Eastwood High School Physics Department

Cfe Higher Unit 3 Electricity



Summary Notes

Electrons and Energy

Monitoring and measuring alternating current

Alternating current

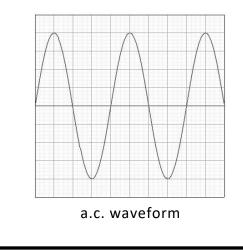
An alternating current (a.c.) changes direction and instantanteous value with time. The electrons flow in one direction before changing to flow in the opposite way. This contrasts with direct current (d.c.), which flows in one direction only.

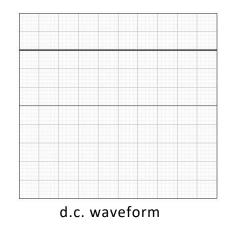
Alternating current is produced by rotating an electromagnet in a coil of wire. This means that the induced voltage, which is constantly changing in the form of a sine function, pushes the current one way and then the other.

An oscilloscope shows a trace on a screen of how a voltage varies with time.

The changing voltage is plotted on the *y*-axis against time on the *x*-axis.

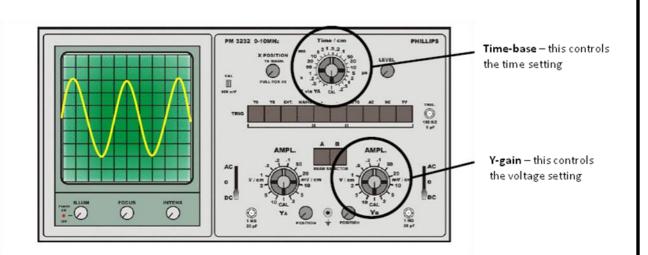
Examples of each type of current when displayed on an oscilloscope screen are shown below:





Measuring frequency and peak voltage

The values for voltage and time on an oscilloscope can be read from the number of divisions on the screen multiplied by the scale shown on one of two dials on the control panel at the side of the screen.



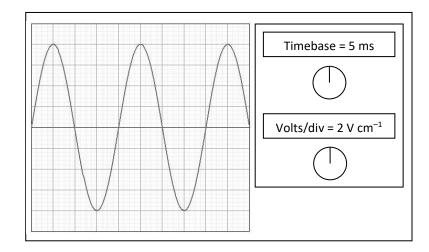
The voltage axis scale, called the y-gain, is usually given as volts/div or volts/cm and the time axis scale, known as the time-base, is shown as multiples of seconds/div or seconds/cm.

The **frequency** of an a.c. signal is calculated from its period. This is the time for one complete cycle of the current as it moves in one direction then the other, so we measure the horizontal distance on the screen between crests.

The **peak voltage** is defined as the distance from the maximum positive value to the centre line (or from the maximum negative value to the centre line). This can be obtained from an oscilloscope by counting the number of volts from the maximum value to the minimum value and dividing by two.

Worked example

Calculate (i) the frequency and (ii) the peak voltage of the waveform shown on the CRO screen below. Each box on the CRO screen has a side of length 1 cm.



(i) Frequency:

The distance between crests is 4 cm. The time base is set at 5 ms cm^{-1} ,

Period, $T = 4 \times 5 \text{ ms} = 4 \times 0.005 = 0.02 \text{ s}$ $V_{\text{peak}} = \frac{1}{2} \times 8 \times 2$

 $f = \frac{1}{T} = \frac{1}{0.02} = \frac{50 \text{ Hz}}{2}$

(ii) Peak Voltage:

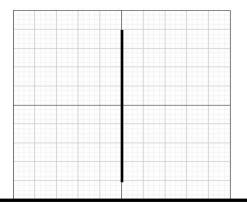
The distance from bottom to top is 8 cm. The volts/div is set at 2 V cm⁻¹,

 $V_{\text{peak}} = 8 \text{ V}$

Timebase switched off

If the time base is switched off, the a.c. signal will not spread along the x-axis. However, the voltage variation will continue to oscillate up and down, meaning a straight vertical line will be displayed on the screen.

The height of this line from bottom to top can be processed in exactly the same way as above, ie halved then converted into voltage using the volts/div.



Alternating current – calculating an average

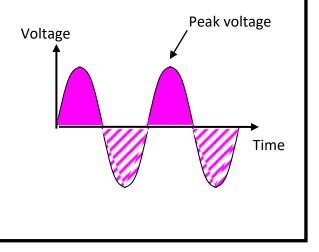
Electricity is a method of transferring energy, so alternating current (a.c.) is capable of transferring energy in the same way as direct current (d.c.).

