Eastwood High School

Name:

Unit 2 Particles and Waves

Summary Notes

Introduction

Structure within the Atom

Quark
Size < 10^{-19} m

Nucleus
Size ≈ 10^{-14} m

Electron
Size < 10^{-18} m

Neutron and Proton
Size ≈ 10^{-15} m

Atom
Size ≈ 10^{-10} m

If the protons and neutrons in this picture were 10 cm across, then the quarks and electrons would be less than 0.1 mm in size and the entire atom would be about 10 km across.
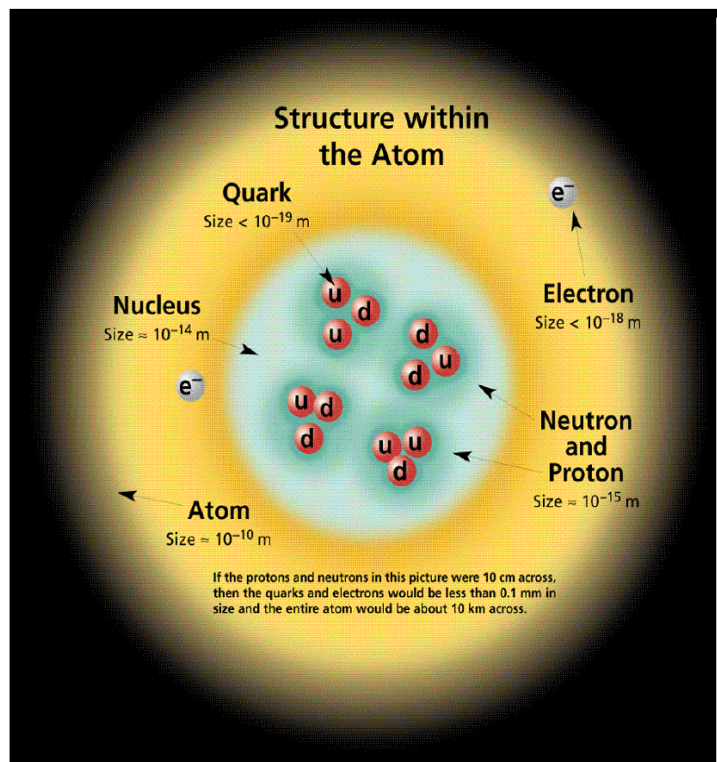
Today, we know that atoms do not represent the smallest unit of matter. In first year we learned that atoms are made up of a positively charged nucleus containing protons and neutrons with negatively charged electrons orbiting it. The standard model attempts to explain everything in the universe in terms of fundamental particles. **A fundamental particle is one which cannot be broken down into anything else.** These fundamental particles are the building blocks of matter, and the things which hold matter

Orders of Magnitude

Often, to help us grasp a sense of scale, newspapers compare things to everyday objects: heights are measured in double-decker buses, areas in football pitches etc. However, we do not experience the extremes of scale in everyday life so we use scientific notation to describe these. Powers of 10 are referred to as orders of magnitude, i.e. something a thousand times larger is three orders of magnitude bigger. It would be useful to get an idea of scale to better understand how sub-nuclear and astronomical dimensions compare with those in our everyday life. You can see how we fit into the grand scheme of things by carrying out the following activity.

When we get into the world of the very small or very large it is difficult to get a picture of scale in our minds. Below is a table giving some examples of scale in our world;

1 m	Human scale – the average British person is 1.69 m
10 m	The height of a house
100 m	The width of a city square
10^3 m	The length of an average street
10^4 m	The diameter of a small city like Perth
10^5 m	Approximate distance between Aberdeen and Dundee
10^6 m	Length of Great Britain
10^7 m	Diameter of Earth

Thinking in terms of the smaller end of the scale.

If a proton is measured as having a radius of distance roughly 10^{-15}m, how many of these protons would fit on the point of a pencil?

Assuming the pencil point was 1mm across, there would be 1 000 000 000 000 (10^{12}) protons.

In terms of the larger end of the scale, we have space and quasars.

The distance to a quasar is 10^{26} m.

This would take light, travelling at 3 x 10^8m/s, 10 000 000 000 (10^9) years to get from Earth to the quasar.

Example

How many orders of magnitude greater is a quasar compared to a proton?

$1\times10^{26}/1\times10^{-15} = 1\times10^{41}$

A quasar is 42 orders of magnitude greater than a proton.

The structure of atoms

At the start of modern physics at the beginning of the 20th century, atoms were treated as semi-solid spheres with charge spread throughout them. This was called the Thomson model after the physicist who discovered the electron. This model fitted in well with experiments that had been done by then, but a new experiment by Ernest Rutherford in 1909 would soon change this. This was the first scattering experiment – an experiment to probe the structure of objects smaller than we can actually see by firing something at them and seeing how they deflect or reflect.
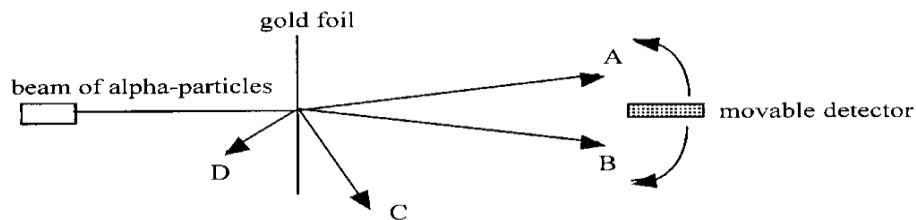
The Rutherford alpha scattering experiment

The main results of this experiment were: gold

- Most of the alpha particles passed straight through the foil, with little or no deflection, being detected between positions A and B.
- A few particles were deflected through large angles, e.g. to position C, and a very small number were even deflected backwards, e.g. to position D

Rutherford interpreted his results as follows:

- The fact that most of the particles passed straight through the foil, which was at least 100 atoms thick, suggested that the atom must be mostly empty space!
- In order to produce the large deflections at C and D, the positively charged alpha particles must be encountering something of very large mass and a positive charge


D Deflected right back   **C** Large deflection

Matter and antimatter

Almost everything we see in the universe appears to be made up of just ordinary protons, neutrons and electrons. However high-energy collisions revealed the existence of antimatter. **Antimatter consists of particles that are identical to their counterparts in every way apart from charge**, e.g. an antiproton has the same mass as a proton but a negative charge. It is believed that every particle of matter has a corresponding antiparticle.
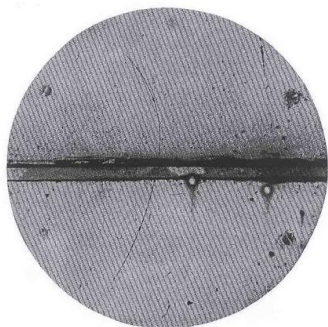
The experimental proof for the positron came in the form of tracks left in a cloud chamber. The rather faint photograph on the right shows the first positron ever identified. The tracks of positrons were identical to those made by electrons but curved in the opposite direction.

Annihilation

When a matter particle meets an anti-matter particle they **annihilate**, giving off energy. Often a pair of high energy photons (gamma rays) are produced but other particles can be created from the conversion of energy into mass (using $E = mc^2$). An application of this includes PET (Positron Emission Tomography) scanners work.

The particle zoo

The discovery of anti-matter was only the beginning. The particle zoo was created when particle accelerators discovered nearly 200 more particles. A new theory was needed to explain and try to simplify what was going on. This theory is called the **Standard Model.**

In a particle accelerator a very small particle, eg an electron, can be accelerated by electric and magnetic fields to a very high speed. Being very small, speeds near to the speed of light may be achieved. When **electrons collide with nucleons a substantial amount of energy is released** in a small space. Some of this energy may be converted into mass (**$E = mc^2$**), producing showers of nuclear particles. By passing these particles through a magnetic field and observing the deflection their mass and charge can be measured.

For example, an electron with low mass will be more easily deflected than its heavier cousin, the Muon. A positive particle will be deflected in the opposite direction to a negative particle. Cosmic rays from outer space also contain particles, which can be studied in a similar manner.

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Most matter particles, such as protons, electrons and neutrons have corresponding **antiparticles**. These have the same rest mass as the particles but the opposite charge. With the exception of the antiparticle of the electron (e⁻), which is the positron (e⁺), antiparticles are given the same symbol as the particle but with a bar over the top.

When a particle and its antiparticle meet, in most cases, they will annihilate each other and their mass is converted into energy. There are far more particles than antiparticles in the Universe, so annihilation is extremely rare.

At present physicists believe that there **are 12 fundamental mass particles** called **Fermions** which are split into two groups: **Leptons and Quarks**
There are also **4** force mediating particles called **Bosons**. The table below shows the fundamental particles [at the moment!]

		fermions		bosons	
quarks	u up(⅔)	c charm (⅔)	t top (⅔)	γ photon	force carriers
quarks	d down (- ⅓)	s strange (- ⅓)	b bottom (- ⅓)	g gluon	force carriers
leptons	ν_e electron neutrino (0)	ν_μ muon neutrino (0)	ν_τ tau neutrino (0)	Z Z boson	force carriers
leptons	e electron (-1)	μ muon (-1)	τ tau (-1)	W W boson	force carriers

Quarks

It was noted that protons and neutrons consisted of three smaller particles called '*quarks*'.There are two first generation quarks called *up* and *down*. These make up neutrons and protons. There are two 2nd generation quarks called *charm* and *strange*. Finally there are two 3rd generation quarks called *top* and *bottom*. Each quark has only a fraction (⅓ or ⅔) of the electron charge (1.6 × 10⁻¹⁹ C). These particles also have other properties, such as spin, colour, quantum number and even something called strangeness, which are not covered by this course.

Quarks were discovered during high-energy collisions between electrons and nucleons in particle accelerators.

Hadrons

Particles which are made up of quarks are called **hadrons** (the word hadron meant heavy particle). The Large Hadron Collider at CERN collides these particles. There are two different types of hadron, called **baryons** and **mesons** which depend on how many quarks make up the particle.

Baryons are made up of *3* quarks. Examples include the proton and the neutron.

The charge of the proton (and the neutral charge of the neutron) arise out of the fractional charges of their inner quarks. This is worked out as follows:

- A **proton** consists of **2 up quarks and a down quark**. Total charge=+1 ($\frac{2}{3} + \frac{2}{3} - \frac{1}{3}$ **= 1)**.
- A **neutron** is made up of **1 up quark and 2 down quarks**. No charge ($\frac{2}{3} - \frac{1}{3} - \frac{1}{3}$ **= 0)**.

Mesons are made up of **2** quarks. They always consist of a **quark and an anti-quark pair**.

An example of a meson is a negative pion ($\Pi^- = \bar{u}\,d$). It is made up of an anti-up quark and a down quark: This gives it a charge of $-\frac{2}{3} - \frac{1}{3}$ = -1.

Note: A bar above a quark represents an antiquark e.g. ū is the anti-up quark (this is **not** the same as the down quark.) The negative pion only has a lifetime of around 2.6 x 10⁻⁸ s

| baryons		mesons	
proton up, up ,down	**neutron** up, down, down	**pion** up & anti-down	**kaon⁰** down & anti-strange
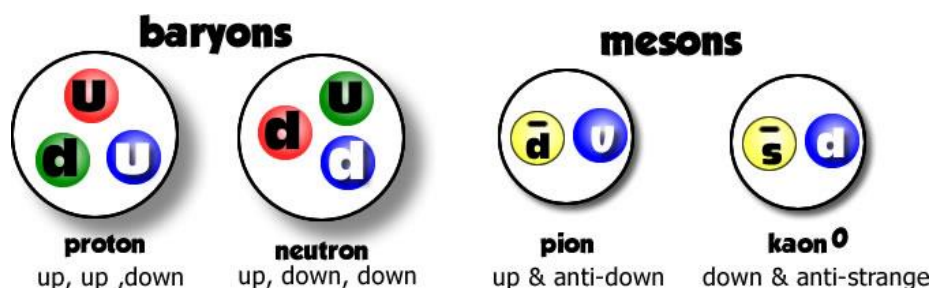
Forces and Bosons

In the nucleus of every element other than hydrogen there is more than one proton. The charge on each proton is positive, so why don't the protons fly apart, breaking up the nucleus?

There is a short range force that exists that holds particles of the same charge together. This force is stronger than the electrostatic repulsion that tries to force the particles apart. We call it *the strong force*.

This force acts over an extremely short range [approx 10^{-15} m], of the order of magnitude of a nucleus. Outside of this range the strong force has no effect whatsoever. If a proton was placed close to a nucleus it would be repelled and forced away.
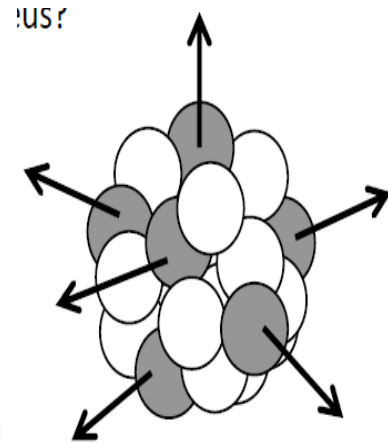
The particle responsible for carrying the strong force is called the **gluon**.

The *weak nuclear force* is involved in radioactive beta decay. It is called the weak nuclear force to distinguish it from the strong nuclear force, but it is not actually the weakest of all the fundamental forces. It is also an extremely short-range force. Its exchange particle are the **W- and Z- bosons**.

The *electromagnetic force* stops the electron from flying out of the atom. The theory of the electromagnetic force and electromagnetic waves was created by the Scottish Physicist James Clerk Maxwell in the 19th Century. Its exchange particle is the **photon**.

The final force is *gravity*. Although it is one of the most familiar forces to us it is also one of the least understood.

