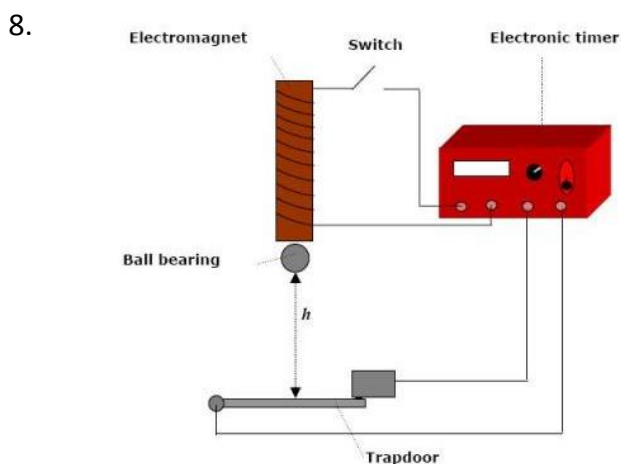


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**Projectiles**

1. A stone is dropped down a deep well and strikes the water 3.0 s later.
  - (a) How deep is the well?
  - (b) At what speed does the stone enter the water?
2. A teacher throws his pay cheque, wrapped around a stone, from the Kingston Bridge. If the initial velocity of the stone is  $15 \text{ ms}^{-1}$  and it takes 2.5 s to reach the water, what is the height of the bridge?
3. A stone dropped from the top of a cliff reaches the sea travelling at  $25 \text{ ms}^{-1}$ . What is the height of the cliff?
4. A stone, thrown vertically downwards from the top of another cliff at  $5 \text{ ms}^{-1}$ , reaches the sea travelling at  $35 \text{ ms}^{-1}$ .
  - (a) What is the height of the cliff?
  - (b) What is the time of flight?
5. Yet another stone is thrown vertically down a well at  $5 \text{ ms}^{-1}$ .
  - (a) Calculate the speed of the stone as it reaches the water surface 60 m below.
  - (b) How long does it take for the stone to reach the water?
6. An arrow is fired vertically upwards at  $40 \text{ ms}^{-1}$ .
  - (a) How long does it take to reach its maximum height?
  - (b) What is the maximum height?
7. At what vertical speed should an arrow be fired in order to reach a height of 180 m?



In an experiment to find the acceleration due to gravity (see the apparatus opposite) a steel ball falls from rest through 40 cm.

The time taken is 0.29 s.

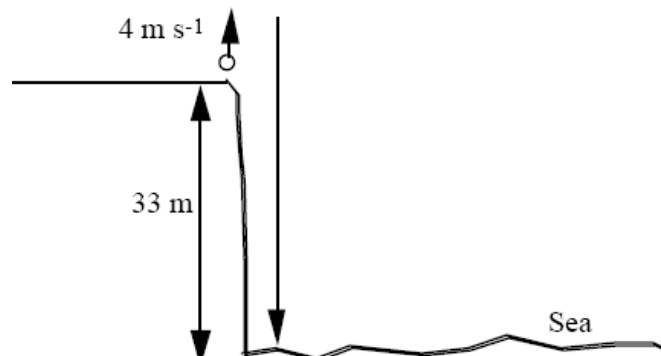
What is the value for the acceleration due to gravity?

9. A marble is thrown vertically upwards at  $20 \text{ ms}^{-1}$  from the edge of a 105 m high cliff and eventually lands in the sea at the foot of the cliff.
  - (a) What is the speed of the marble when it lands in the sea?
  - (b) How long does the marble take to reach the cliff foot?
  - (c) What is the maximum height above the sea reached by the marble?

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10. A ball is thrown upwards from the side of a cliff as shown below.



- (a) Calculate:
- the height of the ball above sea level after 2 s
  - the ball's velocity after 2 s.
- (b) What is the total distance travelled by the ball from launch to landing in the sea?
11. A helicopter is rising vertically at a steady speed of  $5.0 \text{ ms}^{-1}$  when James Bond drops from it. He reaches the ground 2.0 s later.
- What is his speed when he reaches the ground?
  - What is the height of the helicopter when he jumps?
  - What is his maximum height above the ground?

12. A Darth Vader hot air balloon rises vertically at a steady speed. When it is 80 m above the ground, an object is released. If the object hits the ground 5 s later, calculate the rising speed of the balloon.

