S3 National 4 Block Test 3 Revision Booklet



Contents

Algebra Substitution Statistics Averages The Circle (No Solutions) Symmetry Patterns Surface Area (No Solutions)

Algebra



Breaking Brackets

- 1. Multiply out each bracket :-
 - 3(x+4)b 7(y-3)a 5(2k+5) $11(6\gamma - 7)$ α. d y(y+2)
 f k(k-3) a u(3u+4) 3r(3r - 4)h i k -5(j-2) -3(q+5) j -4(2t+6) I -2(3f - 8) m - y(y+7) = n - h(h-3) = o - 2w(2w+1)p = -5k(3 - 4k).
- Write down the area and perimeter of this rectangle :-
 - using brackets
 - b without brackets.

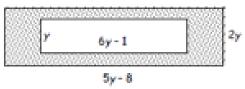




Exercise 3

Breaking Brackets and Simplifying

- 1. Multiply out the brackets and simplify fully where necessary :
 - a 5(k+2)+3b 8(2y+4)-12c 7(3e-2)+11d 8+2(t+3)e 11-3(3+w)f 15-(g+15)g 3(w-1)+2(w+1)h 4(2y-3)+5(4y+3)i 2(4r+3)-6j 3w-(w+4)+2(2-w)k 4(3y+4)-2(5y-1)-18l 3p+2(4p-6)-(9p+12)m 5(3-2m)+3(2m-6)-4(1-8m)+2m+7.
- Calculate the shaded area of the rectangle shown, in terms of y.



Algebra

Exercise 1

Solving Equations



- 1. Copy each equation and solve to find the value of x :-
 - a
 x+6=11
 b
 x+1=23
 c
 x+7=6

 d
 x+14=14
 c
 x-7=8
 f
 x-3=2

 g
 13+x=17
 h
 9+x=7
 i
 17-x=-17.
- 2. Copy each equation and solve to find the value of the letter :-

۵	4x = 12	ь	5p = 35	c	6k= 24
d	3h = 33	c	4 <i>g</i> = 56	f	7 <i>n</i> = 0
9	4 <i>m</i> = 144	h	6c = 9	i	8d = 1.

3. Find the value of x in the following equations (Set down ALL your working).

٩	2 <i>x</i> + 6 = 14	ь	5x + 4 = 29	c	4x + 7 = 39
d	3 <i>x</i> + 1 = 31	c	4 <i>x</i> - 8 = 16	f	7x - 11 = 3
9	10x - 9 = 41	h	3x - 6 = 0	i	11x - 7 = 37
j	6 <i>x</i> - 3 = 12	k	8 <i>x</i> + 12 = 15	1 I.	9x + 1 = 43.

E	xercise 2 Harder E	quations	
1.	Copy and complete :- a	8x+1 = 6x+17 b	7x - 3 = x + 15
	*(You may have been shown a different method)	$\Rightarrow 2x + 1 =$ $\Rightarrow 2x =$ $\Rightarrow x =$	=> 7x = => 7x = => x =
2.	Solve these equations :-		
	a 5x+4=2x+19	b $3x + 7 = x + 11$	c 8x+6=7x+22

-

3. These equations are a little "different". Solve :-

d 4x - 5 = x + 16

a	5x = 4x + 3	ь	3x = x + 44	c	7x = 4x + 42
d	12x = 8x + 1	c	15x = 3x + 18	f	6x - 2 = 8x.

11x - 1 = 2x + 17

 Joe bought 5 bags of marbles. Harry bought 3 bags, but he already had 20 loose marbles. They then had exactly the same number of marbles.

C



f 6x - 4 = 4x + 23.

- Make up an equation to show this information.
- b Solve the equation to determine how many marbles there are in a bag.