The instantaneous amount of power being supplied can be calculated from the voltage and/or current at a particular time, using the equation $P = I \times V$.

However, in a.c. these values are changing constantly, so it is necessary to calculate an average. However, for a sine wave there is an equal number of peaks above the centre line (positive) and below the line (negative).

Therefore, the average value of the voltage during any complete cycle is zero!

It is necessary to use a different 'average'!



Alternating current – peak and rms

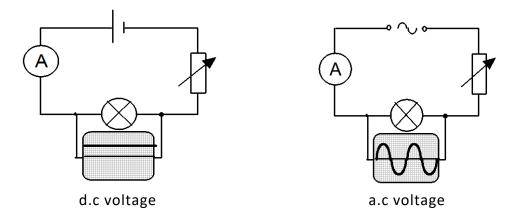
The amount of energy transmitted by a.c. will depend on some 'average' value of the voltage. The 'average' value of an a.c. voltage is called the root mean square (rms) voltage ($V_{\rm rms}$).

The rms voltage is defined as the value of direct voltage that produces the same power (eg heating or lighting) as the alternating voltage.

The rms value is what is quoted on a power supply so that a fair comparison between a.c. and d.c. can be made eg a 6 V battery (d.c.) will produce the same brightness of light bulb as a 6 V rms a.c. supply.

The rms current has a similar definition to the rms voltage.

Consider the following two circuits, which contain identical lamps.



The variable resistors are altered until the lamps are of equal brightness. As a result the d.c. has the same value as the effective a.c. (ie the lamps have the same power output).

By measuring the voltages shown on the two oscilloscopes, it is possible to determine the relationship between the rms voltage and the peak voltage. Also, since V = IR applies to the rms values and to the peak values, a similar equation for current can be deduced.

$$V_{peak} = \sqrt{2}V_{rms}$$
 $I_{peak} = \sqrt{2}I_{rms}$

Example: A transformer is labelled with a primary coil of 230 V_{rms} and a secondary coil of 12 V_{rms}. What is the peak voltage which would occur in the secondary?

$$V_{peak} = \sqrt{2} \times V_{rms}$$
$$V_{peak} = 1.41 \times 12$$
$$V_{peak} = \frac{17.0 \text{ V}}{2}$$

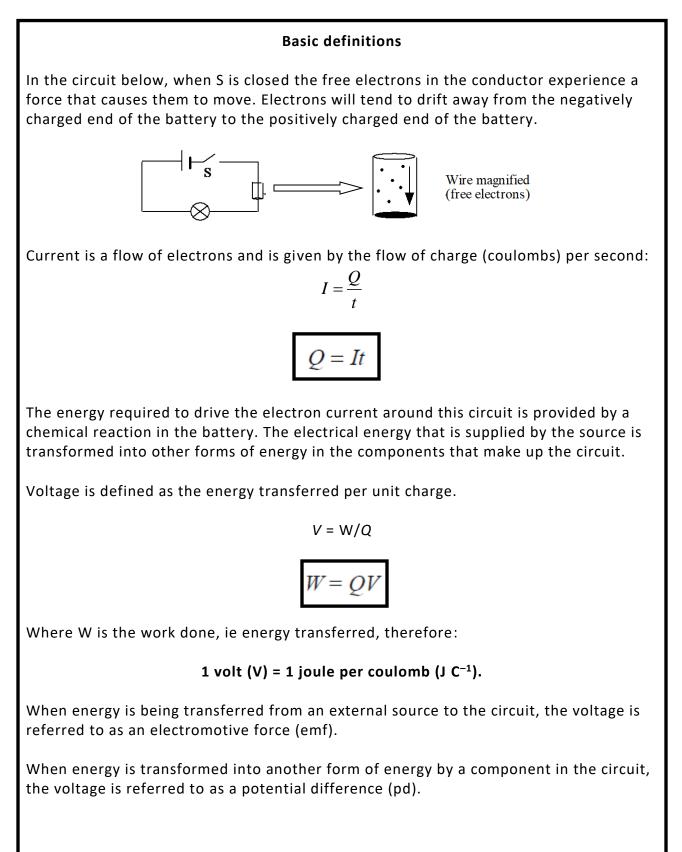
Important notes:

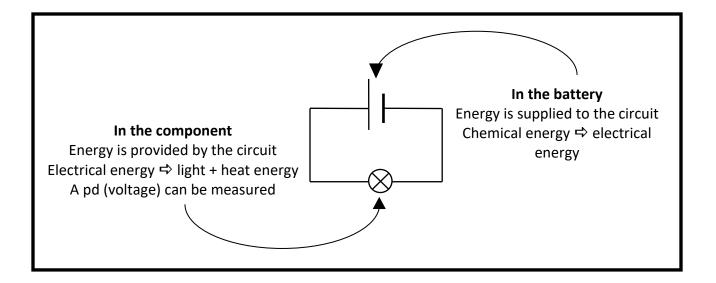
- 1. Readings on meters that measure a.c. are rms values, not peak values. e.g. a multimeter switched to a.c. mode will display rms values.
- 2. For power calculations involving a.c. always use rms values:

$$P = I_{\rm rms} V_{\rm rms} = I_{\rm rms}^2 R = \frac{V_{\rm rms}^2}{R}$$

 The mains supply is usually quoted as 230 V a.c. This is of course 230 V rms. The peak voltage rises to approximately 325 V. This voltage is dangerous, therefore electrical insulation must be provided to withstand this peak voltage.

Current, voltage, power and resistance





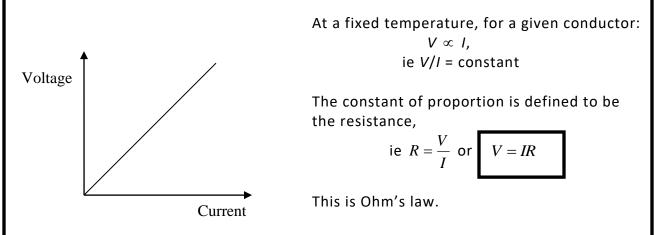
Sources of emf

Emfs can be generated in a great variety of ways. See the table below for examples.

Chemical cell	Chemical energy drives the current (eg battery)
Thermocouple	Heat energy drives the current (eg temperature sensor in an oven)
Piezo-electric generator	Mechanical vibrations drive the current (eg acoustic guitar pickup)
Solar cell	Light energy drives the current (eg solar panels on a house)
Electromagnetic generator	Changes in magnetic field drive the current (eg power stations)

Ohm's law

In any circuit, providing the resistance of a component remains constant, if the potential difference V across the component increases, the current I through the component will increase in direct proportion.



A component that has a constant resistance when the current through it is increased is said to be ohmic.

Some components do not have a constant resistance; their resistance changes as the pd across the component is altered, for example a light bulb, a transistor or a diode. These are said to be non-ohmic.

A graph of *V* versus *I* for such components will not be a straight line.

Circuit rules

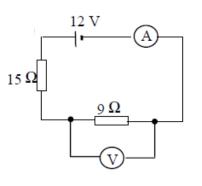
You must be able to apply the circuit rules that you learned last year to series and parallel circuits, both alone and in combination. The circuit rules are summarized in the table below:

	Series	Parallel
Current	$I_{\rm S} = I_1 = I_2 = I_3$	$I_S = I_1 + I_2 + I_3$
Voltage	$V_{\rm S} = V_1 + V_2 + V_3$	$V_S = V_1 = V_2 = V_3$
Resistance	$R_T = R_1 + R_2 + R_3$	$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$

where V_S = supply voltage, I_S = current from the supply and R_T = total resistance

Examples:

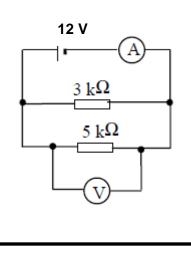
1. Find the readings on the meters in the following circuit.



Solution:

Step 1:	Calculate the total resistance in the circuit $R_T = R_1 + R_2 = 15 + 9 = \frac{24 \Omega}{2}$
Step 2:	Calculate current <i>I = V / R = 12/24 = <u>0.5 A</u></i>
Step 3:	Calculate the voltage across the 9 Ω resistor <i>V = IR = 0.5 x 9 = <u>4.5 V</u></i>

2. Find the readings on the meters in the following circuit.



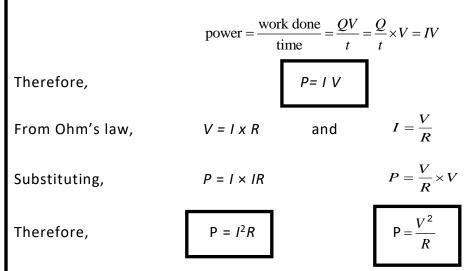
Solution:

Step 1:	Calculate the total resistance in the circuit.
	$1/R_T = 1/R_1 + 1/R_2 = 1/3 + 1/5 = 8/15$
	R _T = <u>1.9 Ω</u>

- Step 2: Calculate current. I = V / R = 12/1.9 = 6.3 A
- Step 3: Voltage across each branch is equal to the supply voltage so V = 12 V

Electric power

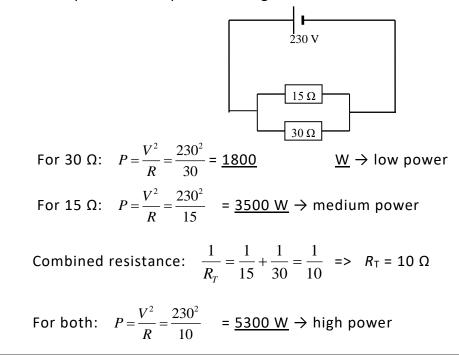
The power is defined as the electrical energy transferred in one second:



The expression I^2R gives the energy transferred in one second due to resistive heating. Apart from obvious uses in electric fires, cookers, toasters etc, consideration has to be given to heating effects in resistors, transistors and integrated circuits, and care taken not to exceed the maximum ratings for such components.

The expression V^2/R is particularly useful when the voltage of a power supply is fixed and you are considering changes in resistance, eg different power of heating elements.

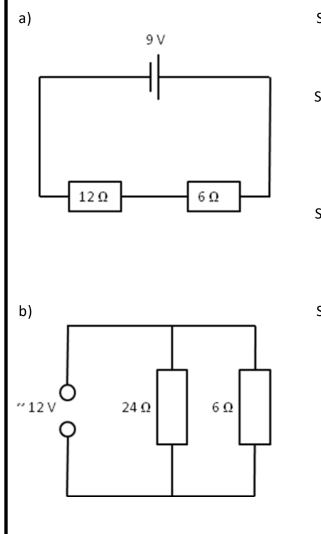
Example: An electric heater has two heating elements allowing three settings: low, medium and high. Show by calculation which element(s) would be switched on to provide each power setting.



Addition of power

By conservation of energy, the total power used in both series and parallel circuits is the sum of the power used in each component.

Example: Calculate the total power dissipated in each of the following circuits



Step 1: Calculate the total current in circuit

 $I = V_S / R_T = 9 / 18 = 0.5 A$

Step 2: Calculate power in each resistor

 $P_1 = I^2 R = 0.5^2 \times 12 = \underline{3 \ W}$

$$P_2 = I^2 R = 0.5^2 \times 6 = 1.5 W$$

Step 3: Calculate total power

 $P_T = P_1 + P_2 = 3 + 1.5 = 4.5 W$

Step 1: Calculate power in each resistor

 $P_1 = V^2/R = 12^2/24 = 6 W$

 $P_2 = V^2/R = 12^2/6 = 24 W$

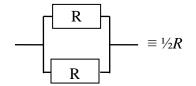
Step 2: Calculate total power

 $P_T = P_1 + P_2 = 6 + 24 = 30 W$

Identical resistors in parallel

Two resistors of the same value (R) wired in parallel:

 $R_{\rm P}$ = half the value of one of them (½R).



Examples: 2 × 1000 Ω in parallel, R_T = 500 Ω 2 × 250 Ω in parallel, R_T = 125 Ω

Voltage and current by proportion

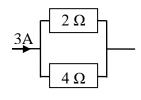
The voltage across an individual resistor in a **series** circuit is proportional to the resistance.

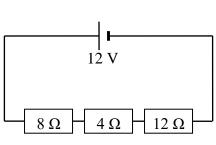
The current through one of two resistors in **parallel** is inversely proportional to the resistance, ie proportional to the other resistance.