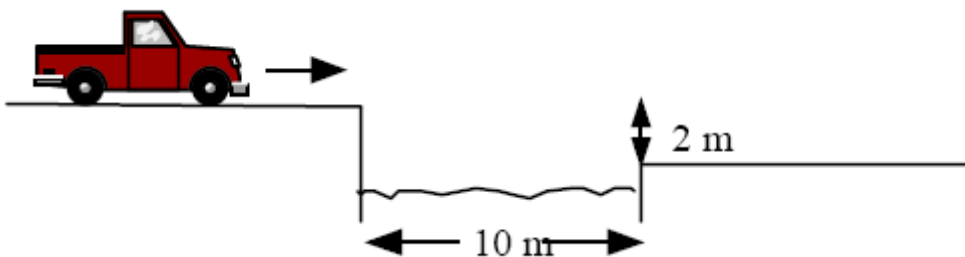


13. A stone is thrown horizontally from the top of a cliff at  $40 \text{ ms}^{-1}$  and lands in the sea 3.0 s later.
- How far from the foot of the cliff does it land?
  - What is the height of the cliff?
14. A projectile is fired horizontally from the edge of a cliff at  $12 \text{ ms}^{-1}$  and hits the sea 60 m away.  
Find : (a) the time of flight  
(b) the height of the starting point above sea level.
15. A car drives over the edge of a 125 m high cliff and lands in the sea 75 m from the cliff foot.
- How long does the car take to land?
  - How fast is the car travelling when it goes over the edge?

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16. In **question 15**, at the instant the car hits the sea, what is
- the horizontal component of the cars velocity
  - the vertical velocity
  - the resultant velocity of the car (magnitude and direction)?
17. A box is released from a plane travelling with a horizontal velocity of  $300 \text{ ms}^{-1}$  and a height of 300 m, find :
- how long it takes the box to hit the ground
  - the horizontal distance between the point of impact and the release point
  - the position of the plane relative to the box at the time of impact.
18. A rifle is aimed directly at a target which is a horizontal distance of 120 m away.
- Explain why the bullet does not the strike the target (you may use a sketch).
  - If the bullet velocity is  $240 \text{ ms}^{-1}$ , by what vertical distance does it miss the target?
19. A ball is projected horizontally at  $15 \text{ ms}^{-1}$  from the top of a vertical cliff. It reaches the ground 45 m from the foot of the cliff.
- Draw graphs, giving appropriate numerical values of the balls
    - horizontal speed against time
    - vertical speed against time, for the period between projection until it hits the ground.
  - Use a vector diagram, to find the resultant velocity (magnitude and direction) of the ball 2 s after its projection.
20. A stunt driver hopes to jump across a canal of width 10 m.  
The drop to the other side is 2 m as shown.

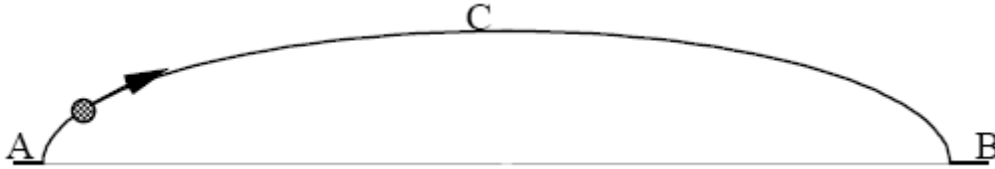


- Calculate the horizontal speed required to make it to the other side
- State any assumptions you have made.

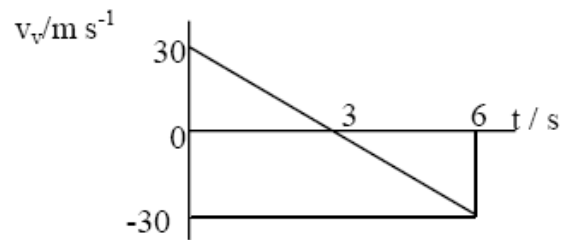
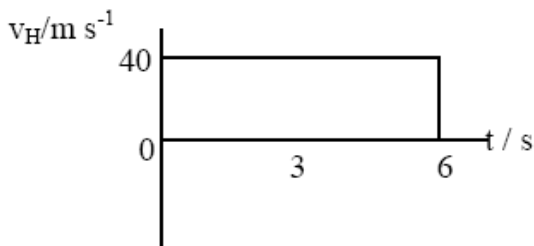
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21. A projectile is fired across level ground taking 6 s to travel from A to B. The highest point reached is C. Air resistance is negligible.



Velocity - time graphs for the flight are shown below.



