8
10	16
15	32
20	40
25	48
30	56
35	64
40	72
40 is the LCM	

# Adding Fractions

$$\frac{2}{3} + \frac{4}{5} =$$



## Worked Example

$$\frac{1}{7} + \frac{2}{5}$$

$$= \frac{5}{35} + \frac{14}{35}$$

$$= \frac{19}{35}$$

## Your Turn

$$\frac{1}{6} + \frac{3}{5}$$

$$= \frac{5}{30} + \frac{18}{30}$$

$$= \frac{23}{30}$$

05:00

1.  $\frac{1}{8} + \frac{2}{8}$

6.  $\frac{1}{4} + \frac{1}{5}$

11.  $\frac{2}{9} + \frac{2}{5}$

16.  $\frac{3}{9} + \frac{3}{7}$

2.  $\frac{1}{8} + \frac{4}{8}$

7.  $\frac{1}{4} + \frac{2}{5}$

12.  $\frac{3}{9} + \frac{2}{5}$

17.  $\frac{2}{9} + \frac{3}{7}$

3.  $\frac{1}{8} + \frac{1}{2}$

8.  $\frac{1}{4} + \frac{3}{5}$

13.  $\frac{4}{9} + \frac{2}{5}$

18.  $\frac{x}{9} + \frac{3}{7}$

4.  $\frac{1}{4} + \frac{1}{2}$

9.  $\frac{1}{9} + \frac{3}{5}$

14.  $\frac{4}{9} + \frac{2}{7}$

19.  $\frac{x}{9} + \frac{y}{7}$

5.  $\frac{1}{4} + \frac{1}{3}$

10.  $\frac{1}{9} + \frac{2}{5}$

15.  $\frac{4}{9} + \frac{3}{7}$

20.  $\frac{x}{9} + \frac{x}{7}$

$$1. \quad \frac{1}{8} + \frac{2}{8} \quad \frac{3}{8}$$

$$2. \quad \frac{1}{8} + \frac{4}{8} \quad \frac{5}{8}$$

$$3. \quad \frac{1}{8} + \frac{1}{2} \quad \frac{5}{8}$$

$$4. \quad \frac{1}{4} + \frac{1}{2} \quad \frac{3}{4}$$

$$5. \quad \frac{1}{4} + \frac{1}{3} \quad \frac{7}{12}$$

$$6. \quad \frac{1}{4} + \frac{1}{5} \quad \frac{9}{20}$$

$$7. \quad \frac{1}{4} + \frac{2}{5} \quad \frac{13}{20}$$

$$8. \quad \frac{1}{4} + \frac{3}{5} \quad \frac{17}{20}$$

$$9. \quad \frac{1}{9} + \frac{3}{5} \quad \frac{14}{45}$$

$$10. \quad \frac{1}{9} + \frac{2}{5} \quad \frac{23}{45}$$

$$= \frac{10}{16}$$

$$\frac{32}{45}$$

$$11. \quad \frac{2}{9} + \frac{2}{5} \quad \frac{28}{45}$$

$$12. \quad \frac{3}{9} + \frac{2}{5} \quad \frac{33}{45}$$