It may appear surprising that gravity is, in fact, the weakest of all the fundamental forces when we are so aware of its affect on us in everyday life. However, if the electromagnetic and strong nuclear forces were not so strong then all matter would easily be broken apart and our universe would not exist in the form it does today.
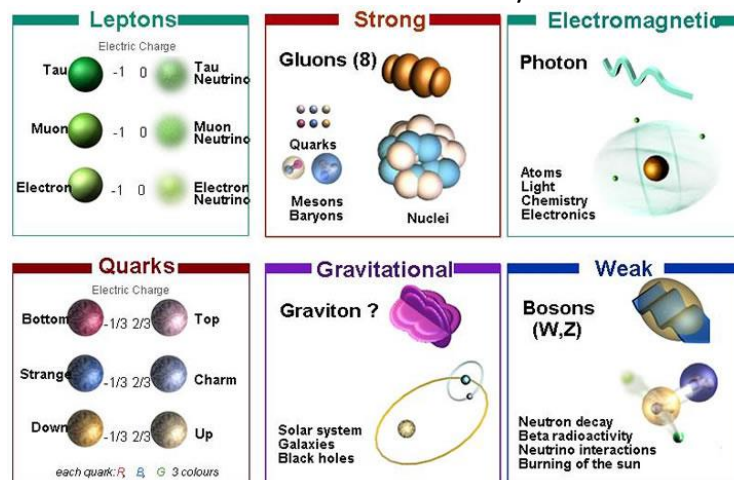
Force particles – The bosons

Each force has a particle associated with it which transmits the effects of that force. The table below summarizes the current understanding of the fundamental forces.

Force	Exchange Particle	Range (m)	Relative strength	Approximate decay time (s)	Example effects
Strong nuclear	gluon	10^{-15}	10^{38}	10^{-23}	Holding protons in the nucleus
Weak nuclear	W and Z bosons	10^{-18}	10^{25}	10^{-10}	Beta decay; decay of unstable hadrons
Electromagnetic	photon	∞	10^{36}	$10^{-20} - 10^{-16}$	Holding electrons in atoms
Gravitational	graviton	∞	1	Undiscovered	Holding matter in planets, stars and galaxies

At an everyday level we are familiar with contact forces when two objects are touching each other. Later in this unit you will consider electric fields as a description of how forces act over a distance. At a microscopic level we use a different mechanism to explain the action of forces; this uses something called exchange particles. Each force is mediated through an exchange particle or boson.

Many theories postulate the existence of a further boson, called the Higgs boson (sometimes referred to as the 'God particle'), which isn't involved in forces but is what gives particles mass. Attempts to verify its existence experimentally using the Large Hadron Collider at CERN and the Tevatron at Fermilab were rewarded on the 4th July 2012 when the announcement was made that the Higgs boson had been discovered

The Higgs boson plays a unique role in the Standard Model, by explaining why the other elementary particles, except the photon and gluon, are massive. In particular, the Higgs boson would explain why the photon has no mass, while the W and Z bosons are very heavy. The Higgs itself is incredibly massive with a mass equivalent to that of 133 protons (10^{-25} kg).
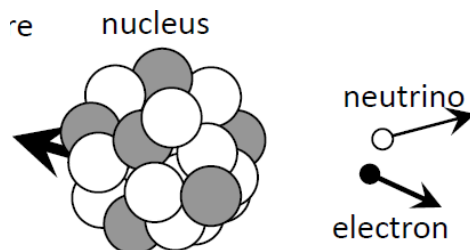
Neutrinos

All 3 leptons have a "ghostly" partner associated with it called the **neutrino**. This has no charge (its name means little neutral one). There is an electron neutrino, a muon neutrino and a tau neutrino.

Neutrinos were first discovered in radioactive beta decay experiments. In beta decay, a neutron in the atomic nucleus decays into a proton and an electron. When physicists were investigating beta decay they came up with a possible problem, the law of conservation of momentum appeared to be being violated.
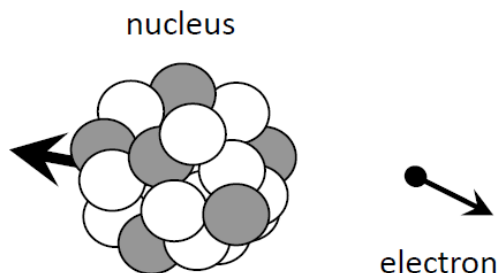
To solve this problem, it was proposed that there must be another particle emitted in the decay which carried away with it the missing energy and momentum. Since this had not been detected, the experimenters concluded that it must be neutral and highly penetrating.

This was the first evidence for the existence of the neutrino. (In fact, in beta-decay an anti-neutrino is emitted along with the electron as lepton number is conserved in particle reactions).

The equation for beta decay is

$$\,_{0}^{1}n \rightarrow \,_{1}^{1}p + \,_{-1}^{0}e + \,_{0}^{0}\bar{\nu}$$
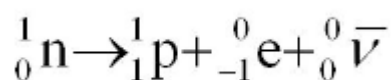
This shows a neutron changing into a proton while releasing an electron and an anti-neutrino.

Forces on Charged Particles

Electric Fields

In an electric field, a charged particle will experience a force. We use lines of force to show the strength and direction of the force. The closer the field lines the stronger the force. Field lines are continuous they start on positive charge and finish on negative charge. The direction is taken as the same as the force on a *positive* "test" charge placed in the field.
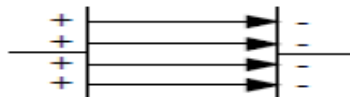
Point charges

Positive point charge
+ test charge has a force 'outwards'

Negative point charge
+ test charge has a force 'inwards'
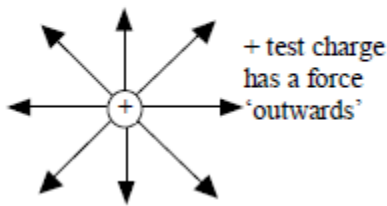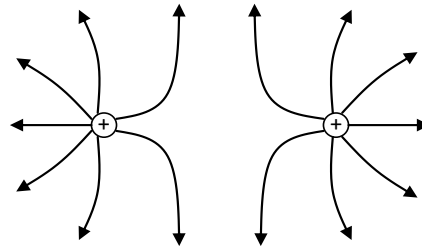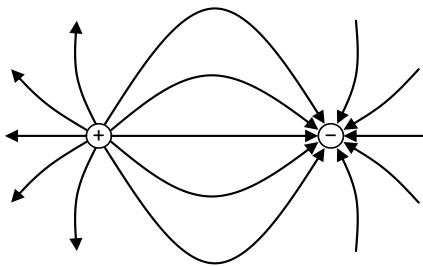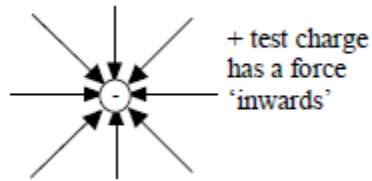
Parallel Plates

The field lines are equally spaced between the parallel plates. This means the field strength is constant. This is called a *uniform field*.

Moving changes

Depending on the nature of the field, charge will either be attracted or repelled. The rules are

- Opposite changes attract
- Same changes repel

For example the charged particle in this diagram must be negative as it is attracted to the positive plate.

Charge particle
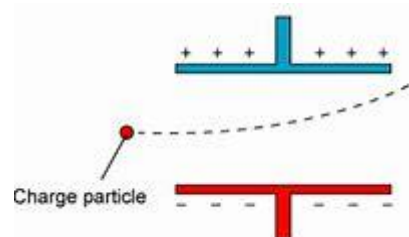
Work Done

We have seen already that electric fields are similar to gravitational fields. Consider the following:

If a mass is lifted or dropped through a height then work is done i.e. energy is changed.
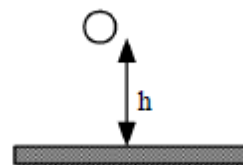
If the mass is dropped then the energy will change to kinetic energy. If the mass is lifted again then the energy will change to gravitational potential energy.

Change in gravitational potential energy = work done

Now consider a negative charge moved through a distance in an electric field
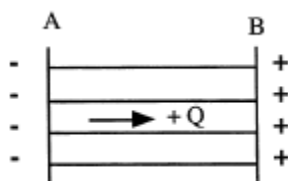
If the charge moves in the direction of the electric force, the energy will appear as kinetic energy. If a positive charge is moved against the direction of the force, as shown in the diagram, the energy will be stored as electric potential energy □

Definition of potential difference and the volt

Potential difference (p.d.) is defined to be a measure of the work done in moving one coulomb of charge between two points in an electric field. Potential difference (p.d.) is often called voltage. This gives the definition of the volt.

There is a potential difference of 1 volt between two points if 1 joule of energy is required to move 1 coulomb of charge between the two points, 1 V = 1 J C⁻¹

This relationship can be written mathematically: $E_w = QV$

Where E_w is energy (work done) in joules (J), Q is the charge in coulombs (C) and V is the potential difference (p.d.) in volts (V).
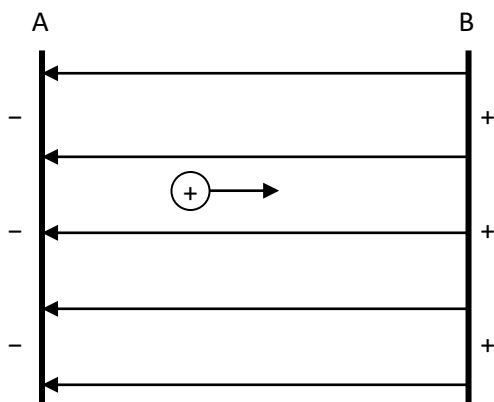
If the small positive charge, above, is released there is a transfer of energy to kinetic energy, i.e. the charge moves. Again, using the conservation of energy means that;

$$E_w = E_K$$

$$QV = \tfrac{1}{2}mv^2$$

Example: A positive charge of 3.0 μC is moved from A to B. The potential difference between A and B is 2.0 kV.

(a) Calculate the electric potential energy gained by the charge–field system.

(b) The charge is released. Describe the motion of the charge.

(c) Determine the kinetic energy when the charge is at point A.

(d) The mass of the charge is 5.0 mg. Calculate the speed of the charge

(a) $Q = 3.0\ \mu C = 3.0 \times 10^{-6}$ C

   $V = 2.0\ kV = 2.0 \times 10^3$ V

   $E_w = ?$

   $E_w = QV$

   $E_w = 3.0 \times 10^{-6} \times 2.0 \times 10^3$

   $E_w = 6.0 \times 10^{-3}$ J

(b) The electric field is uniform so the charge experiences a constant unbalanced force. The charge accelerates uniformly towards the negative plate A

(c) By conservation of energy,

   $E_K = E_w = 6.0 \times 10^{-3}$ J

(d) $m = 5.0\ mg = 5.0 \times 10^{-6}$ kg

   $E_K = 6.0 \times 10^{-3}$ J

   $v = ?$

   $E_K = \tfrac{1}{2}mv^2$

   $6.0 \times 10^{-3} = 0.5 \times 5.0 \times 10^{-6} \times v^2$

   $v^2 = 2.4 \times 10^{-3}$

   $v = 49\ m\ s^{-1}$

# Magnetic Field Around A Current Carrying Wire

In 1820 the Danish physicist Oersted discovered that a magnetic compass was deflected when an electrical current flowed through a nearby wire. This was explained by saying that when a charged particle moves a magnetic field is generated. In other words, a wire with a current flowing through it (a current-carrying wire) creates a magnetic field.

The magnetic field around a current-carrying wire is circular. For electron flow, the direction of the field can be found by using the left-hand grip rule.

direction of electron flow

Summary

A **stationary charge** creates an **electric field**.

A **moving charge** also creates a **magnetic field**
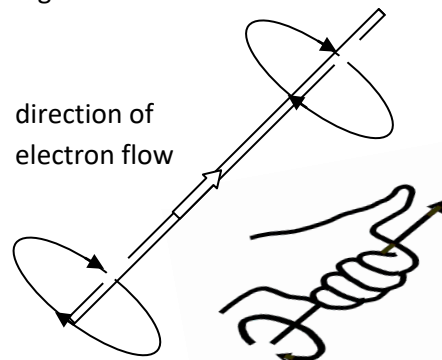
# Moving charges experience a force in a magnetic field

A magnetic field surrounds a magnet. When two magnets interact, they attract or repel each other due to the interaction between the magnetic fields surrounding each magnet.

A moving electric charge behaves like a mini-magnet as it creates its own magnetic field. This means it experiences a force if it moves through an external magnetic field (in the same way that a mass experiences a force in a gravitational field or a charge experiences a force in an electric field.)

Simple rules can be used to determine the direction of force on a charged particle in a magnetic field.

Movement of a negative charge in a magnetic field

One common method is known as **the right-hand motor rule**. This is shown in the figure on the right. The thumb gives the **motion (M)**, the **f**irst finger gives the **field (F)** and the second finger is the direction of <u>electron</u> **current (I)**.
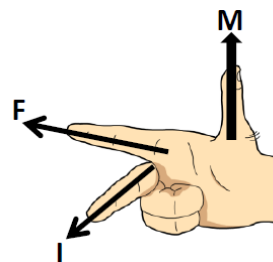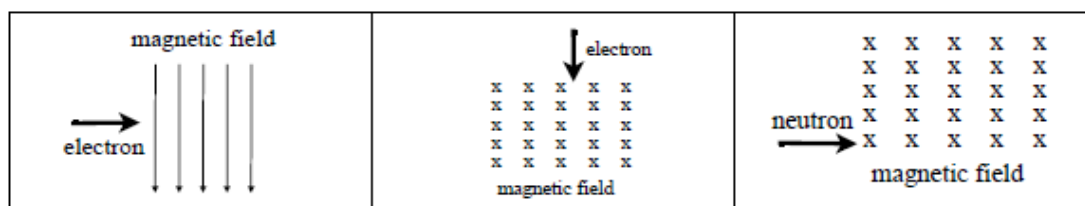
Movement of a positive charge in a magnetic field

For a positive charge, the left hand rule can be used. Again, the thumb gives the **motion (M)**, the **f**irst finger gives the **field (F)** and the second finger is the direction of <u>positive</u> **current (I)**.