Consider the following examples:

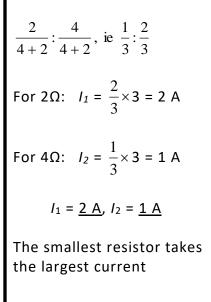
(i) Current in parallel

(ii) Voltage in series





3A will split in the ratio:

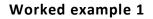


$$R_{\rm S} = 8 + 4 + 12 = 24 \ \Omega$$

For 8
$$\Omega$$
: $V_1 = \frac{8}{24} \times 12 = 4$ V

For 4
$$\Omega$$
: $V_2 = \frac{4}{24} \times 12 = 2$ V

For 12
$$\Omega$$
: $V_3 = \frac{12}{24} \times 12 = 6 \text{ V}$

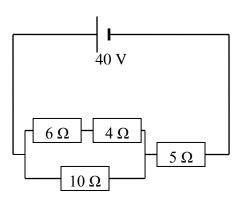


In the circuit shown opposite calculate:

- (a) the current in each resistor
- (b) the pd across each resistor
- (c) the power dissipated in each resistor.

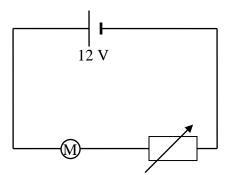
Solution

(a) $R_s = R_1 + R_2 = 4 + 6 = 10 \Omega$ $\frac{1}{R_{\rm p}} = \frac{1}{10} + \frac{1}{10} = \frac{1}{5}$ $R_{\rm P} = 5 \Omega$ $R_{\rm T} = 5 + 5 = 10 \ \Omega$ $I_{\rm T} = \frac{V_{\rm T}}{R_{\rm T}} = \frac{40}{10} = 4$ A (current through 5 Ω) I_1 meets a resistance of 10 Ω and so does I_2 . so $I_1 = I_2 = 2 A$ (b) For the 5 Ω resistor: $V = IR = 4 \times 5 = 20 V$ for the 4 Ω resistor: $V = IR = 2 \times 4 = \underline{8}V$ for the 6 Ω resistor: $V = IR = 2 \times 6 = \frac{12 \text{ V}}{12 \text{ V}}$ for the 10 Ω resistor: $V = IR = 2 \times 10 = 20 V$ (c) For 5 Ω : *P* = *IV* = 4 × 20 = <u>80 W</u> for 4 Ω : $P = I^2 R = 2^2 \times 4 = 16$ W for 6 Ω : $P = \frac{V^2}{R} = \frac{12^2}{6} = \frac{24}{6}$ W for 10 Ω : *P* = *IV* = 2 × 20 = 40 W



Worked example 2

A 10 W model car motor operates on a 12 V supply. In order to adjust the speed of the car it is connected in series with a controller (rheostat).



The controller is adjusted to reduce the motor's power to 4 W.

Assuming that the resistance of the motor does not change, calculate:

- (a) the resistance of the controller at this setting
- (b) the power wasted in the controller.

<u>Solution</u>

(a) We cannot find the resistance of the controller directly. We need to find the resistance of the motor and the total resistance of the circuit when the motor is operating at 10 W.

At 10 W, the full 12 V acts across the motor. The voltage across the rheostat is 0 V (i.e. the rheostat is set to zero Ohms)

For the motor at 10 W, P = 10 W, V = 12 V

$$P = \frac{V^2}{R}$$
, so $R = \frac{V^2}{P} = \frac{12^2}{10}$

 $R = 14.4 \ \Omega$

For the motor at 4 W, $P = I^2 R$, so I = $\sqrt{\frac{P}{R}} = \sqrt{\frac{4}{14 \cdot 4}} = 0.527 \text{ A}$

For the whole circuit: $R_T = \frac{V_T}{I} = \frac{12}{0.527} = 22.8 \ \Omega$

Resistance of controller = $22.8 - 14.4 = 8.4 \Omega$

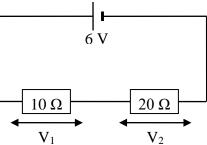
(b) Power in controller = $I^2 R = 0.527^2 \times 8.4$

= <u>2.3 W</u>

The potential divider

A potential divider provides a convenient way of obtaining a variable voltage from a fixed voltage supply.