$$13. \quad \frac{4}{9} + \frac{2}{5} \quad \frac{38}{45}$$

$$14. \quad \frac{4}{9} + \frac{2}{7} \quad \frac{46}{63}$$

$$15. \quad \frac{4}{9} + \frac{3}{7} \quad \frac{55}{63}$$

$$16. \quad \frac{3}{9} + \frac{3}{7} \quad \frac{48}{63}$$

$$17. \quad \frac{2}{9} + \frac{3}{7} \quad \frac{41}{63}$$

$$18. \quad \frac{x}{9} + \frac{3}{7} \quad \frac{7x+27}{63}$$

$$19. \quad \frac{x}{9} + \frac{y}{7} \quad \frac{7x+9y}{63}$$

$$20. \quad \frac{x}{9} + \frac{x}{7} \quad \frac{16x}{63}$$

## Worked Example

$$\frac{2}{5} - \frac{1}{3}$$

$$= \frac{6}{15} - \frac{5}{15}$$

$$= \frac{1}{15}$$

## Your Turn

$$\frac{2}{3} - \frac{1}{5}$$

$$= \frac{10}{15} - \frac{3}{15}$$

$$= \frac{7}{15}$$

05:00

1.  $\frac{2}{5} - \frac{1}{7}$

2.  $\frac{1}{7} - \frac{2}{5}$

3.  $\frac{2}{5} - \frac{2}{7}$

4.  $\frac{2}{3} - \frac{2}{5}$

5.  $\frac{2}{3} - \frac{1}{4}$

6.  $\frac{2}{3} - \frac{3}{4}$

7.  $\frac{3}{4} - \frac{2}{3}$

8.  $\frac{3}{4} - \frac{2}{30}$

9.  $\frac{3}{4} - \frac{3}{5}$

10.  $\frac{3}{4} - \frac{9}{15}$

$$1. \quad \frac{2}{5} - \frac{1}{7} = \frac{9}{35}$$

$$2. \quad \frac{1}{7} - \frac{2}{5} = -\frac{9}{35}$$

$$3. \quad \frac{2}{5} - \frac{2}{7} = \frac{4}{35}$$

$$4. \quad \frac{2}{3} - \frac{2}{5} = \frac{4}{15}$$

$$5. \quad \frac{2}{3} - \frac{1}{4} = \frac{5}{12}$$

$$6. \quad \frac{2}{3} - \frac{3}{4} = -\frac{1}{12}$$

$$7. \quad \frac{3}{4} - \frac{2}{3} = \frac{1}{12}$$

$$8. \quad \frac{3}{4} - \frac{2}{30} = \frac{41}{60}$$

$$9. \quad \frac{3}{4} - \frac{3}{5} = \frac{3}{20}$$

$$10. \quad \frac{3}{4} - \frac{9}{15} = \frac{3}{20}$$

## Explain

This can be simplified to  $\frac{3}{4} \times \frac{1}{3} = \frac{3}{12} = \frac{1}{4}$