Examples

| magnetic field → electron	electron ↓ x x x x x x x x x x x x x x x x x x x x x x x x x magnetic field	x x x x x x x x x x x x x x x neutron x x x x x → x x x x x magnetic field
Electron curves out of page	**Electron curves to the right**	**No change in direction (no charge=movement)**

Particle Accelerators

Particle accelerators are used to probe matter. They have been used to determine the structure of matter and investigate the conditions soon after the Big Bang. Particle accelerators are also used produce a range of electromagnetic radiations which can be used in many other experiments.

There are three main types of particle accelerators:

- linear accelerators
- cyclotrons
- synchrotrons

Regardless of whether the particle accelerator is linear or circular, the basic parts are the same:

- **a source of particles** – This must be a charge particle. At the Large Hadron Collider (LHC) at CERN the source of particles is simply a bottle of hydrogen gas. Electrons are stripped from the hydrogen atoms leaving positively charged protons.

- **beam pipes** (also called the **vacuum chamber)** - Beam pipes are special pipes which the particles travel through while being accelerated. There is a **vacuum** inside the pipes which ensures that the beam particles do not collide with other atoms such as air molecules.

- **accelerating structures** (a method of accelerating the particles) - As the particles speed around the beam pipes they enter special accelerating regions where there is **a rapidly changing electric field**. At the LHC, as the protons approach the accelerating region, the electric field is negative and the protons accelerate towards it. As they move through the accelerator, the electric field becomes positive and the protons are repelled away from it. In this way the protons increase their kinetic energy and they are accelerated to almost the speed of light.

- **a system of magnets** (electromagnets or superconducting magnets as in the LHC) - Newton's first law states that an object travels with a constant velocity (both speed and direction) unless acted on by an external force. The particles in the beam pipes would go in a straight line if they were not constantly going past powerful, fixed magnets which cause them to travel in a circle. There are over 9000 superconducting magnets at the LHC in CERN. These operate best at temperatures very close to the absolute 0K and this is why the whole machine needs to be cooled down. If superconducting magnets were not used, they would not be able to steer and focus the beam within such a tight circle and so the energies of the protons which are collided would be much lower.
- **a target** In some accelerators the beam collides directly with a stationary target, such as a metal block. In this method, much of the beam energy is simply transferred to the block instead of creating new particles. In the LHC, the target is an identical bunch of particles travelling in the opposite direction. The two beams are brought together at four special points on the ring where massive detectors are used to analyse the collisions
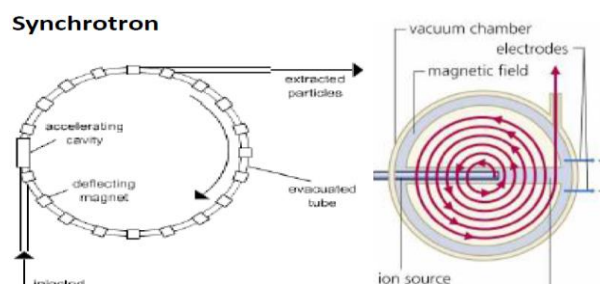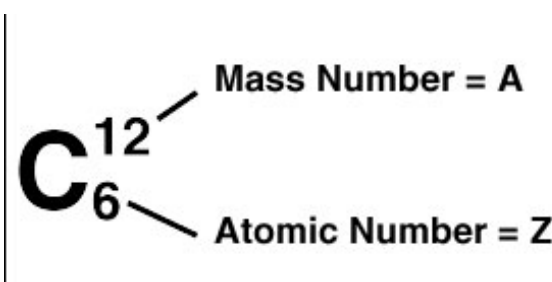
Nuclear Reactions

Nuclear Reactions

To examine nuclear reactions it is necessary to define a number of terms used to describe a nucleus.

Nucleon

A nucleon is a particle in a nucleus, i.e. either a proton or a neutron.

Atomic Number

The atomic number, Z, equals the number of protons in the nucleus. In a chemical symbol for an element it is written as a subscript before the element symbol

Example: There are 92 protons in the nucleus of a uranium atom so we write $_{92}U$

Mass Number

The mass number, A, is the number of nucleons in a nucleus. In a chemical symbol for an element it is written as a superscript before the element symbol.

Example: One type of atom of uranium has 235 nucleons so we write ^{235}U

Each element in the periodic table has a different atomic number and is identified by that number. It is possible to have different versions of the same element, called isotopes. An isotope of a atom has the same number of protons but a different number of neutrons, i.e. the same atomic number but a different mass number. An isotope is identified by specifying its chemical symbol along with its atomic and mass numbers. For example:

$C\ ^{12}_{6}$	$C\ ^{14}_{6}$
Contains $6p^+$	Contains $6p^+$
$6n$	$8n$
$6e^-$	$6e^-$
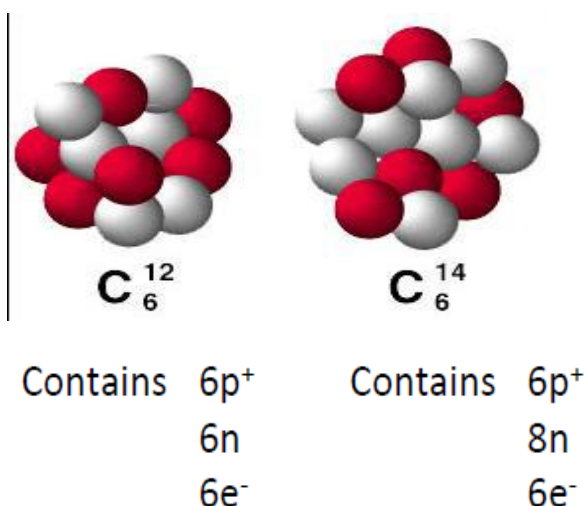
Radioactive Decay

Radioactive decay is the breakdown of a nucleus to release energy and matter from the nucleus. This is the basis of the word 'nuclear'. The release of energy and/or matter allows unstable nuclei to achieve stability. Unstable nuclei are called radioisotopes or radionuclides.

Radiation	Nature	Symbol
Alpha particle	Helium nucleus	^4_2He α
Beta particle	Fast electron	$^0_{-1}\text{e}$ β
Gamma ray	High frequency electromagnetic wave	γ

Representation of decay by symbols and equations
In the following equations, both mass number and atomic number are conserved, i.e. the totals are the same before and after the decay. The original radionuclide is called the parent and the new radionuclide produced after decay is called the daughter product

Alpha decay
Uranium 238 decays by alpha emission to give Thorium 234

$$^{238}_{92}\text{U} \rightarrow {}^{234}_{90}\text{Th} + {}^4_2\text{He}$$
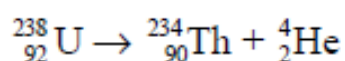
Mass number decreases by 4, atomic number decreases by 2 (due to loss of 2 protons and 2 neutrons).

Alpha decay usually occurs in heavy nuclei such as uranium or plutonium, and therefore is a major part of the radioactive fallout from a nuclear explosion. Since an alpha particle is relatively more massive than other forms of radioactive decay, it can be stopped by a sheet of paper and cannot penetrate human skin. A 4 MeV alpha particle can only travel a few centimetres through the air.
Although the range of an alpha particle is short, if an alpha decaying element is ingested, the alpha particle can do considerable damage to the surrounding tissue. This is why plutonium, with a long half-life, is extremely hazardous if ingested.

Beta decay
Atoms emit beta particles through a process known as beta decay. Beta decay occurs when an atom has either too many protons or too many neutrons in its nucleus. Two types of beta decay can occur. One type (positive beta decay) releases a positively charged beta particle, called a positron, and a neutrino; the other type (negative beta decay) releases a negatively charged beta particle, called an electron, and an antineutrino. The neutrino and the antineutrino are high-energy elementary particles with little or no mass and are released in order to conserve energy during the decay process. Negative beta decay is far more common than positive beta decay.
Lead 210 decays by beta emission to give Bismuth 210.

$$^{210}_{82}\text{Pb} \rightarrow {}^{210}_{83}\text{Bi} + {}^0_{-1}\text{e}$$
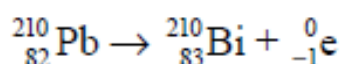
Mass number is unchanged, atomic number increases by 1

Gamma decay

Gamma rays are a type of electromagnetic radiation that results from a redistribution of electric charge within a nucleus. Gamma rays are essentially very energetic X - rays; the distinction between the two is not based on their intrinsic nature but rather on their origins. X rays are emitted during atomic processes involving energetic electrons. Gamma radiation is emitted by excited nuclei or other processes involving subatomic particles; it often accompanies alpha or beta radiation, as a nucleus emitting those particles may be left in an excited (higher-energy) state. 6

7 Gamma rays are more penetrating than either alpha or beta radiation, but less ionising. Gamma rays from nuclear fallout would probably cause the largest number of casualties in the event of the use of nuclear weapons in a nuclear war. They produce damage similar to that caused by X-rays, such as burns, cancer and genetic mutations.

Example

Thorium 230 decays into Radon. State the name of the particle emitted and give the equation for this decay. (Atomic number of Thorium is 90 and that of Radon is 88).

Solution

Because the atomic number of Radon is less than Thorium, an alpha particle must have been emitted.

$$^{230}_{90}\text{Th} \rightarrow \ ^{226}_{88}\text{Ra} + \ ^{4}_{2}\alpha$$
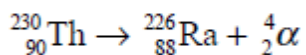
Nuclear Fission

Fission occurs when a heavy nucleus disintegrates, forming two nuclei of smaller mass number. This
radioactive decay is spontaneous fission. In this decay process, the nucleus will split into two
nearly equal fragments and several free neutrons. A large amount of energy is also released. Most
elements do not decay in this manner unless their mass number is greater than 230.

The stray neutrons released by a spontaneous fission can prematurely initiate a chain reaction. This means that the assembly time to reach a critical mass has to be less than the rate of spontaneous fission. Scientists have to consider the spontaneous fission rate of each material when designing nuclear weapons or for nuclear power. For example, the spontaneous fission rate of plutonium 239 is about 300 times larger than that of uranium 235.
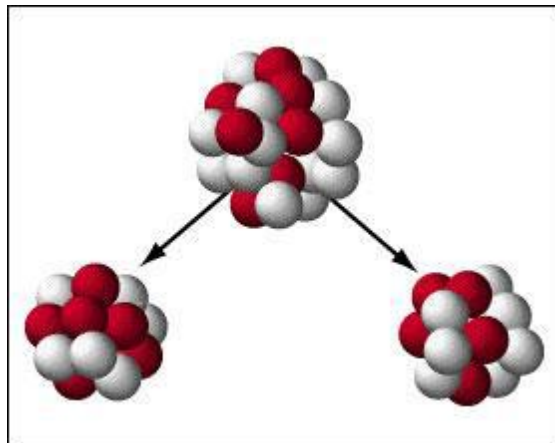
Fission can also be induced (persuaded to happen) by neutron bombardment.
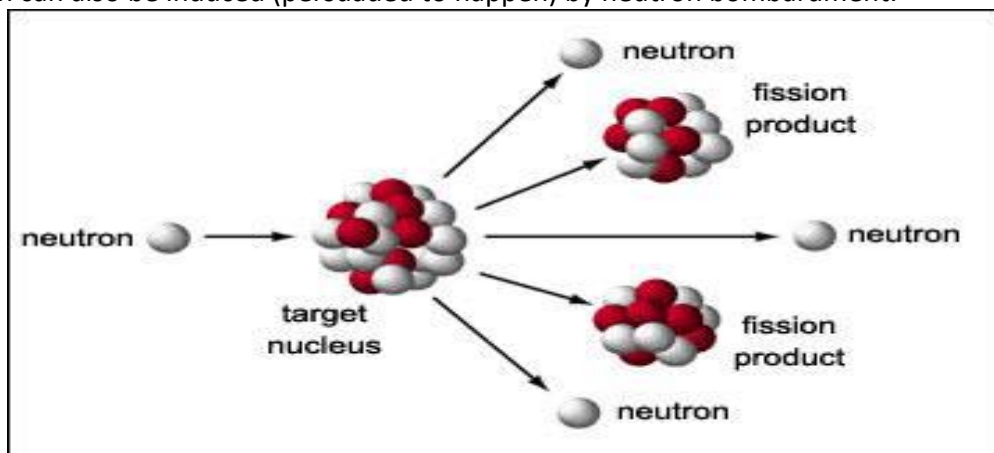
This is what happens in a nuclear reactor and is given by the equation;

$$^{235}_{92}U + ^{1}_{0}n \rightarrow ^{92}_{36}Kr + ^{141}_{56}Ba + 3\ ^{1}_{0}n + energy$$
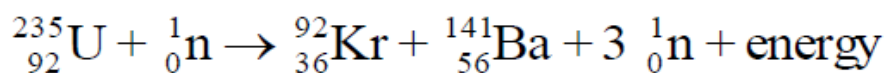
Mass number and atomic number are both conserved during this reaction. Even though the mass number is conserved, when the masses before and after the fission are compared accurately, there is a mass difference. The total mass before fission is greater than the total mass of the products.