Solutions

Exercise 2 - Breaking Brackets

1.	a	3x + 12	Ь	7y - 21
	c	10k + 25	d	66y - 77
	e	y2 + 2y	f	k2 - 3k
	9	3u2 + 12u	h	9r2 - 12r
	i	-39 - 15	j	-8+-24
	k	-5j + 10	1	-6f + 16
	m	-y2 - 7y	n	$-h^{2} + 3h$
	0	-4w2 - 2w	P	$-15k + 20k^2$

2. a = 2x(3x+4) $b = 6x^2 + 8x$

Exercise 3 - Breaking Brackets & Simplifying 1. a 5k+13 b 16y+20 c 21e-3d 2t+14 e 2-3w f -gg 5w-1 h 28y+3 i 8rj 0 k 2yl 2p-24 m 30m2. $A = 2y(5y-8) - y(6y-1) = 10y^2 - 16y - 6y^2 + y$ $A = 4y^2 - 15y$

Solutions

d 7

4. a 5x = 3x + 20

3. a 3

Ch 5 Ex 1 Solving Equations ¢ L a 5 b 22 c -1 f 5 e 15 d 0 ŝ h -2 i 34 9 4 c 4 ь 7 2 a 3 f O c 14 d 11 $h^{3}/_{2}$ i 1/8 g 36 b 5 3. a 4 c 8 f 2 6.5 OID i 4 g 5 h 2 $j \frac{16}{6} = 2.5 \text{ k} \frac{3}{8}$ 1 42/g = 14/3 = 4 2/3 Ch 5 Ex 2 Harder Equations 1 a 8 b 3 2 a 5 b 2 16

c 2

b 22

d 1/4 c 18/12 = 1.5 f -1

f 27/2

c 14

b 10

Substitution

Exercise 6

Evaluating Expressions and Formulae

- 1. Given a = 2, find :
 - a a+6b 2ac 5a-3d $(7a+4)\div 2$ e 4(a+2)f 6(11-a)-53g 3(a+1)-12h 5(a+2)+15i 3(a-11)+27

2. Given b = 3, c = 5 and d = -1, evaluate : a b + c + d
 b 2b - c - 3d
 c ¹/₂(bc + d)
 d 3bcd
 e cdb - dbc
 f 0.5(bd - cd).

3. a If f = 2, g = 4 and h = -2, find e, given f + g + h + e = 10.
b If p = 3, r = -3 and s = 2, find t given st - prs = 12.

4. If m = 4 and n = 6, find the values of :**a** m^2 **b** n^2 **c** \sqrt{m} **d** $m^2 + n^2$ **e** $2m^2$ **f** $3mn^2$ **g** $\sqrt{mn+1}$ **h** $\sqrt{5m-2n+1}$ **i** $\sqrt{m^2 + n^2 - 3}$.

Substitution

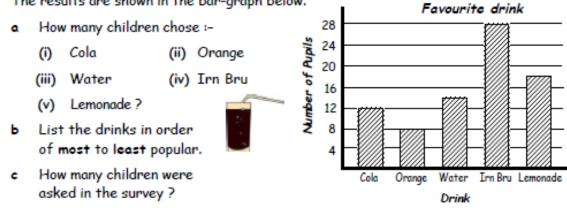
Ex	erc	ise 6 -	- Eva	luating	Exp	ressions	and	Formulae
1.	۵	8	b	4	с	7		
	d	9	e	16	f	1		
	9	-3	h	35	i	0		
2.	۵	7	b	4	С	7		
	d	-45	e	0	f	1		
3.	۵	6	b	-3				
4.	۵	16	b	36	с	2		
	d	52	e	32	f	432		
	9	5	h	3	i	7		

Exercise 1

Bar Graphs & Line Graphs



 A group of children were asked to name their favourite drink. The results are shown in the bar-graph below.



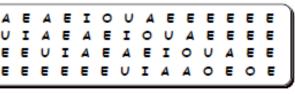
2. A primary 5 class were asked about the towns they had visited.

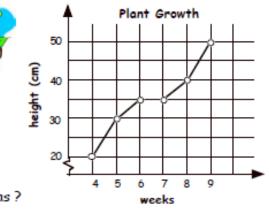
London	Inverness	Carlisle	Newcastle	Leeds	Liverpool	
6	8	3	7	1	5	



Draw and label a neat bar graph to show this information.

- Pupils in the Primary 7 classes were asked to name the most commonly used vowel. The table shows their list of answers.
 - Make a frequency table and use tally marks to complete it.
 - Draw and label a neat bar graph from your frequency table.
- The line graph shows the height of a plant over a period of time.
 - How tall was the plant after :-
 - (i) 4 weeks (ii) 5 weeks
 - (iii) 9 weeks (iv) 7 weeks?
 - b On which week was the plant :-
 - (i) 35 cm (ii) 40 cm tall ?
 - c One week the plant was not given any water. Which week do you think it was?
 - Estimate the height of the plant at 8¹/₂ weeks.