$\frac{3}{12}$		

$$\frac{1}{3} \times \frac{3}{4}$$

## Worked Example

$$\frac{2}{3} \times \frac{5}{8}$$

$$= \frac{10}{24}$$

$$= \frac{5}{12}$$

## Your Turn

$$\frac{2}{3} \times \frac{7}{10}$$

$$= \frac{14}{30}$$

$$= \frac{7}{15}$$

$$= \frac{2}{2}$$



1.  $\frac{1}{2} \times \frac{2}{5} = ?$

2.  $\frac{2}{5} \times \frac{1}{2} = ?$

3.  $\frac{2}{5} \times \frac{1}{3} = ?$

4.  $\frac{2}{5} \times \frac{1}{4} = ?$

5.  $\frac{2}{5} \times \frac{3}{4} = ?$

6.  $\left(\frac{3}{4}\right)^2 = ?$   $\frac{3}{4} \times \frac{3}{4}$

7.  $\frac{0}{5} \times \frac{3}{4} = ?$

8.  $\frac{2}{3} \times \frac{5}{7} = ?$

9.  $\frac{2}{3} \times \frac{5}{?} = \frac{10}{12}$

10.  $\frac{2}{3} \times ? = \frac{2}{6}$

11.  $\frac{2}{?} \times \frac{5}{?} = \frac{10}{9}$

12.  $\frac{2}{3} \times \frac{a}{b} = ?$

13.  $\frac{a}{b} \times \frac{a}{b} = ?$

14.  $\frac{b}{a} \times \frac{a}{b} = ?$

15.  $\frac{2}{3} \times \frac{3}{5} \times \frac{4}{7} = ?$

16.  $\frac{2}{3} \times \frac{3}{5} \times \frac{9}{11} = ?$

17.  $\left(\frac{2}{3}\right)^2 = ?$

18.  $\frac{2}{3} \times \left(\frac{3}{5}\right)^2 = ?$

$$1. \quad \frac{1}{2} \times \frac{2}{5} = \frac{2}{10} = \frac{1}{5}$$

$$2. \quad \frac{2}{5} \times \frac{1}{2} = \frac{2}{10} = \frac{1}{5}$$

$$3. \quad \frac{2}{5} \times \frac{1}{3} = \frac{2}{15}$$

$$4. \quad \frac{2}{5} \times \frac{1}{4} = \frac{2}{20} = \frac{1}{10}$$

$$5. \quad \frac{2}{5} \times \frac{3}{4} = \frac{6}{20} = \frac{3}{10}$$

$$6. \quad \left(\frac{3}{4}\right)^2 = \frac{9}{16}$$

$$7. \quad \frac{0}{5} \times \frac{3}{4} = \frac{0}{20} = 0$$

$$8. \quad \frac{2}{3} \times \frac{5}{7} = \frac{10}{21}$$

$$9. \quad \frac{2}{3} \times \frac{5}{4} = \frac{10}{12}$$

$$10. \quad \frac{2}{3} \times \frac{1}{2} = \frac{2}{6}$$

$$11. \quad \frac{2}{3} \times \frac{5}{3} = \frac{10}{9}$$

$$12. \quad \frac{2}{3} \times \frac{a}{b} = \frac{2a}{3b}$$

$$13. \quad \frac{a}{b} \times \frac{a}{b} = \frac{a^2}{b^2}$$

$$14. \quad \frac{b}{a} \times \frac{a}{b} = \frac{ab}{ab} = 1$$

$$15. \quad \frac{2}{3} \times \frac{3}{5} \times \frac{4}{7} = \frac{24}{105}$$

$$16. \quad \frac{2}{3} \times \frac{3}{5} \times \frac{9}{11} = \frac{54}{165} = \frac{18}{55}$$

$$17. \quad \left(\frac{2}{3}\right)^2 = \frac{4}{9}$$

$$18. \quad \frac{2}{3} \times \left(\frac{3}{5}\right)^2 = \frac{18}{75}$$

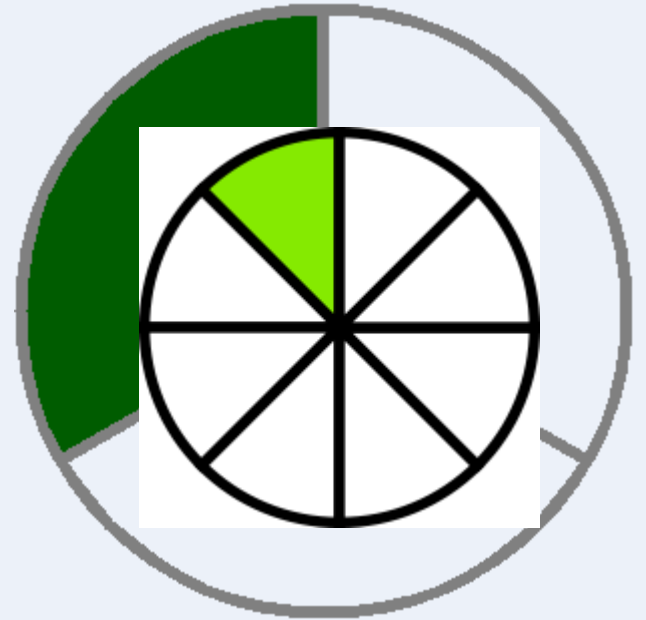
# Dividing fractions

- What is  $\frac{2}{3} \div \frac{1}{3}$ ?

$$= \frac{2}{3} \times \frac{3}{1} = \frac{6}{3} = 2$$

- What about  $\frac{12}{8} \div \frac{4}{8}$ ?

$$= \frac{12}{8} \times \frac{8}{4} = \frac{96}{32} = 3$$



# Dividing fractions

- We could find a common denominator and then divide the numerators.
- But it's easier to just multiply the first fraction by the reciprocal of the second.