Einstein suggested that mass was a form of energy, and that when there was a decrease in mass, an equivalent amount of energy was produced.
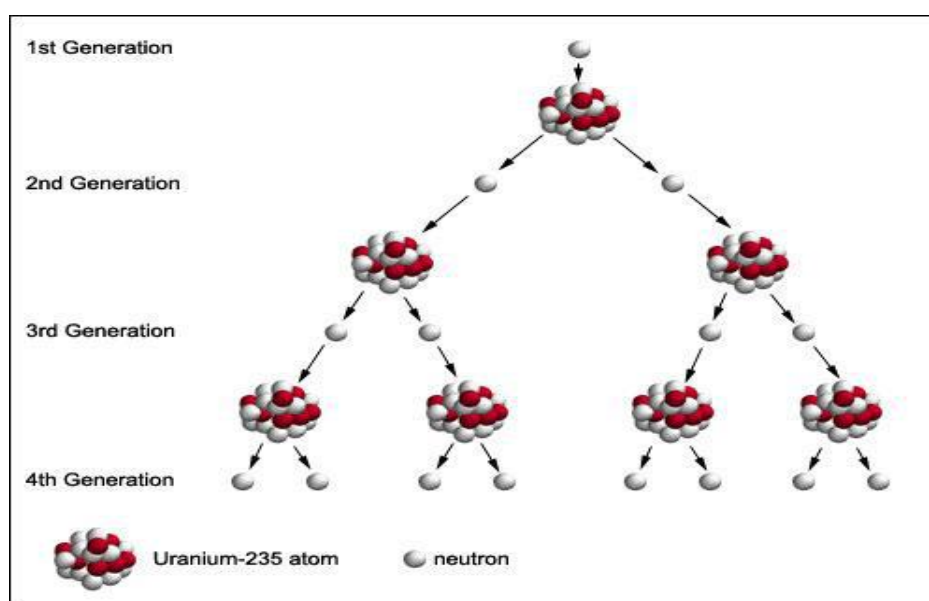
Energy In A Fission Reaction

Einstein's famous equation shows how mass and energy are related;

$$E = mc^2$$

This shows that the mass lost in a nuclear fission reaction is converted into energy.

Fission reactions take place in nuclear reactors. A chain reaction refers to a process in which neutrons released in fission produce an additional fission in at least one further nucleus. This nucleus in turn produces neutrons, and the process repeats. The process may be controlled (nuclear power) or uncontrolled (nuclear weapons).

These slow (thermal) neutrons cause a chain reaction so that more fissions occur. Control rods, e.g. boron, absorb some of the slow neutrons and keep the chain reaction under control. The kinetic energy of the fission products converts to **heat** in the reactor core.

Example
Calculate the energy released during this fission reaction

$$^{235}_{92}U + ^{1}_{0}n \rightarrow ^{137}_{56}Ba + ^{97}_{42}Mo + 2\,^{1}_{0}n + energy$$
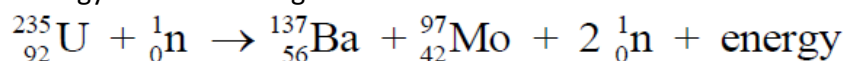
Solution

Mass before fission (kg)		Mass after fission (kg)	
U	390.2×10^{-27}	Ba	227.3×10^{-27}
n	1.675×10^{-27}	Mo	160.9×10^{-27}
		2n	3.350×10^{-27}
391.875×10^{-27}			
		391.550×10^{-27}	

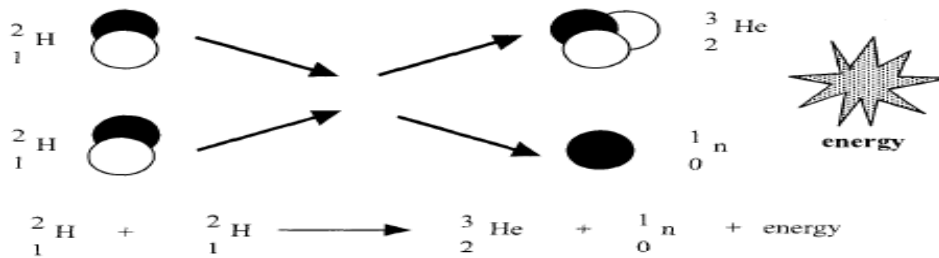Decrease in mass = $(391.875 - 391.550) \times 10^{-27} = 0.325 \times 10^{-27}$ kg

Energy released during this fission reaction, using $E = mc^2$

$E = 3.25 \times 10^{-28} \times (3 \times 10^8)^2 = 2.9 \times 10^{-11}$ J

This is the energy released by fission of a single nucleus.

Nuclear Fusion

Nuclear energy can also be released by the fusion of two light elements (elements with low atomic numbers).

$$^{2}_{1}H \ + \ ^{2}_{1}H \ \longrightarrow \ ^{3}_{2}He \ + \ ^{1}_{0}n \ + \ energy$$

Unlike nuclear fission, there is no limit on the amount of the fusion that can occur. The immense energy produced by our Sun is as a result of nuclear fusion.

Very high temperatures in the Sun (2.3×10^{7} K according to NASA) supply sufficient energy for nuclei to overcome repulsive forces and fuse together. When nuclei fuse, the final mass is less than the initial mass, ie there is a mass difference or mass defect. The energy produced can be calculated using;

$$E = mc^{2}$$

Fusion Example
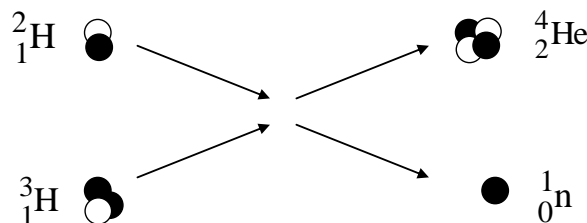
The nuclear reaction can be represented by:

$$^{2}_{1}H \ + \ ^{3}_{1}H \ \longrightarrow \ ^{4}_{2}He \ + \ ^{1}_{0}n \ + \ energy$$
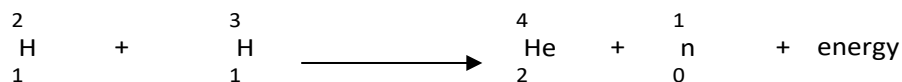
deuterium + tritium $\longrightarrow$ α-particle + neutron + energy

Once again it is found that the total mass after the reaction is less than the total mass before. This reduction in mass appears as an increase in the kinetic energy of the particles.

Mass before fusion (m_1):	deuterium	$3{\cdot}345 \times 10^{-27}$ kg
	tritium	$5{\cdot}008 \times 10^{-27}$ kg
	total	**$8{\cdot}353 \times 10^{-27}$ kg**
Mass after fusion (m_2):	α-particle	$6{\cdot}647 \times 10^{-27}$ kg
	neutron	$1{\cdot}675 \times 10^{-27}$ kg
	total	**$8{\cdot}322 \times 10^{-27}$ kg**
Loss of mass ($m_1 - m_2$):	$\underline{\Delta m}$	**$0{\cdot}031 \times 10^{-27}$ kg**

$$
\begin{aligned}
\text{Energy released} \qquad E \ &= \ mc^{2} \\
&= \ 0{\cdot}031 \times 10^{-27} \ \times \ (3{\cdot}0 \times 10^{8})^{2} \\
&= \ 2{\cdot}8 \times 10^{-12} \ \text{J}
\end{aligned}
$$

A Fusion Reactor

Fusion has been successfully achieved with the hydrogen bomb. However, this was an uncontrolled fusion reaction and the key to using fusion as an energy source is control.

The Joint European Torus (JET), in Oxfordshire, is Europe's largest fusion device. In this device, deuterium–tritium fusion reactions occur at over 100 million kelvin. Even higher temperatures are required for deuterium–deuterium and deuterium–helium 3 reactions
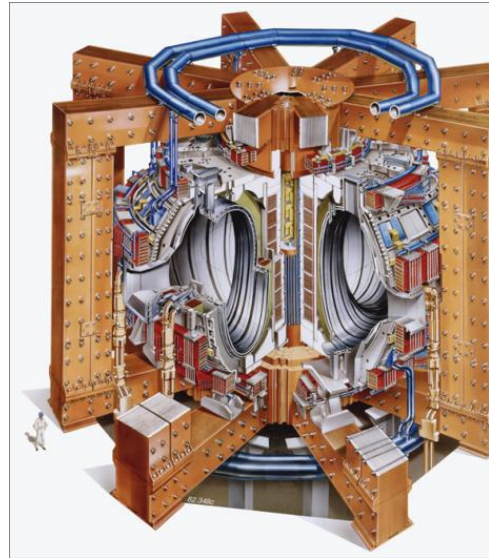
To sustain fusion, 3 conditions must be met at the same time.

- Extremely high plasma (ionised gas = charged particles) temperature (T): 100–200 million K

- A stable reaction lasting at least 5 seconds. This is called the **energy confinement time (t)**

- A precise plasma density of around 10^{20} particles/m^3
  (This is one thousandth of a gram/m^3 = one millionth the density of air).

One type of fusion reactor is called a Tokomak. In this design the plasma is heated in a torus or "doughnut-shaped" vessel.

The hot plasma is kept away from the vessel walls by applied magnetic fields. This is shown in the diagram on the right.

One of the main requirements for fusion is to heat the plasma particles to very high temperatures or energies. The methods on the following page are typically used to heat the plasma – all of them are employed on JET.
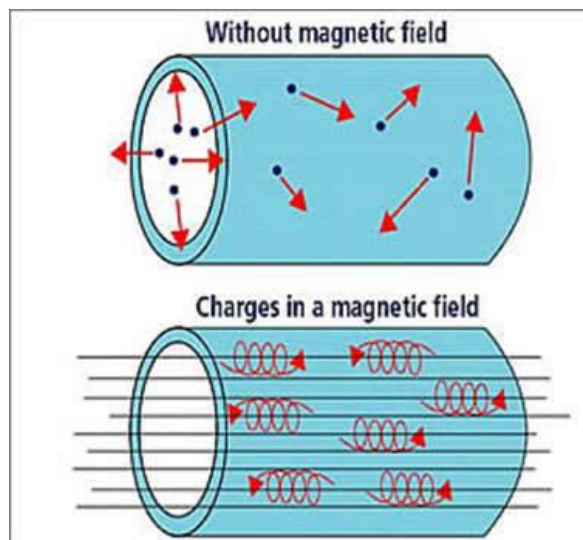
Wave-Particle Duality

The Photoelectric Effect

Under certain situations an electrically charged object can be made to discharge by shining electromagnetic radiation at it. This can be best demonstrated by charging a device on which the charge stored can be measured, like on a gold leaf electroscope. As charge is added to a gold leaf electroscope the thin piece of gold leaf rises up at an angle from the vertical rod to which it is attached.
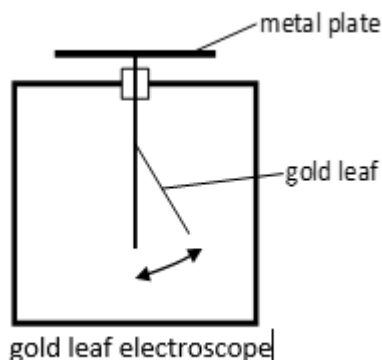
It is found that the electroscope will only discharge if it is **negatively charged** and the incident light is of a sufficiently **high frequency**. What does this mean? *How do we explain our results?*

Well, the UV radiation is causing electrons to leave the metal, making it discharge. We call these electrons **photoelectrons**. We know that all electromagnetic waves deliver **energy** so if they deliver enough energy to a particular electron, surely that electron could use the energy to leave the metal surface.

So, why is that low frequency (long wavelength) radiation won't eject electrons but waves of higher frequency will. Wave theory says that **any** wave will deliver energy so surely if you shine **any** radiation onto the metal for long enough eventually enough energy will be delivered to allow electrons to leave. But this is not the case!

The effect can only be explained if we consider that electromagnetic radiation does not always behave like a wave - a smooth continuous stream of energy being delivered to a point. In this case you can only explain the effect if the radiation is behaving like packets of energy being delivered one by one. We call these packets of energy **quanta** or **photons**. <u>**The photoelectric effect is evidence for the particle model of light.**</u>

Modern physics now takes the view that light can act both like a wave and like a particle without contradiction. This is known as **wave-particle duality.**

We can see that electrons are emitted if the following conditions are met:

- the radiation must have a high enough frequency (or short enough wavelength)
- the surface must be suitable – the energy in UV radiation will not eject electrons from iron, copper, lead etc., but will from sodium and potassium, although these are a bit tricky to use!

Light photons   Electrons ejected from the surface

Sodium metal
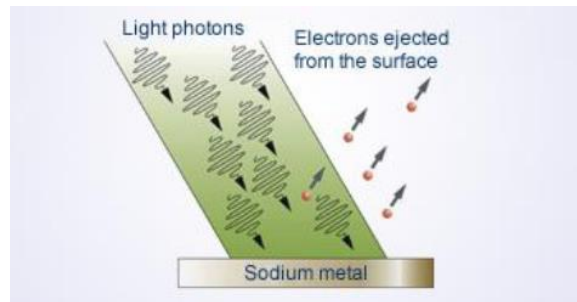
Each photon has a frequency and wavelength associated with it just as a wave in the wave theory had. However, each photon has a particular energy that depends on its frequency, given by the equation below.

$$E = hf$$

Where;

- E = energy of the photon (J)
- f = frequency of the photon (Hz)
- h = Planck's constant = 6.63×10^{-34} J s.

From this equation it can be seen that the energy of each photon is directly proportional to its frequency. The higher the frequency the greater the energy.

It is important to realise that if the **frequency** of the incident radiation is **not high enough** then no matter how great the **irradiance** of the radiation **no** photoelectrons are emitted. This critical or **threshold frequency**, f_o, is different for each metal. For copper the value of f_o is even greater than that of the ultraviolet part of the spectrum as no photoelectrons are emitted for ultraviolet radiation. Some metals, such as selenium and cadmium, exhibit the photoelectric effect in the visible light region of the spectrum.