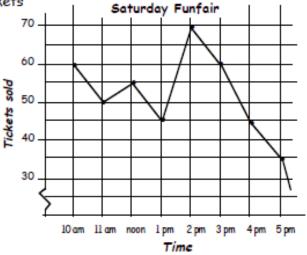


- The line graph shows the number of tickets sold each hour at a Saturday Funfair.
 - a How many tickets were sold :-
 - (i) at 10 am (ii) at 11 am
 - (iii) at 12 noon (iv) at 5 pm?
 - b What was the main peak time (most tickets sold)?
 - Between which two times was there the biggest increase in ticket sales ?
 - d Why do you think the ticket sales dropped after two o'clock ?
- Another plant's height was recorded over a period of time.

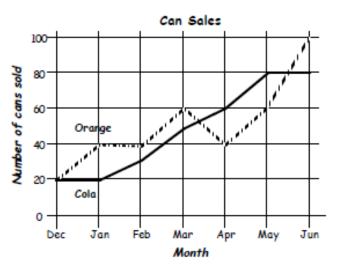
Use the information from the table shown to draw a line graph.

- The comparative line graph shows the sales of Orange and Cola from the tuck shop.
 - Which drink sold better in :-
 - (i) January (ii) March
 - (iii) April (iv) June?
 - b How many cans of Cola were sold in :-
 - (i) January (ii) June?
 - How many cans of Orange were sold in total ?
- This table shows 6 months of car sales from two different car dealers, Arnold Clunk and Reg Barney.

Construct a comparative line graph to show this information.



Week 4 - 25 cm	Week 5 - 30 cm
Week 6 - 35 cm	Week 7 - 40 cm
Week 8 - 50 cm	Week 9 - 65 cm



	Jul	Aug	Sep	Oct	Nov	Dec
Clunk's	100	250	300	250	400	200
Barney's	300	200	350	450	100	150

Exercise 6

Mean and Range



The range (= highest - lowest).

For each set of data, find the RANGE of numbers :-

- a 7, 9, 8, 12, 6, 15, 8, 7, 10, 10, 12, 5, 9, 11
- b 73, 57, 44, 11, 33, 8, 26, 1, 4, 2, 74, 16, 15, 7.
- 2. Find the mean of :
 - a 8, 10, 12, 14 b 14, 50, 23, 41, 62, 50
 - c £2, £5, £8, £26, £20, £11. d 9.1 cm, 10.3 cm, 7.6 cm, 4.1 cm, 3.9 cm.
- 3. Ten boxes of matches have their contents counted.

It is found that they contain the following number :-

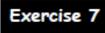
60, 62, 64, 62, 65, 61, 63, 60, 64, 64.

- Work out the range.
- b Calculate the mean number of matches.
- The Match Company claim that each of their boxes should contain an average of 63 matches.

Is the company's claim correct? (Explain)



4. Tom sat two mental tests (each out of 10). His mean score for the tests was 6. If Tom scored 9 in the first test, what must he have scored in the second ?



Median & Mode



1. Find the mode for each set of data :-

۵	1, 1, 2, 3, 5, 8, 13, 21, 34, 55	ь	3, 2, 1, 8, 4, 5, 9, 2, 7, 6, 0
c	1.7, 2.3, 1.6, 3, 2.3, 3.7, 2.9	d	A, C, F, G, H, Y,T, E, D, D, G, H, G.

 For each set of data, find the MEDIAN :-(Make sure you put the numbers in order first)

a 5, 6, 6, 7, 8, 9, 9, 10, 11 b 16, 18, 18, 20, 24, 26, 28, 32 c 17, 9, 3, 9, 9, 5, 7, 13, 11, 15, 15, 9, 9, 7, 1, 1, 17, 15, 13, 13, 7.

- 3. Find the mean, median, mode and range of each set of data :
 - a 10, 12, 14, 15, 16, 19, 22, 23, 23 b
 - c 4, 1, 14, 12, 6, 7, 11, 13, 9, 1



46, 31, 66, 73, 83, 43, 16, 66

d All the prime numbers between 30 and 50.