## Worked Example

$$\frac{3}{4} \div \frac{2}{7} = \frac{3}{4} \times \frac{7}{2}$$
$$= \frac{21}{8}$$

## Your Turn

$$\frac{3}{4} \div \frac{4}{7} = \frac{3}{4} \times \frac{7}{4}$$
$$= \frac{21}{16}$$

# Starter Questions

05:00

1. A rectangle is  $\frac{3}{5}$  *cm* long and  $\frac{5}{8}$  *cm* high. Find its perimeter and area.
2. One angle of a triangle is 22 degrees. Its sides are 5cm, 12cm and 13cm. Find the other 2 angles.
3. Solve:  $x + 3 \geq 2x - 10$

# Division with Fractions Notes

1.  $\frac{2}{3} \div \frac{4}{5} =$

2.  $\frac{4}{6} \div \frac{4}{5} =$

3.  $\frac{4}{3} \div \frac{4}{5} =$

4.  $\frac{4}{3} \div \frac{2}{5} =$

5.  $\frac{3}{4} \div \frac{2}{5} =$

6.  $\frac{3}{4} \div \frac{5}{2} =$

7.  $\frac{3}{4} \div \frac{1}{2} =$

8.  $\frac{1}{2} \div \frac{3}{4} =$

9.  $\frac{1}{2} \div \frac{1}{4} =$

10.  $\frac{1}{2} \div 4 =$

11.  $\frac{1}{3} \div 4 =$

12.  $4 \div \frac{1}{3} =$

13.  $4 \div \frac{7}{3} =$

14.  $20 \div \frac{7}{3} =$

15.  $5 \div \frac{7}{12} =$

16.  $\frac{1}{5} \div \frac{7}{15} =$

17.  $\frac{1}{5} \div 1\frac{13}{15} =$

18.  $\frac{a}{5} \div 1\frac{13}{15} =$

19.  $\frac{1}{b} \div 1\frac{13}{15} =$

20.  $\frac{1}{5} \div 1\frac{c}{15} =$

21.  $\frac{1}{5} \div 1\frac{13}{d} =$



# Plenary

$$\frac{3}{4} + \left( \frac{5}{2} - \frac{4}{5} \right) = \frac{3}{4} + \left( \frac{25}{10} - \frac{8}{10} \right)$$
$$= \frac{3}{4} + \frac{17}{10} = \frac{15}{20} + \frac{34}{20}$$

$$1\frac{2}{3} \times 3\frac{5}{6} = \frac{5}{3} \times \frac{23}{6} = \frac{49}{20}$$
$$= \frac{115}{18} = 6\frac{7}{18}$$

# Percentage Change

# Recap

- How do we find:

- 10%

$$\div 10$$

$$\times 0.1$$

- 50%

$$\div 2$$

$$\times 0.5$$

- 1%

$$\div 100$$

$$\times 0.01$$

- 30%

$$\div 10 \times 3$$

$$\times 0.3$$

- 20%

$$\div 10 \times 2 \quad \div 5$$

$$\times 0.2$$

- 17.5%

$$\times 0.175$$

- 250%

$$\times 2 + (\div 2)$$

$$\times 2.5$$

# Decimal Multipliers

Increase by 5%

$$100\% + 5\% \\ = 1 + 0.05 = 1.05$$

Decrease by 2.3%

$$100\% - 2.3\% = 97.7\% \\ = 1 - 0.023 \\ = 0.977$$

Worked Example

Your Turn

*Increase 40 by 10%*

$$= 40 \times 1.1$$

$$= 44$$

$$100\% + 10\%$$

$$= 110\%$$

$$= 1.1$$

*Increase 90 by 10%*

$$= 90 \times 1.1$$

$$= 99$$

Worked Example

*Decrease 70 by 25%*

$$\begin{aligned} &= 70 \times 0.75 \\ &= 52.5 \end{aligned}$$

$$\begin{aligned} &100\% - 25\% \\ &= 75\% \\ &= 0.75 \end{aligned}$$

Your Turn

*Decrease 40 by 45%*

$$\begin{aligned} &= 40 \times 0.55 \\ &= 22 \end{aligned}$$

$$\begin{aligned} &100\% - 45\% \\ &= 55\% \\ &= 0.55 \end{aligned}$$

1. *Increase 30 by 10%*
2. *Decrease 30 by 20%*
3. *Increase 60 by 20%*
4. *Decrease 60 by 10%*
5. *Increase 74 by 10%*
6. *Decrease 74 by 50%*
7. *Increase 84 by 50%*
8. *Decrease 84 by 10%*
9. *Increase 84 by 5%*

