

Higher : Addition Formulae

Revision

$(a) (i) \frac{4\sqrt{7}}{11} \quad (ii) \frac{3}{11}$	$(b) \frac{34}{11\sqrt{11}}$
$x = 0.848, 2.29$	
$\cos p = \frac{4}{\sqrt{17}}, \cos q = \frac{4}{5}$ $\sin p = \frac{1}{\sqrt{17}}, \sin q = \frac{3}{5}$	
$(a) \frac{4}{5} \quad (b) \frac{3}{\sqrt{10}}$	
$\sin x = \frac{3}{4}$ and $x = 0.848, 2.29$ $\sin x = -1$, and $x = \frac{3\pi}{2}$	
$x = \frac{\pi}{4}, \frac{\pi}{2}$ $x = \frac{5\pi}{4}, \frac{3\pi}{2}$	
<hr/> $(a) x = 0, 60, 300$ $(b) x = 0, 30, 150, 180, 210, 330$	
$\cos x = -\frac{3}{4}$ and $\cos x = 2$ $2.419, 3.864$ and no solution	

	2010 P1 Q23	(a) (ii) $\sin a = \frac{3}{\sqrt{13}}$ (b) $\sin b = \frac{3}{5}$ $\cos b = \frac{4}{5}$ (c) $\sin(a - b) = \frac{6}{5\sqrt{13}}$ $\sin(b - a) = -\frac{6}{5\sqrt{13}}$
	2009 Q24	$\frac{\sqrt{3} + 1}{2\sqrt{2}} \quad \text{or equivalent}$ <p style="margin-left: 100px;"> ^(a) ^(b) Proof </p> $ \begin{array}{l} \frac{\sqrt{6}}{2} \\ \text{accept } \sqrt{\frac{3}{2}} \text{ or } \frac{\sqrt{3}}{\sqrt{2}} \end{array} $ <p style="margin-left: 100px;"> ^(c) </p>
	2008 P2	$90^\circ, 199.5^\circ, 340.5^\circ$
	2007 P1Q6	$x = 90, 270$
	2007 P2 Q2	<p>(a) $\sqrt{\frac{1}{2}}$</p> <p>(b) (i) $\frac{4}{5}$</p>
	2006 P1 Q7	$x = 0, 180, 360, -60, 300$
	2006 P2 Q8	<p>(a) (i) $\sin a^\circ = \frac{1}{\sqrt{5}}$</p> <p>(ii) $\sin 2a^\circ = \frac{4}{5}$</p> <p>(b) $\sin 3a^\circ = \frac{11}{5\sqrt{5}}$</p>
	2005 P1 Q9	$\cos(x) = \frac{4}{5}$ $\sin(x) = \frac{3}{5}$

2005 P2Q2		<p>(a) $\cos(p) = \frac{8}{17}$, $\sin(p) = \frac{15}{17}$</p> <p>$\cos(q) = \frac{8}{10}$, $\sin(q) = \frac{6}{10}$</p> <p>From $\sin(A+B) = \sin(A)\cos(B) + \cos(A)\sin(B)$</p> $\frac{15}{17} \times \frac{8}{10} + \frac{8}{17} \times \frac{6}{10} = \frac{84}{85}$ <p>(b) (i) $-\frac{13}{85}$</p> <p>(ii) $-\frac{84}{13}$</p>	
2005 P2 Q8		<p>$k\sin(2x) = \sin(x)$</p> <p>$k \times 2\sin(x) \cos(x)$</p> <p>$\sin(x) \times (2k\cos(x) - 1) = 0$</p> <p>$\sin(x) = 0$ and $\cos(x) = \frac{1}{2k}$</p> <p>$\sin(x) = 0 \Rightarrow x = 0, \pi, 2\pi$ at (O), B and D</p> <p>and $\cos(x) = \frac{1}{2k}$ at A and C</p>	
2004 P1		<p>$\cos \hat{D}\hat{E}A = -\frac{6}{10}$</p>	
2003 P1 Q10		<p>(a) (i) $\frac{4}{5}$</p> <p>(ii) $\frac{3}{5}$</p> <p>(b) $\frac{4}{3}$</p>	
2003 P2 Q10		1.23 radians only	
2002W P2		$\frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$	

2002 PI Q3	<p>(a) (i) $\sin(2x^\circ)$ (ii) $2 \sin(x^\circ)$</p> <p>(b) $4\sin(x^\circ)\cos(x^\circ) - 2\sin(x^\circ) = 0$ $2\sin(x^\circ)(2\cos(x^\circ) - 1) = 0$ $\sin(x^\circ) = 0, \cos(x^\circ) =$ $0^\circ, 60^\circ, 180^\circ, 300^\circ, 360^\circ$</p>	
2002 PI Q5	<ul style="list-style-type: none"> $AC = \sqrt{2}$ and $BC = \sqrt{10}$ $\sin(a+b) = \sin a \cos b + \cos a \sin b$ $= \frac{1}{\sqrt{2}} \cdot \frac{3}{\sqrt{10}} + \frac{1}{\sqrt{2}} \cdot \frac{1}{\sqrt{10}}$ $= \frac{4}{\sqrt{20}} = \frac{4}{\sqrt{4 \times 5}} = \frac{2}{\sqrt{5}}$ 	4
2001 PI Q5	<p>(a) $30, 90, 150$</p> <p>(b) $\left(150, -\frac{\sqrt{3}}{2}\right)$</p>	
2001 PI Q7	<p>(a) (i) $\sin\left(x + \frac{\pi}{4}\right)$; (ii) $\cos\left(x + \frac{\pi}{4}\right)$</p> <p>(b) (i) $\sin x \cos \frac{\pi}{4} + \cos x \sin \frac{\pi}{4}$ (ii) $x = \frac{\pi}{4}, \frac{3\pi}{4}$</p>	
2000 PI Q1	$\frac{63}{65}$	
Spec 2 PI Q7	$\cos x = \frac{2}{\sqrt{11}}$ $\cos 2x = 2 \times \left(\frac{2}{\sqrt{11}}\right)^2 - 1 = -\frac{3}{11}$	
Spec 1 PI Q4	$\sin x^\circ \cos 30^\circ + \cos x^\circ \sin 30^\circ$ $= \frac{4}{5} \times \frac{\sqrt{3}}{2} + \frac{3}{5} \times \frac{1}{2}$ $= \frac{4\sqrt{3} + 3}{10}$	

Spec 1 P2 Q7	$ \begin{aligned} (a) \quad & 2(1 - 2\sin^2 x^\circ) - \cos^2 x^\circ \\ & = 2 - 4\sin^2 x^\circ - \cos^2 x^\circ \\ & = 2 - 4\sin^2 x^\circ - (1 - \sin^2 x^\circ) \\ & = 1 - 3\sin^2 x^\circ \end{aligned} $ $ \begin{aligned} (b) \quad & (\text{i}) \quad 3\sin^2 x^\circ + 2\sin x^\circ - 1 \\ & (\text{ii}) \quad 19.5 \end{aligned} $	
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