The mean weight of 4 boxes is 75 kg. Three of the boxes each weigh 85 kg. What is the weight of the fourth box ?

Exercise 8

Stem & Leaf Diagrams

- The stem and leaf diagram shows the ages of people in a post office queue.
 - Write a key for the diagram.
 - b Write down all the ages.
 - c How old was the youngest person?
 - d What was the modal age ?
 - Find the median.

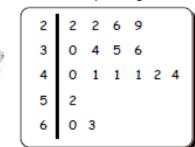
2. For each set of data shown :-

- (i) Construct an ordered stem and leaf diagram. (ii) Find the mode and median.
- Ages of mature students at a University.

ſ	23	42	27	37	25	60	29	35	26	45	35	26
	50	39	27	26	42	47	26	59	42	23	29	29
	20	51	43	44	28	46	42	27	52	30	30	42

Distances (in metres) jumped from a standing position.

1.33 1.20 1.12 1.23 1.10 1.36 1.53 1.08	
	1.53
1·62 1·23 1·41 1·15 0·97 1·31 1·23 1·26 1·33 1·29 1·12 1·23 1·19 1·36 1·53 1·08 0·9 1·2 1·51 1·03 1·66 1·53 1·44 1·23	1.39



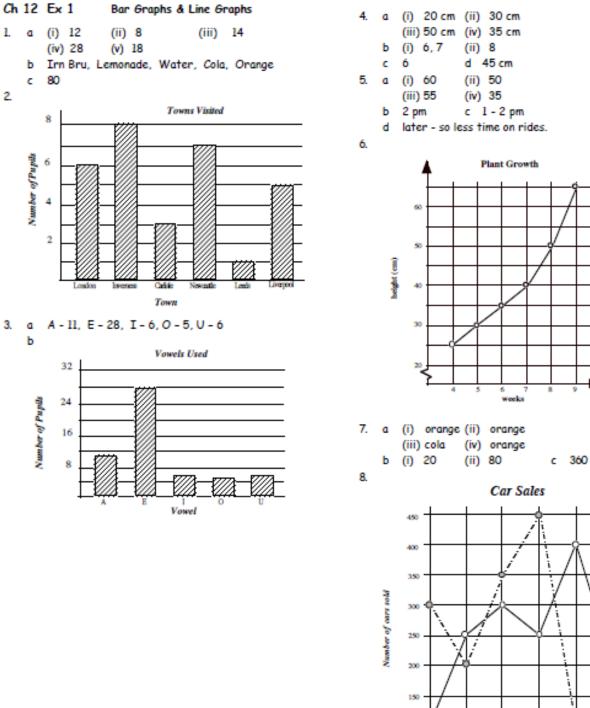
Peoples' Ages

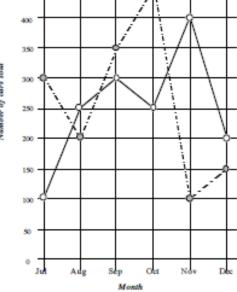


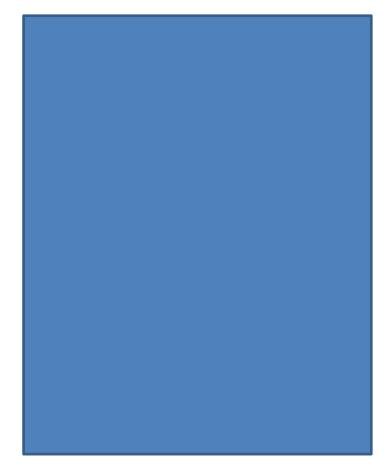
 a Draw an ordered back to back stem and leaf diagram showing the details about how far (in centimetres) S1 and S2 pupils could jump from a standing position.

S1	148	156	172	181	160	157	164	132	184	146	157	139
S 2	182	174	138	145	175	162	159	175	167	173	144	150

- b Find the modal and median heights of :- (i) S1 (ii) S2.
- c Write a few sentences comparing the mode and the median of both groups.