10. *Increase 44 by 5%*
11. *Decrease 44 by 10%*
12. *Increase 44 by 20%*
13. *Decrease 44 by 50%*
14. *Increase 44 by 60%*
15. *Decrease 88 by 60%*
16. *Increase 88 by 30%*
17. *Decrease 88 by 15%*
18. *Increase 88 by 10%*

1. Increase 30 by 10%	33	10. Increase 44 by 5%	46.2
2. Decrease 30 by 20%	24	11. Decrease 44 by 10%	39.6
3. Increase 60 by 20%	72	12. Increase 44 by 20%	52.8
4. Decrease 60 by 10%	54	13. Decrease 44 by 50%	22
5. Increase 74 by 10%	81.4	14. Increase 44 by 60%	70.4
6. Decrease 74 by 50%	37	15. Decrease 88 by 60%	35.2
7. Increase 84 by 50%	126	16. Increase 88 by 30%	114.4
8. Decrease 84 by 10%	75.6	17. Decrease 88 by 15%	74.8
9. Increase 84 by 5%	88.2	18. Increase 88 by 10%	96.8



Use these 12 numbers, once each, in the gaps below.

**10, 20, 25, 35, 40, 50, 60, 70, 75, 80, 90, 100**

£ \_\_\_\_\_ increased by \_\_\_\_\_ % = £ \_\_\_\_\_

£ \_\_\_\_\_ increased by \_\_\_\_\_ % = £ \_\_\_\_\_

£ \_\_\_\_\_ decreased by \_\_\_\_\_ % = £ \_\_\_\_\_

£ \_\_\_\_\_ decreased by \_\_\_\_\_ % = £ \_\_\_\_\_

Notes Page 39

1. A golf professional gives 5% of his winnings to his caddy. How much does the professional keep for himself if he wins £120,000?

$$100\% - 5\% \\ = 95\% = 0.95$$

$$120000 \times 0.95 \\ = \pounds 114000$$

2. The cost of a washing machine before VAT is £240. Calculate the price after VAT at 20% is added.

$$100\% + 20\% \\ = 120\% = 1.2$$

$$240 \times 1.2 = \pounds 288$$

3. A TV is reduced by 15% in the sale. It originally cost £600. How much does it cost now?

$$600 \times 0.85 = \pounds 510$$

4. The population of a small town grew by 6.5% over the course of a year. At the start of the year there were 12 400 people. How many were there at the end of the year? Round your answer to 2 SF.

$$12400 \times 1.065 = 13206 = 13000$$

# Worked example- Simple interest

- £600 is invested for 3 years at 3% **simple** interest per year.
- How much will they have at the end of the 3 years?

$$600 \times 0.03 = \text{£}18$$

$$600 + 18 + 18 + 18 = \text{£}654$$

# Your turn

- £650 is invested in a bank account for 2 years at 1.5% **simple** interest per year.
- How much is in the account at the end of the 2 years?

# Worked example- Compound interest

Christian invested £6500 for 2 years in a savings account.

He was paid 4% per annum **compound** interest.

How much money did Christian have in his savings account at the end of 2 years?

$$\begin{array}{l} \text{Y1} \\ \hline \pounds 6500 \times 1.04 = \pounds 6760 \end{array}$$

$$\begin{array}{l} \text{Y2} \\ \hline \pounds 6760 \times 1.04 = \pounds 7030.40 \\ \hline \hline \end{array}$$

$$100\% + 2.5\%$$

$$\begin{array}{l} \text{Your turn} - 102.5\% \\ \hline = 1.025 \end{array}$$

Ben invests £400 in a bank account.

The account pays **compound** interest at a rate of 2.5% per year.

At the end of two years, how much will Ben have in his account?

$$\begin{array}{l} \text{Y1} \\ \hline \pounds 400 \times 1.025 = \pounds 410 \end{array}$$

$$\begin{array}{l} \text{Y2} \\ \hline \pounds 410 \times 1.025 = \pounds 420.25 \\ \hline \hline \end{array}$$

# Worked example- Compound interest

Christian invested £6500 for 2 years in a savings account.