Threshold frequency and work function
In general there is a minimum frequency of electromagnetic radiation required in order to eject electrons from a particular metal. This is called the **threshold frequency**, f_o, and is dependent on the surface being irradiated. The minimum energy required to release an electron from a surface is called the **work function**, E_o, of the surface.

$$E_o = hf_o$$

Such an electron would escape but would have no kinetic energy. If the energy of the incoming electron, E = hf, is greater than the work function, then the extra energy will appear as kinetic energy of the electron.
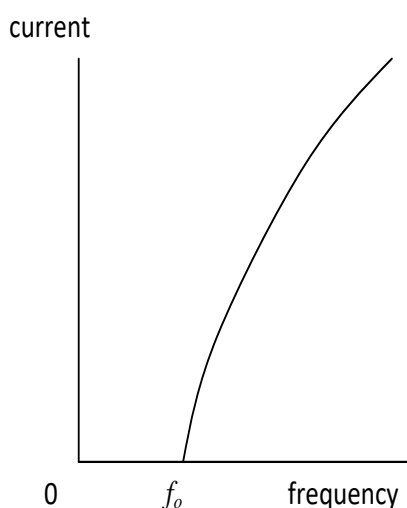
$$E_k = E - E_o$$

$$E_k = hf - hf_o$$

If a photon of incident radiation carries more energy than the work function value then the electron not only is freed at the surface but has "spare" kinetic energy and it can go places. An experiment can be carried out to demonstrate and quantify the photoelectric effect
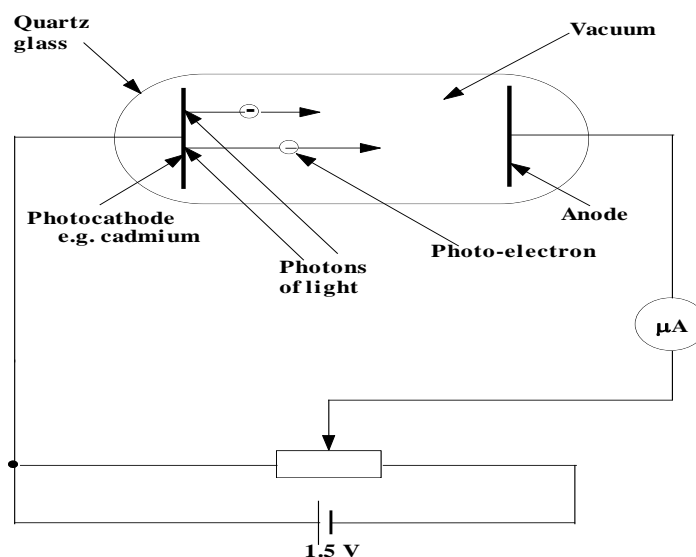
Notice that the supply is opposing the electron flow

Initially with the supply p.d. set at 0 V, light of various wavelengths or frequencies is allowed to fall on the photocathode. In each case a small current is observed on the microammeter. The value of this current can be altered by altering the irradiance of the light as this will alter the number of photons falling on the cathode and thus the number of photoelectrons emitted from the cathode. In fact the photocurrent is directly proportional to the irradiance of the incident light - evidence that irradiance is related to the number of photons arriving on the surface
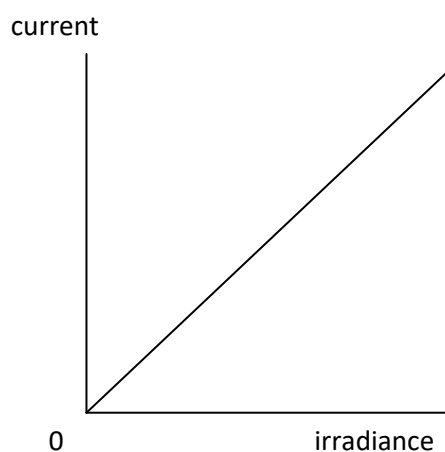
If when red light only is used the p.d. of the supply is slowly turned up in such a direction to oppose the electron flow, there comes a point when the p.d. is just sufficient to stop all the photoelectrons from reaching the anode. This is called the stopping potential for red. The photoelectrons are just not reaching the anode as they have not sufficient kinetic energy to cross the gap to the anode against the electric field. In fact their kinetic energy has all been turned to potential energy and they have come to rest.

Irradiance

The irradiance, *I*, at the surface is given by the power per unit area incident on a surface..

$$I = \frac{P}{A}$$

Where;
- I = irradiance in W m^{-2}
- P = Power in W
- A = Area in ms^2

Example;
A light bulb of power 100 W illuminates an area of 12 m^2. What is the irradiance of light hitting the area?

Solution
I = P/A
I = 100 / 12
I = 8.3 Wm^{-2}

Point Source

A point source is one which irradiates equally in all directions, i.e. the volume that will be irradiated will be a sphere. The surface area of a sphere can be calculated using $A = 4\pi r^2$, i.e. the area which will be irradiated is proportional to r^2 (or d^2).

Investigating irradiance

The relationship between irradiance of a point source and the distance from that source can be investigated using a simple experimental set up.

Activity

Aim: To investigate the variation of irradiance with distance from a point source of light.

Apparatus: 12 V power supply, 12 V lamp, light detector and meter, metre stick.
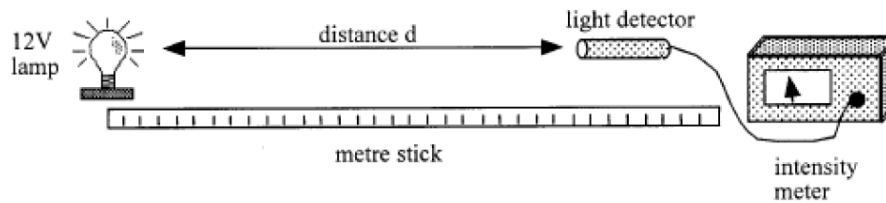
Instructions
1. Darken the room. Place the light detector a distance from the lamp.
2. Measure the distance from the light detector to the lamp and the Irradiance of the light at this distance.
3. Repeat these measurements for different distances between detector and lamp.
4. Plot a graph of light Irradiance against distance from the lamp.
5. Consider this graph and your readings and use an appropriate format to find the relationship between the light irradiance and distance from the lamp.

The graph of a typical set of results from the experiment is shown:

It is clear from this graph that the relationship between irradiance and distance is not a linear one. A plot of irradiance (in Wm^{-2}) against 1/distance is also not a straight line.

Plot of irradiance versus distance
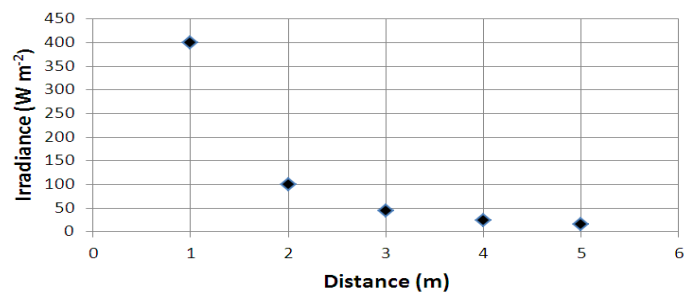
However, the graph of average irradia... against 2, a is a straight line. This demonstrates an **inverse relationship between irradiance and distance.**

Plot of irradiance versus 1/d^2
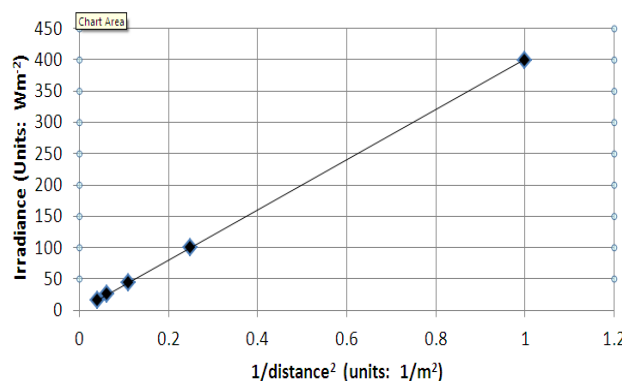
From the graph:

$$I \propto 1/d^2$$
$$Id^2 = \text{constant}$$

$$\boxed{I_1d_1^2 = I_2d_2^2}$$

I = irradiance in Wm^{-2}
d = the distance from a point source in m.

This is described as an ***inverse square law.***

Irradiance and Laser Light

Light from a laser
- is monochromatic (one frequency)
- is coherent
- is irradiant
- forms a parallel beam.

Because the beam is intense and parallel, it is a potential hazard to the eye.

A laser of power 0.1 mW forming a beam of radius 0.5 mm produces a light intensity given by

$$I = P/A = 0.1 \times 10^{-3} / \pi r^2 = 0.1 \times 10^{-3} / 7.85 \times 10^{-7} = 127 \ Wm^{-2}$$

An irradiance of this size is high enough to cause severe eye damage. It is far higher than the irradiance of light produced by a filament lamp.

Phase and Coherence

Phase

Two points on a wave that are vibrating in exactly the same way, at the same time, are said to be **in phase**, e.g. two crests, or two troughs.

Two points that are vibrating in exactly the opposite way, at the same time, are said to be **exactly out of phase**, or **180° out of phase**, e.g. a crest and a trough

v
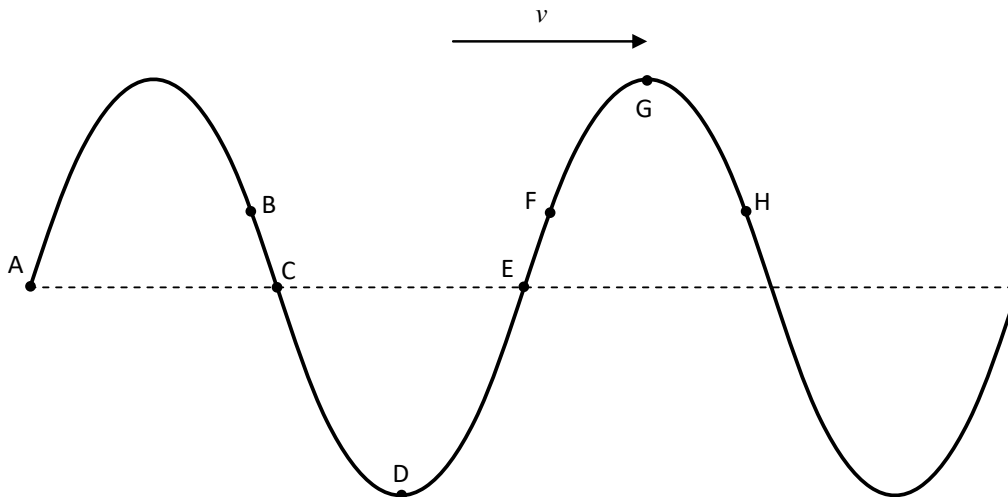
Points _A_ & _E_ or _B_ & _H_ are in phase.

Points _A_ & _C_ or _C_ & _E_ or _D_ & _G_ are exactly out of phase.

Points _C_ & _D_ or _D_ & _E_ or _E_ & _G_ are 90° out of phase.

Points _D_ and _G_ are at present stationary.

Points _A_ , _E_ and _F_ are at present rising.

Points _B, C_ and _H_ are at present dropping

Coherent Sources

Two sources that are oscillating with a constant phase relationship are said to be **coherent**. This means the two sources also have the same frequency. Interesting interference effects can be observed when waves with a similar amplitude and come from coherent sources meet

Interference

When two, or more, waves meet superposition, or adding, of the waves occurs resulting in one waveform. Interference is evidence for the wave model of light.
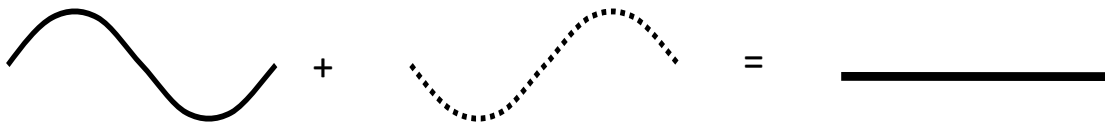
Constructive Interference

When the two waves are in phase constructive interference occurs
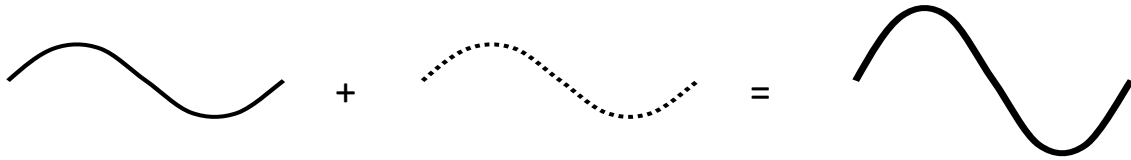
Destructive Interference

When the two waves are exactly out of phase destructive interference occurs

Only waves show this property of interference. Therefore interference is the test for a wave.