Consider first two fixed resistors, $R_1 = 10 \Omega$ and $R_2 = 20 \Omega$, connected in series across a 6 V supply:



The voltage across each resistor can be calculated in two steps using Ohm's law:

Step 1 - Calculate the current in the circuit

$$R_T = 10 + 20 = 30 \ \Omega$$

$$I = \frac{V_s}{R} = \frac{6}{30} = 0.2 \text{ A}$$

Step 2 – Use the current in the circuit to calculate the voltage across each resistor

The voltage across R_1 : $V_1 = IR_1 = 0.2 \times 10 = 2 V$

The voltage across R₂: $V_2 = IR_2 = 0.2 \times 20 = 4 \text{ V}$

If you look closely you can see that the voltages across the resistors are in the ratio of their resistances (1:2 in this case). This is expressed in the following relationship:

$$\frac{V_1}{V_2} = \frac{R_1}{R_2}$$

Alternatively, the voltage across reach resistor can be calculated using the potential divider rule:

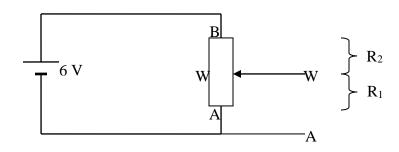
The voltage across R_1 is given by: Similarly, the voltage across R_2 is given by:

$$V_1 = \frac{R_1}{R_1 + R_2} \times V_{\rm S}$$

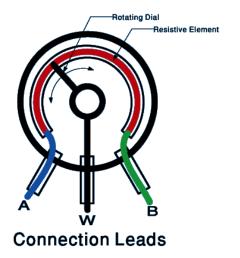
$$V_2 = \frac{R_2}{R_1 + R_2} \times V_S$$

Variable resistors

A variable resistor provides another way of changing the ratio R_1/R_2 . In the circuit diagram below, the resistance between A and W represents R_1 while the resistance between W and B represents R_2 .

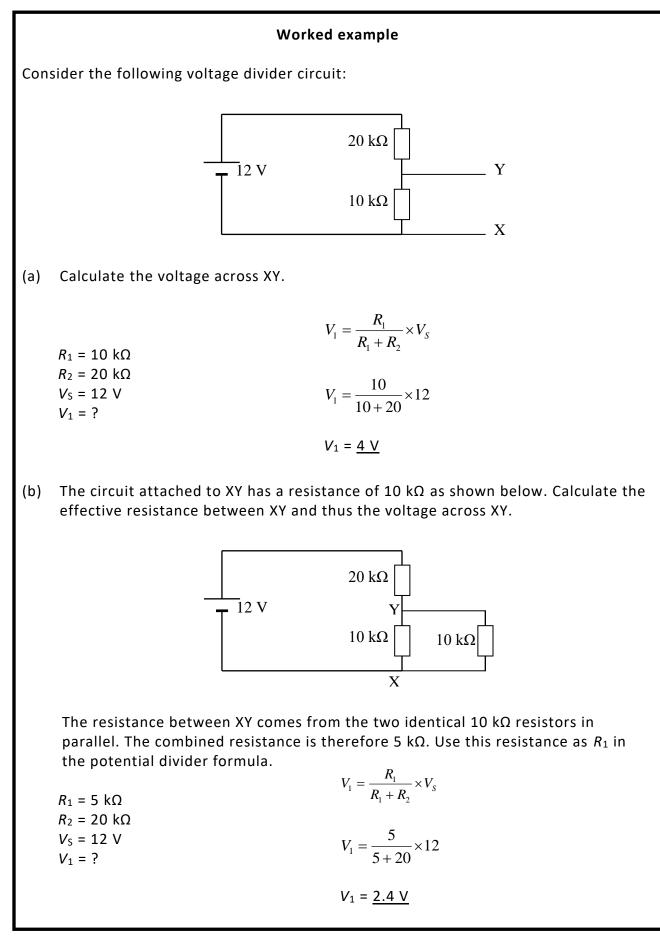


A **potentiometer** is a type of variable resistor. It has two terminals A and B connected by a length of resistance wire. A third terminal W, known as the wiper (or slider), can be rotated to touch the resistance wire anywhere along its length. In this way, the size of the resistance between terminals A and W or between W and B can be varied. The greater the length of resistance wire, the greater the resistance and vice versa.



If a 6 V supply is connected across terminals A and B, a variable voltage of 0 V to 6 V is available between A and W as the wiper is rotated. For example, the output voltage between A and W will be 0 V when the wiper is set at A, 3 V when the wiper is halfway round the track and 6 V when the wiper is at B.

Note that the above only holds true as long as the load connected across A and W has a very high resistance. If it has a resistance comparable with that of A - W the situation becomes more complicated. The effective resistance at the output must then be calculated before the potential divider rule is applied.



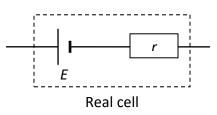
Internal resistance

Up until now, it has been assumed that power supplies are ideal. This means that their voltage remains constant and they can supply any current as long as they are connected to the correct resistance.