He was paid 4% per annum **compound** interest.

How much money did Christian have in his savings account at the end of 2 years?

$$\begin{aligned} &£6500 \times (1.04)^2 \\ &= \underline{\underline{£7030.40}} \end{aligned}$$

# Your turn

Ben invests £400 in a bank account.

The account pays **compound** interest at a rate of 2.5% per year.

At the end of two years, how much will Ben have in his account?

$$\begin{aligned} &£400 \times (1.025)^2 \\ &= \underline{\underline{£420.25}} \end{aligned}$$

## Worked example- Compound interest

The value of a second-hand car is £6000.

Each year it loses 20% of its value.

Work out its value in 3 years' time.

## Your turn

Emma bought a car for £10,000

Each year the car depreciates by 15%

How much will the car be worth in 2 years' time?

## Worked example- Compound interest

The value of a second-hand car is £6000.

Each year it loses 20% of its value.

Work out its value in 3 years' time.

## Your turn

Emma bought a car for £10,000

Each year the car depreciates by 15%

How much will the car be worth in 2 years' time?



Notes Page 40

- 1. City Police aim to reduce crime figures by 8% each year for the next 3 years. If the current number of crimes committed each year is 25,000, how many do they hope for in 3 years time? Give your answer to the nearest hundred.**
- 2. The number of bacteria in a Petri dish increases at a rate of 3% every hour. If there are 12,000 bacteria at the start, how many will there be in 4 hours? Give your answer to 2SF.**
- 3. The number of subscribers to a new magazine is expected to increase by 24% every year. This year there are 16,500 subscribers. How many subscribers are there expected to be in 3 years time? Give your answer to 3 significant figures.**
- 4. The amount of serum in a patient's bloodstream decreases by 20% every hour. A patient is injected with 6mg of the serum at 9am. How many milligrams will remain in his bloodstream at 1pm? Give your answer to the nearest tenth of a milligram.**
- 5. Jamie bought a house for £120,000. It appreciated in value by 3.7% for each of the next four years. How much was the house worth after four years?**

# Plenary

Sam wants to invest £2000 for 2 years in the same bank.

At the end of 2 years, Sam wants to have as much money as possible.

Which bank should Sam use?

## **Bonus Bank**

Compound Interest  
5% for the first year  
0.5% for each extra year

## **Super Savings Bank**

Compound Interest  
4% for the first year  
1% for each extra year

# Reverse Percentages

1. City Police aim to reduce crime figures by 8% each year for the next 3 years. If the current number of crimes committed each year is 25,000, how many do they hope for in 3 years time? Give your answer to the nearest hundred.

$$25000 \times (0.92)^3 = 19500$$

$$\left. \begin{array}{l} 100\% - 8\% \\ = 92\% \\ = 0.92 \end{array} \right\} \begin{array}{l} 1y \ 25000 \times 0.92 = 23000 \\ 2y \ 23000 \times 0.92 = 21160 \\ 3y \ 21160 \times 0.92 = 19500 \end{array}$$

2. The number of bacteria in a Petri dish increases at a rate of 3% every hour. If there are 12,000 bacteria at the start, how many will there be in 4 hours? Give your answer to 2SF.

$$12000 \times (1.03)^4$$

3. The number of subscribers to a new magazine is expected to increase by 24% every year. This year there are 16,500 subscribers. How many subscribers are there expected to be in 3 years time? Give your answer to 3 significant figures.
4. The amount of serum in a patient's bloodstream decreases by 20% every hour. A patient is injected with 6mg of the serum at 9am. How many milligrams will remain in his bloodstream at 1pm? Give your answer to the nearest tenth of a milligram.
5. Jamie bought a house for £120,000. It appreciated in value by 3.7% for each of the next four years. How much was the house worth after four years?