Interference can be demonstrated by allowing waves from one source to diffract through two narrow slits in a barrier. This can be done with water waves in a ripple tank, microwaves and light
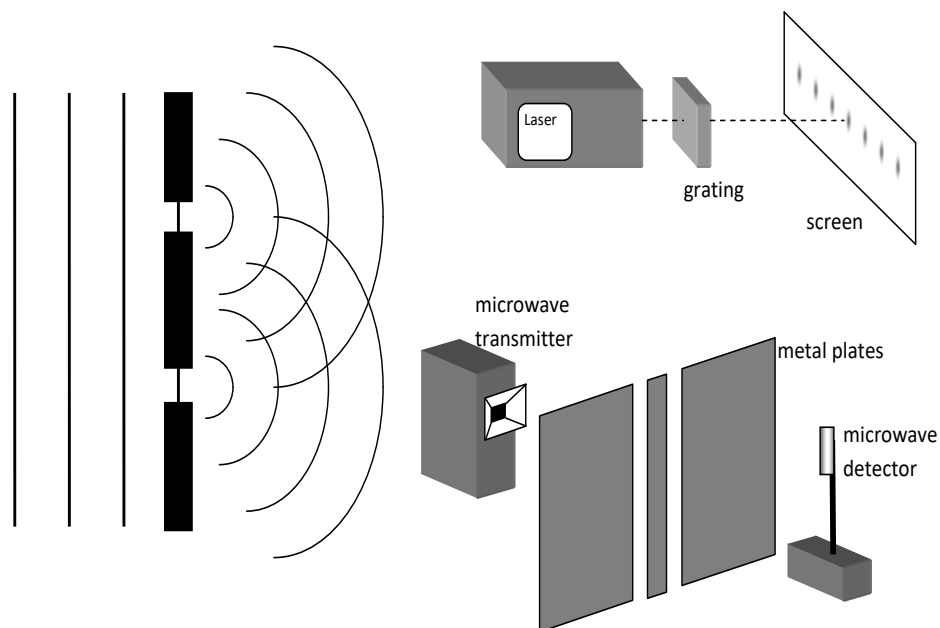
Interference of water waves

If two point sources produce two sets of circular waves, they will overlap and combine to produce an interference pattern. The semicircular lines represent crests; the troughs are between the crests.
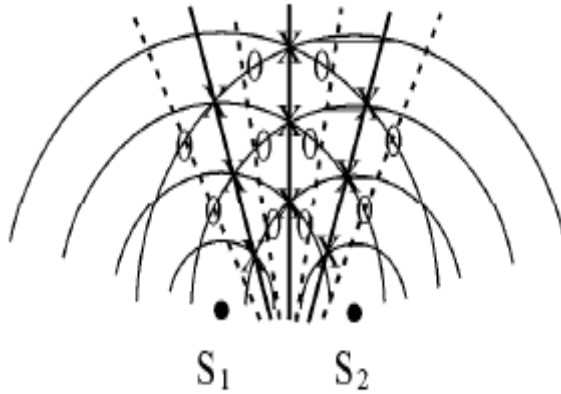
S1 and S2 are coherent point sources, ie the waves are produced by the same vibrator.
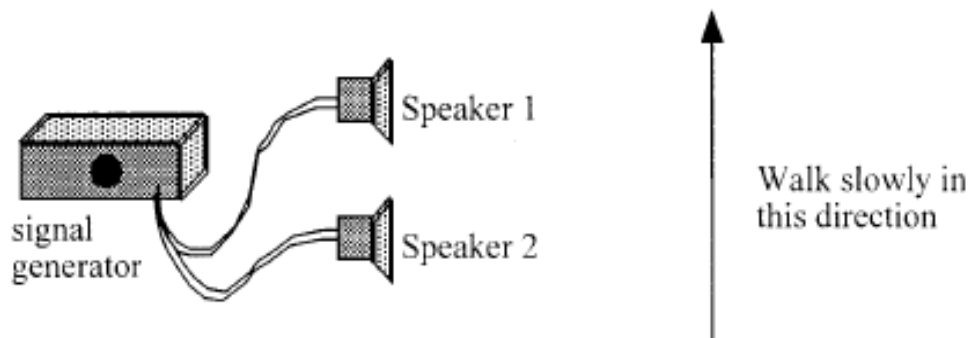
X = point of constructive interference.

O = point of destructive interference.

_____ = line of constructive interference

- - - - = line of destructive interference.

The points of constructive interference form waves with larger amplitude and the points of destructive interference produce calm water. The positions of constructive interference and destructive interference form alternate lines which spread out from between the sources. As you move across a line parallel to the sources, you will therefore encounter alternate large waves and calm water.

Interference of sound waves

If we set up the apparatus as shown and walk slowly across the 'pattern' as shown above. We should be able to listen to the effect on the *loudness* of the sound heard. The effect heard happens as there will be points where the sound is louder [constructive interference] and points where the sound is quieter [destructive interference]. The waves that meet at your ear will have travelled different distances from each loudspeaker. The difference in distance is known as the *path difference*.

Interference of light

Two sources of coherent light are needed to produce an interference pattern. Two separate light sources such as lamps cannot be used to do this, as there is no guarantee that they will be coherent (same phase difference). The two sources are created by producing two sets of waves from one monochromatic (single frequency) source. A laser is a good source of this type of light.

laser

Monochromatic light source

Double slit
Slit size - 10^{-7} m
(- 1λ)

$\leftarrow$ 1 - 3 metres $\rightarrow$

Screen
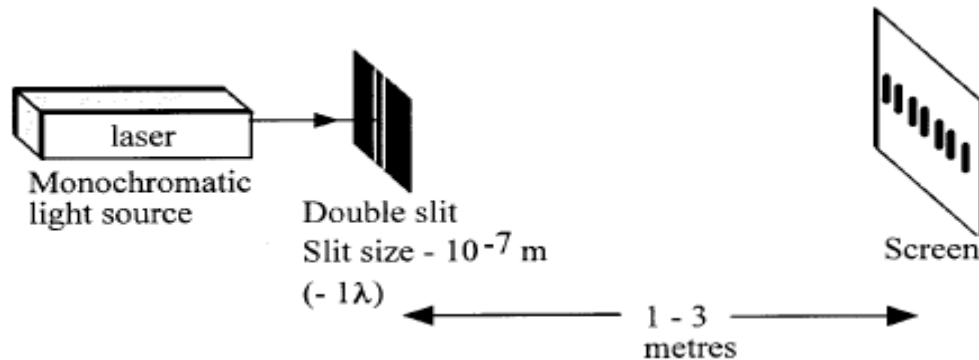
When we set up an experiment like the one shown we see an alternate series of light and dark lines.

Where the light arrives in phase, this is an area of constructive interference, and a bright fringe is seen.
Where the light arrives out of phase, this is an area of destructive interference, and a dark fringe is seen.
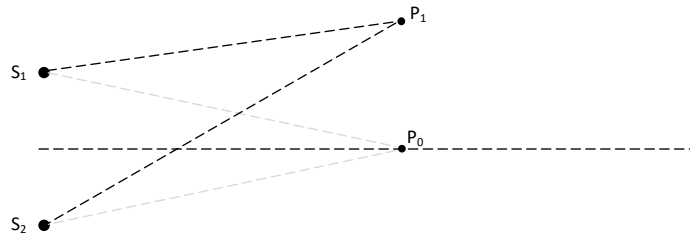
Interference and Path Difference
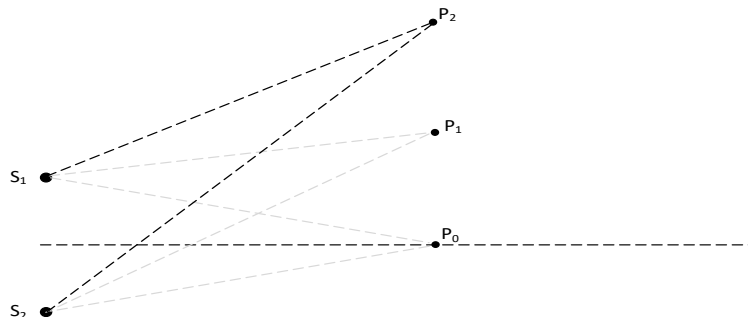## Constructive Interference

Two sources S_1 and S_2 in phase and 3 cm apart, wavelength 1 cm
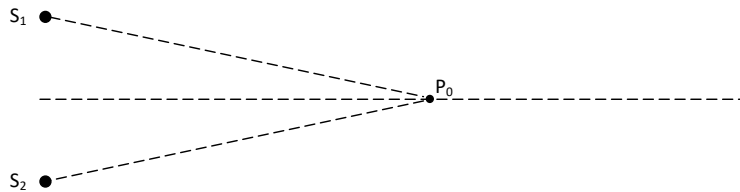
- P_0 is a point on the centre line of the interference pattern.
- P_0 is the same distance from S_1 as it is from S_2.
- The path difference between S_1P_0 and $S_2P_0 = 0$
- Waves arrive at P_0 in phase and therefore constructive interference occurs

- P_1 is a point on the first line of constructive interference out from the centre line of the interference pattern.
- P_1 is one wavelength further from S_2 than it is from S_1.
- The path difference between S_1P_1 and $S_2P_1 = 1 \times \lambda$
- Waves arrive at P_1 in phase and therefore constructive interference occurs


- P_2 is a point on the second line of constructive interference out from the centre line of the interference pattern.
- P_2 is one wavelength further from S_2 than it is from S_1.
- The path difference between S_1P_2 and $S_2P_2 = 2 \times \lambda$
- Waves arrive at P_2 in phase and therefore constructive interference occurs.

Constructive interference occurs when:

$$\text{path difference} = m\lambda$$

where m is an integer

# Destructive Interference
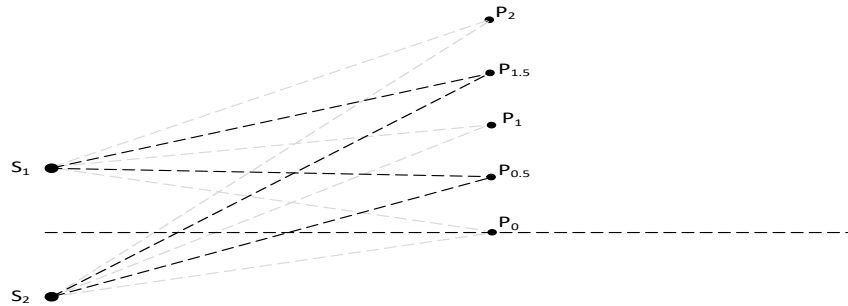
Destructive interference occurs when:

path difference = (m + ½ λ)

where m is an integer

Example

A student sets up two loudspeaker a distance of 1·0 m apart in a large room. The loudspeakers are connected in parallel to the same signal generator so that they vibrate at the same frequency and in phase.

The student walks from A and B in front of the loudspeakers and hears a series of loud and quiet sounds.

B

signal generator

A
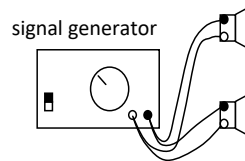
a)   Explain why the student hears the series of loud and quiet sounds.

b)   The signal generator is set at a frequency of 500 Hz. The speed of sound in the room is 340 m s^{-1}. Calculate the wavelength of the sound waves from the loudspeakers.

c)   The student stands at a point 4·76 m from loudspeaker and 5·78 m from the other loudspeaker. State the loudness of the sound heard by the student at that point. Justify your answer.

d)   Explain why it is better to conduct this experiment in a large room rather than a small room

Solution

a)   The student hears a series of loud and quiet sounds due to interference of the two sets of sound waves from the loudspeakers. When the two waves are in phase there is constructive interference and when the two waves are exactly out of phase there is destructive interference

b) $v = f\lambda$
        340 500 × λ
     λ= 0·68 m

c)   Path difference = 5·78 – 4·76 = 1·02 m
     Number of wavelengths = 1·02/0·68 = 1·5λ
     A path difference of 1·5λ means the waves are exactly out of phase. The student hears a quiet sound.

d)   In a small room, sound waves will reflect off the walls and

The Grating

A grating consists of many equally spaced slits positioned extremely close together. Light is diffracted through each slit and interference takes place in a similar fashion to the double slit we used when we investigated the interference of light. The advantage of the grating is that it has many more slits (up to 7500 per mm in our school set) so much more light is transmitted through and a clearer interference pattern is seen.
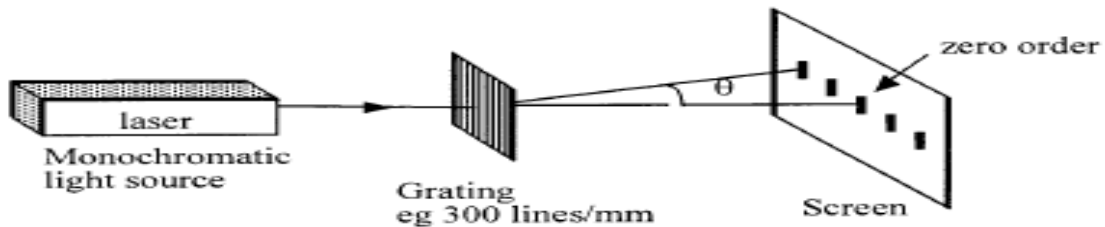
Gratings

A double slit gives a very dim interference pattern since very little light can pass through the two narrow slits. Using more slits allows more light through to produce brighter and sharper fringes.
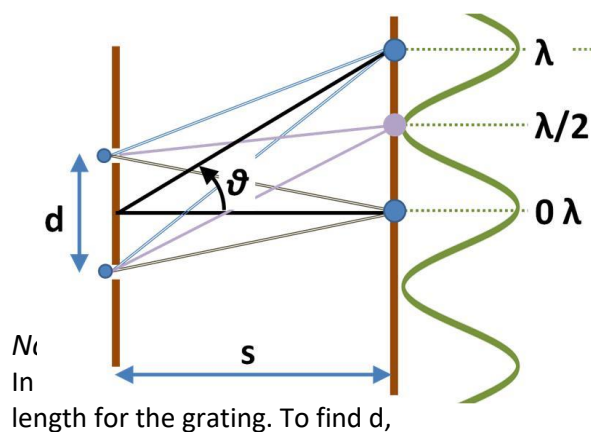
$$d \sin\theta = m\lambda$$

Where;

m = order of the maximum

λ = wavelength of light

d = separation of slits

θ = angle from zero order to m^{th} maximum.