Ch 12 Ex 6 Mean & Range b 73 1. a 10 2. a 11 b 40 c £12 d 7 cm b 62-5 3. a 5 c No-62-5<63 4. 3 Ch 12 Ex 7 Median & Mode b 2 1. a 1 c 2-3 d 6 2. a 8 b 22 c 9 3. a mean - 17·1 median - 16 mode - 23 b mean - 53 median - 56 mode - 66 c mean - 7.8 median - 8 mode - 1 d 31, 37, 41, 43, 47 mean - 39.8 median - 41 mode - none 4. 45 kg Ch 12 Ex 8 Stem & Leaf Diagrams 1. a 314 means 34 years old b 22, 22, 26, 29, 30, 34, 35, 36, 40, 41, 41, 41, 42, 44, 52, 60, 63 e 40 c 22 d 41

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Ch 12 Ex 8
                  Stem & Leaf Diagrams
      314 means 34 years old
1
    α.
    b 22, 22, 26, 29, 30, 34, 35, 36, 40,
       41, 41, 41, 42, 44, 52, 60, 63
                   d 41
    c 22
                                  e 40
   2. a (i) with key
           2 033566667778999
           3
              005579
          4
             2222234567
          5
             0129
          6 0
          (ii) mode - 42, median - 35
       b (i) with key
             09 07
             10 38
             11 259
             12 03333369
             13 1369
             14 14
             15 0133
             16 26
          (ii) mode - 1.23, median - 1.26
   a with key
            92 113 8
                14
            68
                    4.6
           776 15 09
                16 2.7
            40
             2
                17
                    3466
            41
                18
                    2
       b (i) S1: mode - 157, median - 157
          (ii) S2 : mode - 175, median - 164.5
       c both averages are higher for S2
          (but they are older and probably taller)
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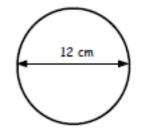
The Circle (No Solutions)

Exercise 1

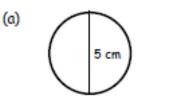
3.

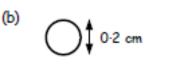


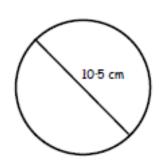
- 1. Calculate the circumference of this circle with diameter 12 cm. Copy and complete : - => $C = \pi D$
 - $c = \pi D$ $c = 3.14 \times 12$ c = 0.000 cm

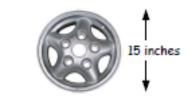


 Showing 3 lines of working for each case, calculate the circumference of each of these circles :-









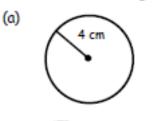
Calculate the circumference of the alloy wheel-trim shown opposite.

(c)

(c)

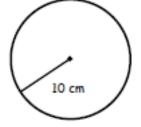
 Calculate the circumference of each of these circles, showing your 3 lines of working each time :-

(b)



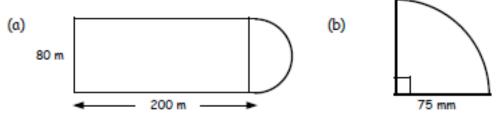
5.

0.9 cm



A semi-circular doorstep has a diameter of 1.5 metres. Calculate the perimeter of the doorstep.

6. Calculate the perimeter of both shapes :-



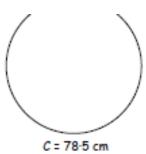
The Circle (No Solutions)

 Find the diameter of the circle with circumference 78.5 cm.
 Copy and complete :-

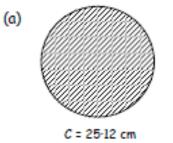
$$D = \frac{C}{\pi}$$

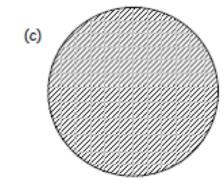
=> $D = \frac{786}{3.14}$
=> $D = \dots cm$

C = 1.57 cm



 Calculate the diameter of each circle below :-(You must set down 3 lines of working)





C = 59-66 cm

3. For a circle with circumference 69.08 cm, calculate its :-

(b)

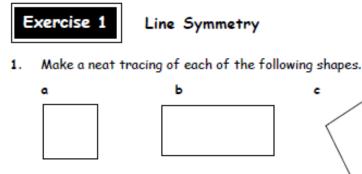
- (a) diameter(b) radius.
- The circumference of a tyre from a child's toy motorbike is 7.85 centimetres.