# Starter Questions

05:00

1. Find the mean of the following numbers:

1, 4, 7, 7, 90, 101

2. Solve the system of equations:

$$5x + 2y = 54$$

$$2x + 2y = 24$$

3.  $6x + 3 - x = 5x + 15$

Comment.

$$6 \div \underline{\underline{6}} = 1$$

$$15 \div \underline{\underline{15}} = 1$$

$$22.5 \div \underline{\underline{22.5}} = 1$$

$$37 \div \underline{\underline{37}} = 1$$

$$72 \div \underline{\underline{72}} = 1$$

$$88 \div \underline{\underline{88}} = 1$$

$$94 \div \underline{\underline{94}} = 1$$

$$104 \div \underline{\underline{104}} = 1$$

$$117.5 \div \underline{\underline{117.5}} = 1$$

$£50 \div 10$   
 $= £5$   
 $£5 \times 7$   
 $= £35$

$\div 70$	$70\% = £35$	$\div 70$
	$1\% = £0.50$	
$\times 100$	$100\% = £50$	$\times 100$

$\div 35$	$35\% = £23.80$	$\div 35$
	$1\% = £0.68$	
$\times 100$	$100\% = £68$	$\times 100$

$\div 88$	$88\% = £220$	$\div 88$
	$1\% = £2.50$	
$\times 100$	$100\% = £250$	$\times 100$



Rob is buying a new car and has seen this advert:

He got a discount of 25% off the price of the car.

He paid £7200 for the car.

Work out the price of the car before the discount.



$$75\% = \text{£}7200$$

$$1\% = \text{£}96$$

$$100\% = \text{£}9600$$

- 75

$\times 100$

# Another example

The price of a washing machine is reduced by 17.5%.

The reduced price is £264.

By how much has the original price been reduced?

$$\begin{array}{l} 82.5\% = \text{£}264 \\ 1\% = \text{£}3.20 \\ 100\% = \text{£}320 \end{array} \quad \begin{array}{l} \div 82.5 \\ \times 100 \end{array}$$

$$\begin{array}{l} 100\% \\ - 17.5\% \\ \hline \end{array}$$

# Reverse Percentages

Find 100% when...

- |   |  |   |
|---|--|---|
| a)<br>15 represents 50%                       | b)<br>12 represents 10%                          | c)<br>8 represents 20%                            |
| d)<br>6 represents 5%                         | e)<br>15% of an amount<br>is 36                  | f)<br>35% of an amount<br>is 21                   |
| g)<br>A coat is reduced<br>by 15% to £68      | h)<br>A top is reduced by<br>6% to £47           | i)<br>A sofa is reduced by<br>17% to £1,162       |
| j)<br>John gets a raise of<br>10% to £7.48/hr | k)<br>A house depreciates<br>by 0.3% to £249,250 | l)<br>Population increases<br>by 0.04% to 718,262 |

# Notes P41

# Practice makes permanent!



## Worded Questions.

- 1). A camera is reduced by 5% in a sale. The sale price is £15.20. What was the original price?
- 2). An antique clock's price increases by 40% in a year. It now costs £112. What was it worth ?
- 3). Jean puts some money into shares. After a year the share price has increased by 16%. It is now worth £139.20. How much was originally spent on shares ?
- 4). Ian buys a second-hand car. The price falls by 24%. He sells it for £2356. How much did he pay for it ?
- 5). A season ticket for Bolton F.C. this season is to go up by 20%. It will cost £288. How much was a season ticket last season ?
- 6). A shirt is slightly shop soiled so it is reduced by 25%. It is now £12, how much was it to be sold for ?
- 7). The bill for a meal came to the cost of the meal plus 15% service charge. The total cost was £80.50. What was just the cost of the meal ?
- 8). In Durry's winter sale the following items were offered at 35% reductions. Here is the sale price, find the original price.
  - a). Stereo £130
  - b). Television £351
  - c). Video recorder £97.50
  - d). Walkman £9.10
  - e). Camcorder £520
  - f). Blender £5.85.
- 9). A salesperson is offered a rise of 12%. She will now earn £268.80 weekly.



# Answers

## Page 6. Worded Questions.

- 1). £16   2). £80   3). £120   4). £3100   5). £240   6). £16   7). £70  
8). a). £200   b). £540   c). £150   d). £14   e). £800   f). £9   9). £240  
10). 64Kg   11). 700   12). 85000   13). 2100   14). £80000   15). 22000  
16). 32   17). 62Kg   18). 42m

# Recap Lesson

SMART Notebook