A question may tell you the number of line per length for the grating. To find d,

$$d = \frac{length\ in\ meters}{number\ of\ lines}$$

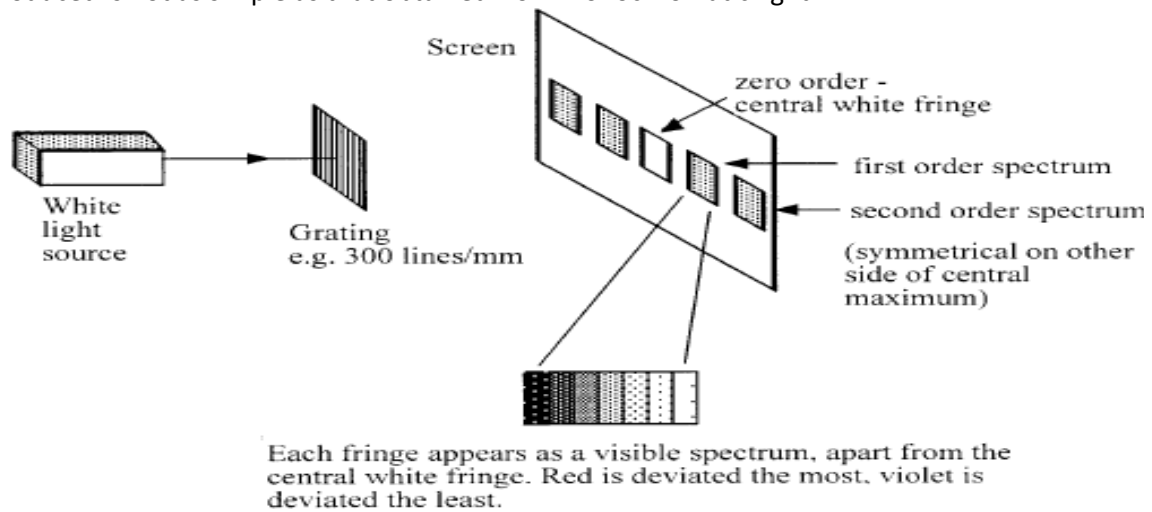For example, a grating with 300 lines per mm $d = \frac{1x10^{-3}}{300} = 3.3x10^{-6}m$

Changing the Pattern

To produce a widely spaced fringe pattern:

(a) Very closely separated slits should be used since $\sin\theta \propto 1/d$.

(b) A long wavelength light should be used, i.e. red, since $\sin\theta \propto \lambda$

(c) A large slit to screen distance should be used

Gratings and White Light

It is possible to use a grating to observe the interference pattern obtained from a white light source. Since white light consists of many different frequencies (wavelengths), the fringe pattern produced is not as simple as that obtained from monochromatic light.


Each fringe appears as a visible spectrum, apart from the central white fringe. Red is deviated the most, violet is deviated the least.

The central fringe is white because at that position, the **path difference** for all wavelengths present is **zero**, therefore all wavelengths will arrive in phase. The central fringe is therefore the same colour as the source (in this case, white).

The first maximum occurs when the **path difference** is 1λ. Since blue light has a shorter wavelength than red light, the path difference will be smaller, so the blue maximum will appear closer to the centre. Each colour will produce a maximum in a slightly different position and so the colours spread out into a **spectrum**.

These effects can also be explained using the formula $m\lambda = d\sin\theta$. If d and m are fixed, the angle θ depends on the wavelength. So, for any given fringe number, the red light, with a longer wavelength, will be seen at a greater angle than the blue light. The higher order spectra overlap.

# Comparing Spectra from Prisms and Gratings
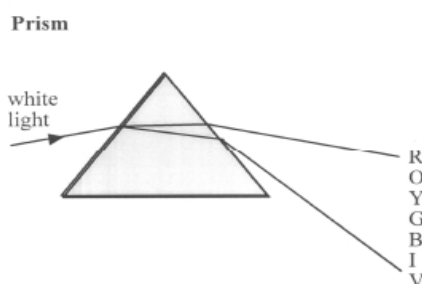
Only one spectrum produced.
Red deviated least, violet the most.
Bright images.
Usually less widely spaced (dispersed).
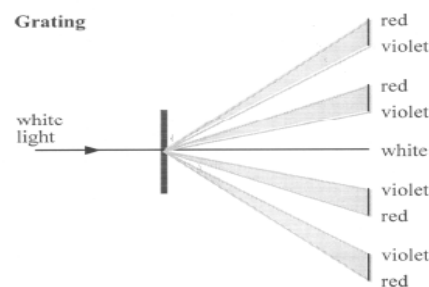
Many spectra produced, symmetrical about the central maximum.
Red deviated most, violet the least.
Less intense – energy divided between several spectra.
Usually more spread out.
Central image always the same colour as the source.

Refractive Index

If we carry out the experiment below;
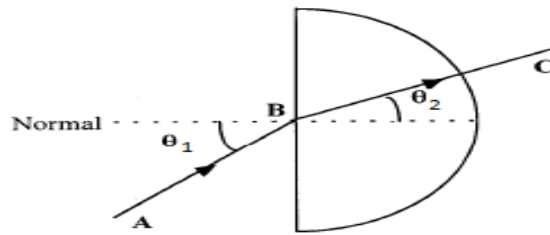
We find that the graph gives a straight line. This shows that sin θ1 / sin θ2 = k

This constant is known as the *refractive index* and is given the symbol n

sin θ1 / sin θ2 = n

The absolute refractive index of a material, n, is the refractive index of that material compared to the refractive index of a vacuum. The absolute refractive index of a vacuum (and therefore also air) is 1·0.

Snell's Law:

$n_1 \sin \theta_1 = n_2 \sin \theta_2$

Where medium 1 is a vacuum or air, and therefore $n_1 = 1·0$, this simplifies to:

$\sin \theta_1 = n_2 \sin \theta_2$ or $n = \dfrac{Sin \theta 1}{Sin \theta 2}$ (remember only when θ_1 is in air)

If the refraction occurs between <u>any</u> 2 mediums though we can still use;

n₁ sin θ1 = n₂ sin **θ₂** which when rearranged gives; $\dfrac{Sin \theta_1}{Sin \theta_2} = \dfrac{n_1}{n_2}$

Measuring the Refractive Index of Glass

The refractive index of glass can be measured by directing a ray of light through optical blocks and measuring the appropriate angles in the glass and the surrounding air.
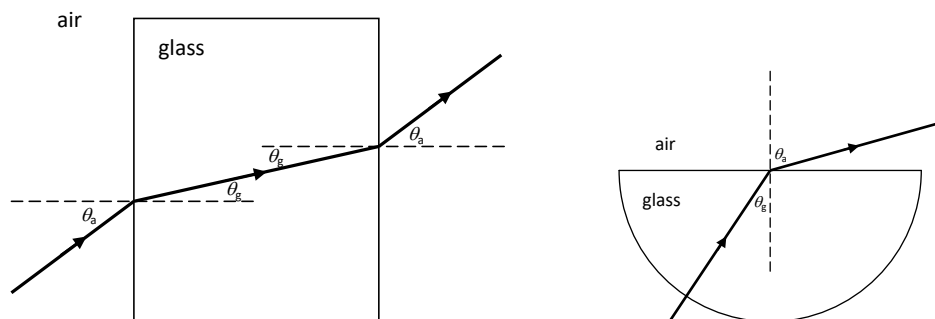
$$n_g = \frac{Sin \theta a}{Sin \theta_g}$$

Refractive Index and Frequency

The frequency of a wave is determined by the source that makes it. It must remain unchanged as it moves through different materials, i.e. the same number of peaks and troughs, otherwise it would no longer be the same wave.

However, we know that the speed of the wave changes so, given the relationship $v = f\lambda$, the wavelength of the wave must be changing. If we consider a wave moving from air to glass then frequency of wave in
air = frequency of wave in glass.

Since $f = v/\lambda$ this can be written as

$$v_1/\lambda_1 = v_2/\lambda_2$$

Rearranging gives

$$v_1/v_2 = \lambda_1/\lambda_2$$

This can be equated to the relationship we found in the last lesson. So,

$$\frac{n_2}{n_1} = \frac{\sin\theta_1}{\sin\theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$$

Example
Calculate the speed of light in glass of refractive index 1.50.

Solution

$$v_1/v_2 = n_2/n_1$$
$$3 \times 10^8/v_2 = 1.5/1$$
$$v_2 = 3 \times 10^8 / 1.5$$
$$= 2 \times 10^8 \text{ ms}^{-1}$$

Dependence of Refraction on Frequency

The refractive index of a medium depends upon the frequency (colour) of the incident light. We saw in the last topic that when light enters a glass prism, it separates into its component colours and produces a spectrum. This happens because each frequency (colour) is refracted by a different amount. Since violet is refracted more than red it follows that the refractive index for violet light must be greater than the refractive index for red light.
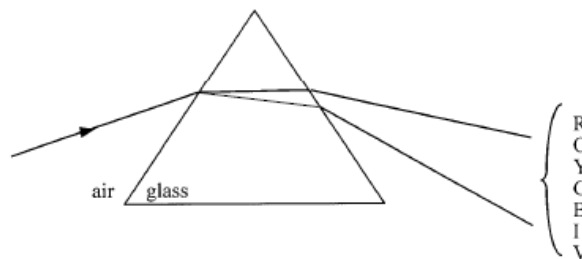
This means that the speed of light in the prism is greater for violet light than red light.

Critical Angle and Total Internal Reflection

When light travels from a medium of high refractive index to one of lower refractive index (e.g. glass into air), it bends away from the normal. If the angle within the medium θ_i is increased, a point is reached where the refracted angle, θ_r, becomes 90o.
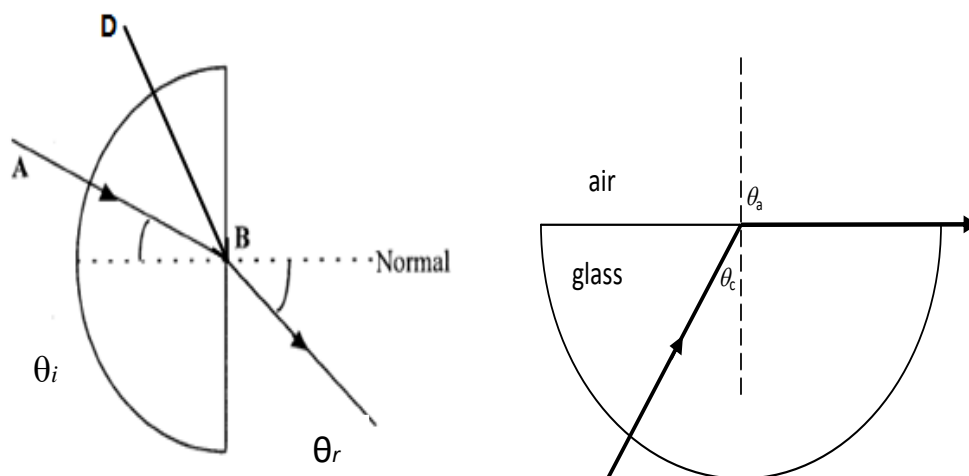
The angle in the medium which causes this is called the ***critical angle, θc***

How to measure the Critical Angle.

Apparatus: Ray box and single slit, 12 V power supply, semicircular perspex block, sheet of white paper, protractor
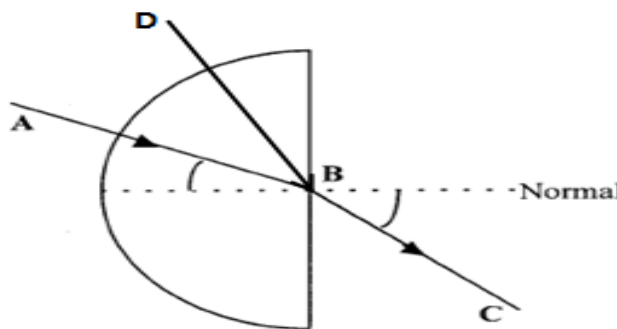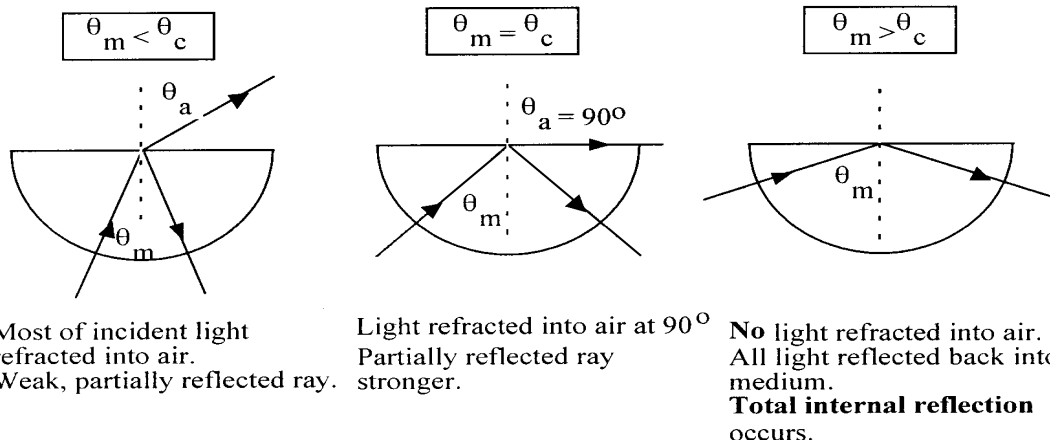

Instructions

1. Place the block on the white paper and trace around its outline. Draw in the normal at the midpoint B**.**

2. Draw a line representing the angle θ_i = 10°, the line AB in the diagram above.

3. Draw a line representing the angle θ_i = 60°, the line DB in the diagram above.

4. Direct the raybox ray along AB and gradually rotate the paper so that the ray moves from 10° to 60°.

5. Stop moving the paper when the refracted ray emerges at 90°to the normal. Mark the incident ray at which this happens.

6. Continue to move the paper and note what happens to the ray beyond this point.

If the angle in the medium is greater than the critical angle, then no light is refracted and **Total Internal Reflection** takes place within the medium.
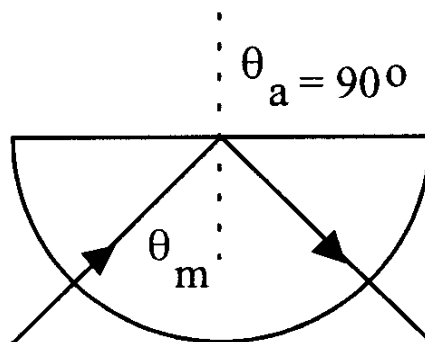
$\theta_m < \theta_c$	$\theta_m = \theta_c$	$\theta_m > \theta_c$

Most of incident light refracted into air. Weak, partially reflected ray.