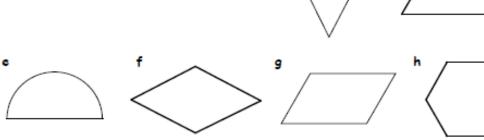
Find the radius of the tyre.

- This CD has an outer circumference of 40 centimetres. The hole has a 0.5 centimetre radius. Calculate :-
 - (a) the radius of the CD.
 - (b) the circumference of the hole.

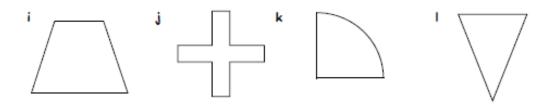


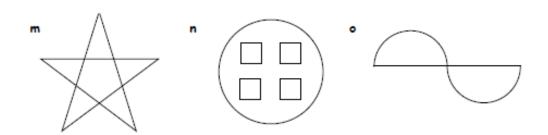
Symmetry



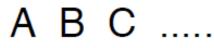


d



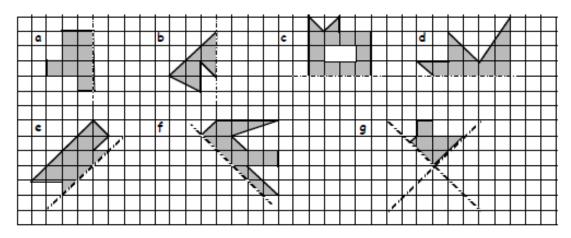


- 2. a For each shape you have traced (or copied) show all lines of symmetry.
 - **b** Write down next to each shape how many lines of symmetry it has.
- 3. Make a list of those capital letters of the alphabet that have lines of symmetry.



Symmetry

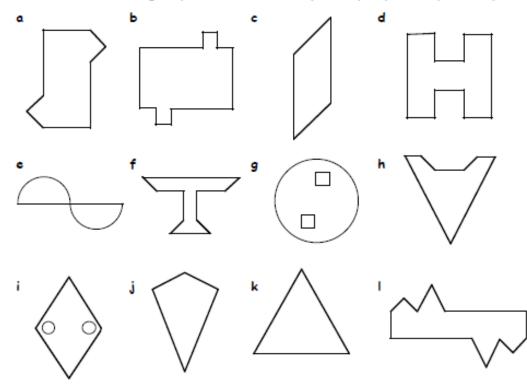
 Copy each of the following shapes neatly and complete each one such that the dotted line is a line of symmetry each time.



Exercise 2

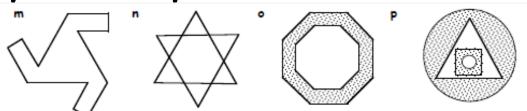
Rotational Symmetry

1. Which of the following shapes have half-turn symmetry? (Answer yes or no).

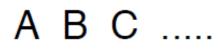


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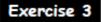
Symmetry



- For each shape in Question 1, state the order of symmetry. 2.
- Which seven capital letters of the alphabet have $\frac{1}{2}$ -turn symmetry? з. a



Of these seven letters, only three do not have a line of symmetry. ь Which three ?



Creating a Shape with Half-turn Symmetry

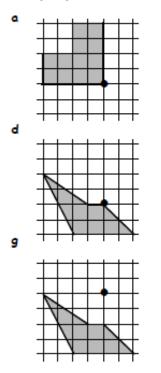
Make a copy of each of the following shapes. 1.

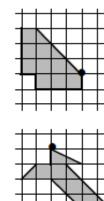
Create a shape which has half turn symmetry by rotating each shape by 180° about the dot.

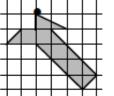
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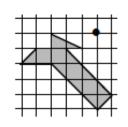
c

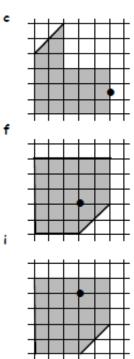
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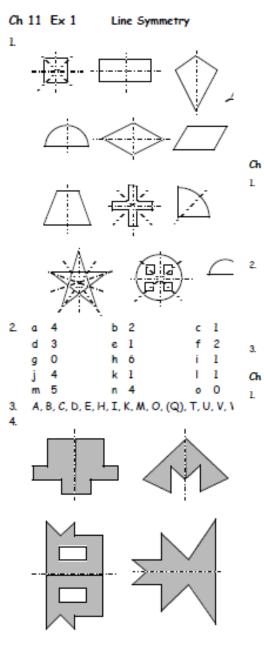