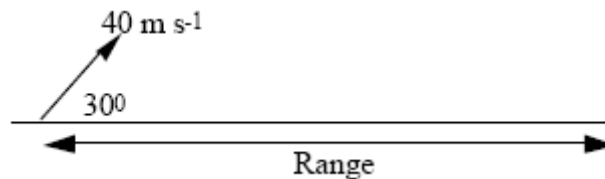
- (a) Describe:
- i) the horizontal motion of the projectile
  - ii) the vertical motion of the projectile?
- (b) Use a vector diagram, to find the velocity (including the angle) at which the projectile was fired from point A.
- (c) Find the velocity at position C. Explain why this is the smallest velocity of the projectile.
- (d) Calculate the height of the projectile at point C.
- (e) Find the range AB.
22. A cannon fires a shell at a target which is a horizontal distance of 7.2 km away. The shell emerges from the muzzle with a horizontal velocity of  $120 \text{ ms}^{-1}$  and an unknown vertical velocity.
- (a) How long does the shell take to reach the target?
  - (b) What is the initial vertical velocity of the shell?
23. A projectile has an initial horizontal velocity of  $60 \text{ ms}^{-1}$  and an initial vertical velocity of  $80 \text{ ms}^{-1}$ .
- (a) What is the time of flight of the projectile?
  - (b) What is the horizontal distance travelled?
  - (c) What is the maximum height reached?
24. A shell is fired with initial horizontal and vertical components of  $100 \text{ ms}^{-1}$  and  $40 \text{ ms}^{-1}$  respectively. At a distance of 600 m from the cannon is a building which is 55 m high. Does the shell clear the building and, if so, by how much?
25. A shell emerges from the muzzle of a gun at a velocity of  $240 \text{ ms}^{-1}$  and at an angle of  $30^\circ$  above the horizontal. What are the initial horizontal and vertical components of the velocity?

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26. A projectile is launched with an initial velocity of  $100 \text{ ms}^{-1}$  at an angle of  $30^\circ$  above the horizontal. Find
- the initial horizontal and vertical components of the velocity
  - the time of flight
  - the horizontal range.

27. An object of mass 5 kg is propelled with a speed of  $40 \text{ ms}^{-1}$  at an angle of  $30^\circ$  to the horizontal.



Find:

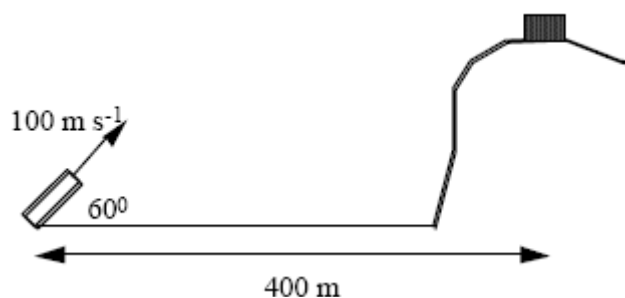
- the initial horizontal and vertical components of the velocity
  - the maximum height reached
  - the time of flight for the whole trajectory
  - the horizontal range of the object.
28. A bullet leaves the barrel of a gun travelling at  $240 \text{ ms}^{-1}$ . What is the range of the bullet if the angle of elevation of the gun is
- $45^\circ$
  - $60^\circ$

29. A projectile is launched with an initial velocity of  $130 \text{ ms}^{-1}$  and reaches a maximum height of 125 m.

Find :

- the initial vertical component of the velocity
- the initial horizontal component of the velocity
- the angle of projection
- the range.

30. A missile is launched at  $60^\circ$  to the ground and strikes a target on a hill as shown below.



If the initial speed of the missile was  $100 \text{ ms}^{-1}$  find:

- the time taken to reach the target
- the height of the target above the launcher.

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31. Explain why a satellite that is travelling at a constant speed is accelerating.

**Gravity and Mass**

32. State the inverse square law of gravitation.

33. Show that the force of attraction between two large ships, each of mass  $5.00 \times 10^7$  kg and separated by a distance of 20 m, is 417 N.

34. Calculate the gravitational force between two cars parked 0.50 m apart. The mass of each car is 1000 kg.

35. In a hydrogen atom an electron orbits a proton in a circle with a radius of  $5.30 \times 10^{-11}$  m. The mass of an electron is  $9.11 \times 10^{-31}$  kg and the mass of a proton is  $1.67 \times 10^{-27}$  kg. Calculate the gravitational force of attraction between the proton and the electron in a hydrogen atom.

36. The distance between the Earth and the Sun is  $1.50 \times 10^{11}$  m. The mass of the Earth is  $5.98 \times 10^{24}$  kg and the mass of the Sun is  $1.99 \times 10^{30}$  kg. Calculate the gravitational force between the Earth and the Sun.

37. Two protons exert a gravitational force of  $1.16 \times 10^{-35}$  N on each other. The mass of a proton is  $1.67 \times 10^{-27}$  kg. Calculate the distance separating the protons.