Light refracted into air at 90° Partially reflected ray stronger.

No light refracted into air. All light reflected back into medium. **Total internal reflection occurs.**

Deriving the critical angle

At the critical angle, $\theta m = \theta c$ and $\theta a = 90°$

$$\frac{\sin \theta_a}{\sin \theta_m} = \frac{\sin 90°}{\sin \theta_c} = \frac{1}{\sin \theta_c}$$

$$n = \frac{1}{\sin \theta_c}$$

Note light would be passing along flat edge at critical angle.

For angles of incidence less than the critical angle some reflection and some refraction occur. The energy of the light is split along two paths.

For angles of incidence greater than the critical angle only reflection occurs, i.e. total internal reflection, and all of the energy of the light is reflected inside the material.
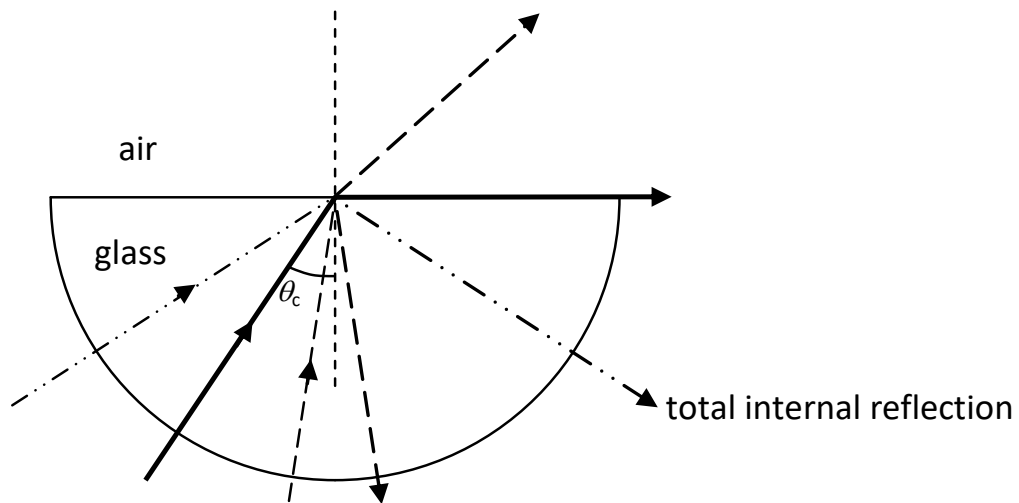
Total internal reflection allows light signals to be sent large distances through optical fibres. Very pure, high quality glass absorbs very little of the energy of the light making fibre optic transmission very efficient.

Background to Spectra

Emission spectra

An emission spectrum is the range of colours given out (emitted) by a light source. There are two kinds of emission spectra: continuous spectra and line spectra. To view spectra produced by various sources, a spectroscope or spectrometer can be used.


Continuous spectra

 In a continuous spectrum all frequencies of radiation (colours) are present in the spectrum. The continuous spectrum colours are red, orange, yellow, green, blue, indigo, violet.

Line spectra

Some sources of light do not produce continuous spectra when viewed through a spectroscope. They produce line spectra – coloured lines spaced out by different amounts. Only specific, well-defined frequencies of radiation (colours) are emitted.
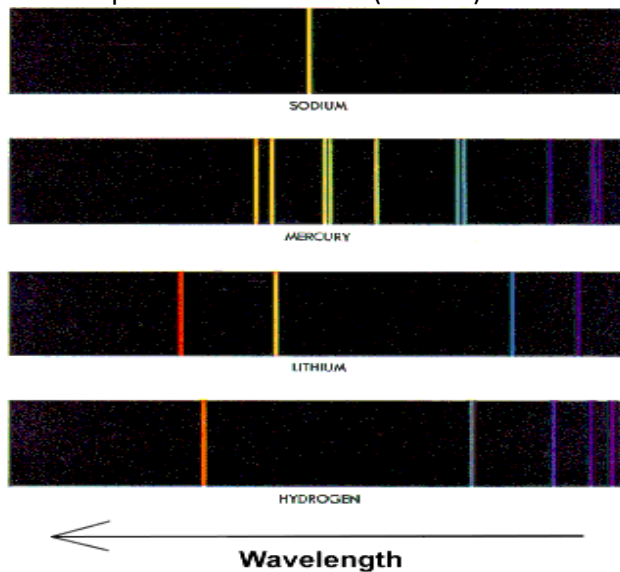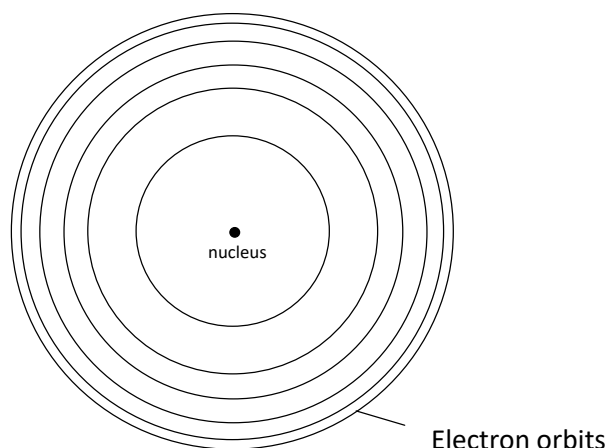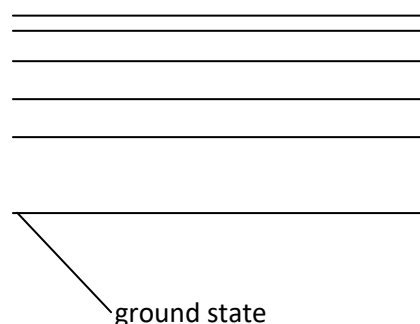
Line Emission Spectra

As with the photoelectric effect, line emission spectra cannot be explained by the wave theory of light. In 1913, Neils Bohr, a Danish physicist, first explained the production of line emission spectra. This explanation depends on the behaviour of both the electrons in atoms and of light to be quantised.

The electrons in a *free* atom are restricted to particular radii of orbits. A free atom does not experience forces due to other surrounding atoms. Each orbit has a discrete energy associated with it and as a result they are often referred to as energy levels.

Bohr model of the atom   **Energy level diagram**


nucleus

ground state

Electron orbits

The Bohr model is able to explain emission spectra as;

- electrons exist only in allowed orbits and they do not radiate energy if they stay in this orbit.
- electrons tend to occupy the lowest available energy level avaliable, i.e. the level closest to the nucleus. (The closest level to the nucleus is called the ground state)
- electrons in different orbits have different energies.
- electrons can only jump between allowed orbits. If an electron absorbs a photon of exactly the right energy, it moves up to a higher energy level.
- if an electron drops down from a high to a low energy state it emits a photon which carries away the energy, i.e light is emitted when electrons drop from high energy levels to low energy levels. The allowed orbits of electrons can be represented in an energy level diagram.

Energy level diagram

Electrons can exist either in the *ground state*, E0, which is the orbit closest to the nucleus (shown as the dashed line at the bottom) or in various *excited states*, E1–E4. These correspond to orbits further away from the nucleus.

An electron which has gained just enough energy to leave the atom has 0J kinetic energy. This is the *ionisation level*. This means that an electron which is trapped in the atom has less energy and so it has a *negative energy* level.
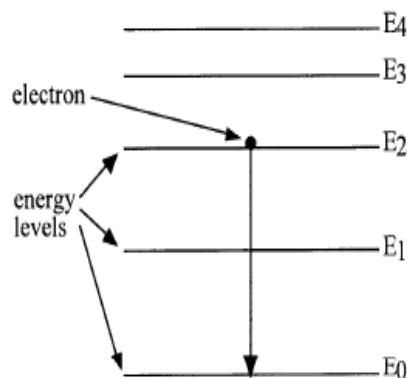
The electrons move between the energy levels by absorbing or emitting a photon of electromagnetic radiation with just the correct energy to match the gap between energy levels. As a result only a few frequencies of light are emitted as there are a limited number of possible energy jumps or transitions. When an electron is not attached to an atom, it has zero potential energy.

The lines on an emission spectrum are made by electrons making the transition from high energy levels (excited states) to lower energy levels (less excited states).
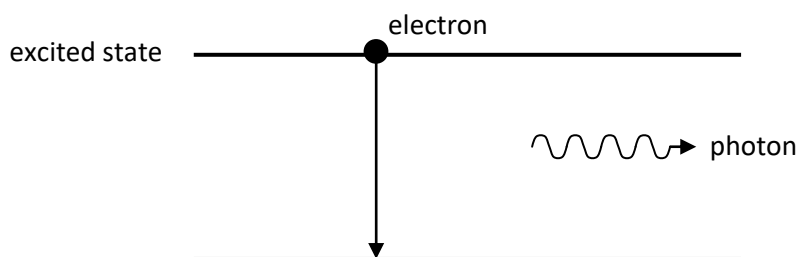
When the electron drops the energy is released in the form of a photon where its energy and frequency are related by the energy difference between the two levels. For example take an electron dropping from level two to one;

$$E_2 - E_1 = E = hf$$

From this calculation we can go on and work out the frequency of the emitted photon.
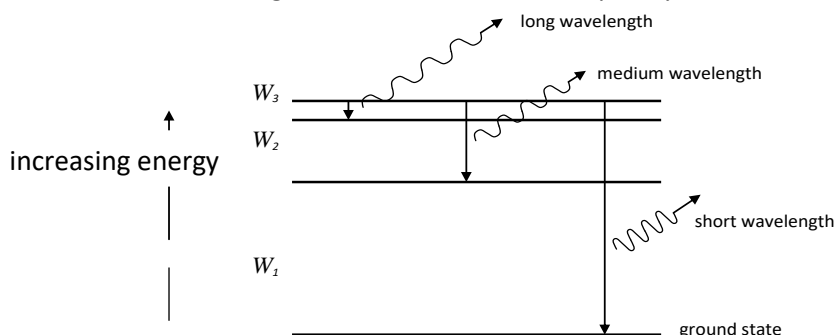
As we can see there are many different combination of gap between energy levels and as such there are numerous frequencies that can be emitted from one type of atom. From this we can say;

- The photons emitted may not all be in the visible wavelength.
- Only certain frequencies of light can be emitted from specific atoms.
- The larger the number of excited electrons that make a particular transition, the more photons are emitted and the brighter the line in the spectrum.

The Continuous Spectrum

A continuous visible spectrum consists of all wavelengths of light from violet (~400 nm) to red (~700 nm). Such spectra are emitted by glowing solids (a tungsten filament in a lamp), glowing liquids or gases under high pressure (stars). In these materials the electrons are not *free*. The electrons are shared between atoms resulting in a large number of possible energy levels and transitions.

Absorption Spectra

When light is passed through a medium containing a gas, then any photons of light which have the same frequency as the photons emitted to produce the emission spectrum of the gas, are absorbed by the gas. This is because the energy of the photons of light (*hf*) is the same as the energy difference required to cause an electron to be moved from the lower to the higher energy level. The energy is then absorbed by the electron and that photon is 'removed' from the incident light.

$$W_2 = W_1 + hf$$
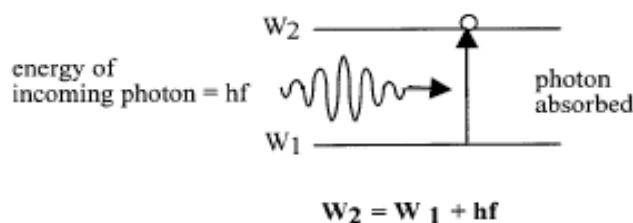
White light from the compact light source is passed through a large lens and brought to a focus within a sodium flame. The light then passes through another lens and is brought to focus on the slit of a spectrometer. Viewing the spectrum produced through the spectrometer reveals a continuous spectrum with two black lines in the yellow region. This is the absorption spectrum of sodium. The black lines correspond to the position of the sodium D lines in the sodium emission spectrum. These lines correspond to the frequencies of the photons absorbed by the electrons within the sodium flame.
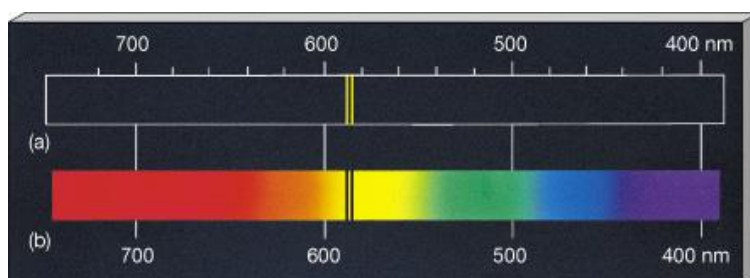
The energy absorbed by the electrons within the sodium flame will be emitted again as a photon of the same energy and frequency as the one absorbed, but it is highly unlikely that it will be emitted in the same direction as the original photon. Therefore the spectrum viewed through the spectrometer will show black absorption lines corresponding to the absorbed frequency of radiation.

Absorption Lines in Sunlight

The white light produced in the centre of the Sun passes through the relatively cooler gases in the outer layer of the Sun's atmosphere. After passing through these layers, certain frequencies of light are missing. This gives dark lines (Fraunhofer lines) that correspond to the frequencies that have been absorbed.

The lines correspond to the bright emission lines in the spectra of certain gases. This allows the elements that make up the Sun to be identified.

In summary

We have three types of spectrum;
1. Continuous, where there is a complete range of wavelength from Red to Violet created by sources such as tungsten lamps and stars
2. Emission, created by excited atoms in a low pressure gas. Each element emits its own unique line spectrum that can be used to identify that element.
3. Absorption, light passes through the a cooler gas and after passing through, certain frequencies of light are missing. This gives dark lines that correspond to the frequencies that have been absorbed.