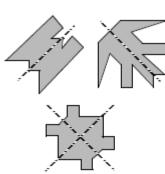




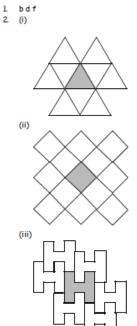


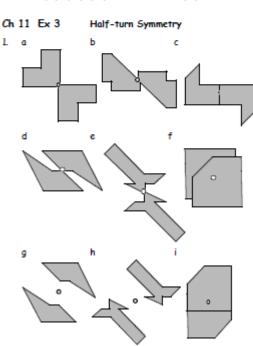






Ch	11	Ex 2	Ro	tational Sym	met	tr y
1.	۵	yes	b	yes	c	yes
	d	yes	е	yes	f	no
	9	yes	h	no	i.	yes
	j	no	k	no	Т.	yes
	m	no	n	yes	0	yes
	Ρ	no				
2.	۵	1/2, 2	b	1/2, 2	c	1/2, 2
	d	¹ / ₂ , 2	е	1/2, 2	f	
	9	1/2,2	h		i	1/2, 2
	j		k	1/3, 3	I.	1/2, 2
	m	1/3, 3	n	1/ ₆ ,6	0	1/8,8
3.	۵	H, I, N, O,	S,)	(,Z	b	N, S, Z





Patterns

V

5 10 15 _ _ _

E	xer	cise 1	Sequence	es å	Pat	terns		ĺ					
1.	Give	e a rule for	each of thes	e sequ	uence	es :-	(begin i	with '	star	•t at .	and	then	").
	a	2, 5, 8,	11, 14,	ь	7, 1	13, 19	, 25,			c 2	5, 20), 15, 1	l O ,
	d	98, 81, 6	4, 47,	e	3, 9	9, 27,	81,			f 1	, 6, 3	86, 216	j,
2.	. Write down the next two numbers in each sequence from question 1.												
3.	Fin	d the next	two numbers i	in eac	h seq	quence							
	a	7, 9, 11,	13,	ь	5, 9	9, 13,	17,	-		c 2	4, 22	, 20, .	
	d	70, 58, 4	46, 34,	e	1, 3	3, 9, .				f 2	. 4, 8	8, 16,	
4.			pattern for so ne first 12 squ	•			0	8	8		0000		0000
5.			numbers is de ne :- a			-			-				
	Exercise 2 Simple Linear Patterns												
1.			six window po			No. of	Doors (D)	1	2	3	4	6
	a		omplete the t	able.		No. of	Panes (/	າ	6	12	?	?	?
	ь	Copy and c the formu	omplete la :- P = ×	D			rises by	. —	- 6	\sim	\sim	$\overline{}$	
	c	How many	panes would t	here b	e in	11 doo	rs?						
	d	How many	doors are the	re if t	there	e are 7	'8 pane:	s ?					
2.	For	the tables	below :-	(i) co	omplet	e each	one	(ii)	cons	truct	a form	ula.
	a	No. of toy	rs and price				b No	of se	conc	ls and	l no, o	f minut	es
		T 1	2 3 4 5	6]			(1	2	3 4	4 5	6	
			18 27	_			s			180 .		_	
		L <u></u>	P = × T		1				5	=	× N	1	
	c	No. of per	ntagons and n	o. of v	ertic	ces	d No	o. of to	bles	to le	gs		
		P 1	2 3 4 5	6				τ 1	2	з -	4 6	6	

L 8 16 24

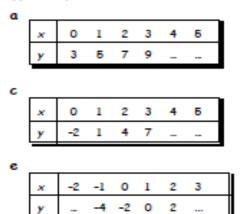
Patterns

Linear Graphs - For each of the tables below :-З. (i) complete each table (ii) construct a formula (iii) take each pair of numbers as coordinates (iv) plot on a coordinate graph (v) draw a line through the points and label the line with your formula. a ь 2 з 1 2 3 0 1 Б 0 4 Б × 3 9 2 4 6 0 6 0 y v Exercise 3 Harder Linear Patterns 1. Look at the pattern shown. 1 triangle 4 triangle 2 triangle 3 triangle perimeter 3 perimeter 4 perimeter 5 perimeter 6 Copy and complete a 1 2 4 No. of triangles (T) 3 5 the table shown. Perimeter (P) 3 4 5 ---_ 1

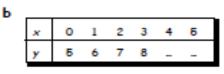
- Copy and complete the formula for the above pattern :-P = ... × T + ь
- Find the perimeter of the pattern with 21 triangles. С
- Find the number of triangles if the perimeter is 27. d

2 For each of the tables below :-

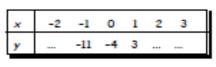
(ï) complete each table



(ii) construct a formula.



f



6

Ch 4 Ex	1	Sequences	ð,	Potterns
---------	---	-----------	----	----------

1. a start at 2 then add 3

- b start at 7 then add 6
- c start at 25 then subtract 5
- d start at 98 then subtract 17
- e start at 3 then times by 3
- f start at 1 then times by 6

2	٥	17,20	ь	31, 37	с	5,0		
	đ	30, 13	e	243,729	f	1296,7776		

3. a 15,17 b 21,25 c 18,16 e 27,81 f 32,64 d 22,10 4. 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144 5. a 11 x 12 b 1001 x 1002 c (n+1) x (n+2) Ch 4 Ex 2 Simple Linear Patterns 1. a 123456 6 12 18 24 30 36 b P=6D c 66 d 13 2. a 123456 9 18 27 36 45 54 P = 9Tb 1 2 3 4 5 6 60 120 180 240 300 360 S = 60M c 1 2 3 4 5 6 5 10 15 20 25 30 V = 5Pd 123456 8 16 24 32 40 48 L = 8T3. a 0123456 0 3 6 9 12 15 18 y = 3xcheck linear diagram b 0123456 y = 2x0 2 4 6 8 10 12 check linear diagram

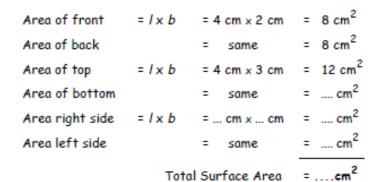
Ch 4 Ex 3 Harder Linear Patterns 1. a 123456 345678 b P=T+2 c 23 d 25 2. a 012345 3 5 7 9 11 13 y = 2x + 3b 012345 5678910 y = x + 5c 012345 -2 1 4 7 10 13 y = 3x - 2d 012345 -1 4 9 14 19 24 y = 5x - 1e -2 -1 0 1 2 3 -6-4-2024 y = 2x - 2f-2-10123 -18 -11 -4 3 10 17 y = 7x - 4

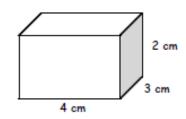
Surface Area- No Solutions





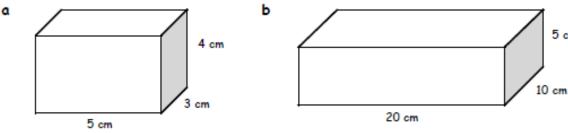
1. Copy and complete to find the total surface area of this cuboid.



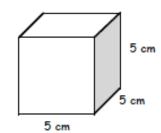


5 cm

Find the total surface area of these cuboids. (Show your working). 2.

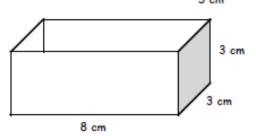


A cube has side 5 centimetres. Find the total surface area of the cube.



4. This carton has no lid.

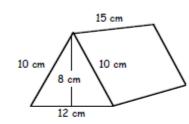
> Find the surface area of the outside of the carton.

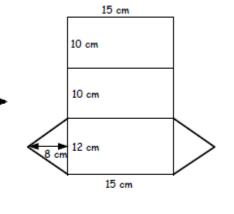


Surface Area- No Solutions



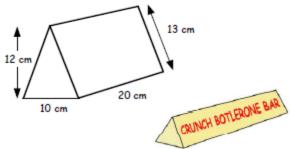
 Calculate the total surface area of the triangular prism. (Show all your working).





 A giant chocolate bar in the shape of a triangular prism is shown.

Find the area of cardboard wrapping required to cover the bar.



Surface Area- No Solutions