However, when a battery is part of a closed circuit, it must itself be a conductor. Since all conductors have a resistance, some of the electrical energy from the supply must be converted to heat energy and will be lost to the circuit. The greater the current flowing in the circuit, the more heat that is dissipated in the power supply and the less energy that is available to the circuit.

As the battery has a resistance of its own, we say that it has an **internal resistance**, **r**. Energy will be used up in overcoming the internal resistance of the supply (this energy appears as heat) and so the energy per unit charge available at the output of the battery (the **terminal potential difference** or **tpd**) will fall. There will be '**lost volts'**. The lost volts = *Ir*.

A real power supply or battery can be thought of as having two parts, a source of electrical energy (E) and an internal resistor (r). This is represented by the following circuit diagram:



Therefore, a circuit can be thought of as a source of energy, an internal resistance (r) and an external resistance (R). The external resistance could be made up of a number of separate resistances.

Real power supply – One with an internal resistance

Ideal power supply - One with no internal resistance

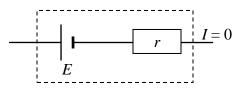
Emf, tpd and 'lost volts'

1. Open circuit (*I* = 0)

Firstly, it would be very useful to know the voltage of the ideal cell. This is called the emf (electromotive force) of the cell, which was defined previously as the **energy supplied to each coulomb of charge passing through the supply**.

The emf is found by measuring the voltage across the cell in an 'open circuit'. This can be done by connecting a voltmeter or oscilloscope across the supply when there is **no current flowing**.

To understand this, consider the diagram below:



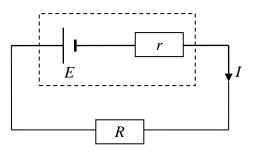
From Ohm's Law, V across $r = l \times r$ Since l = 0V across $r = 0 \times r = 0$ V

So no voltage is dropped across the internal resistance and a voltmeter across the real cell would register the voltage of the ideal cell, the emf.

2. Under load

When a real cell is delivering current in a circuit, the external resistance is referred to as the load resistance.

If Ohm's law is applied to a circuit containing a battery of emf E and internal resistance r with an external load resistance R:



If I is the current in the circuit and V is the pd across R (the tpd.), then from conservation of energy:

$$E = V \operatorname{across} R + V \operatorname{across} r$$
$$\underline{E} = V + Ir$$

This is known as the internal resistance equation The internal resistance equation can clearly be rearranged into different forms, for example:

E = V + Ir or V = E - Ir

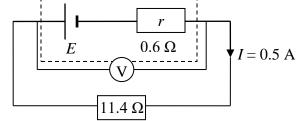
since V = IR,

E = IR + Ir or E = I(R + r)

Consider the case of a cell with an internal resistance of 0.6 Ω delivering current to an external resistance of 11.4 Ω :

Cell emf. = 6 V

Current = 0.5 A



The voltage measured across the terminals of the cell will be the voltage across the 11.4 Ω resistor:

$$V = IR = 0.5 \times 11.4$$

and the voltage across the internal resistance:

The voltage across the terminals is known as the terminal potential difference or tpd. This is only 5.7 V because of the 0.3 V voltage dropped across the internal resistance of the cell. This is called the lost volts.

3. Short circuit (R = 0)

The maximum current is the short-circuit current. This is the current that will flow when the terminals of the supply are joined with a short piece of thick wire (ie there is no external resistance).

By substituting R = 0 in the above equation we get:

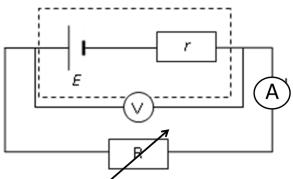
E = I(0 + r)

<u>E = Ir</u>

Experiments to measure EMF and Internal Resistance

First graphical method

When we increase the current in a circuit like the one shown below, the energy lost in the supply due to heating will increase. Therefore, the 'lost volts' will increase and the tpd will decrease.



Starting with a low resistance, take reading from voltmeter and ammeter. Then increase resistance and take a further set of readings from voltmeter and ammeter. Repeat this until several sets of readings have been obtained.

If we plot a graph of **V** on the y-axis against *I* on the x-axis, we get a straight line of negative gradient. We can use this graph to determine the emf and internal resistance:

From the internal resistance equation,

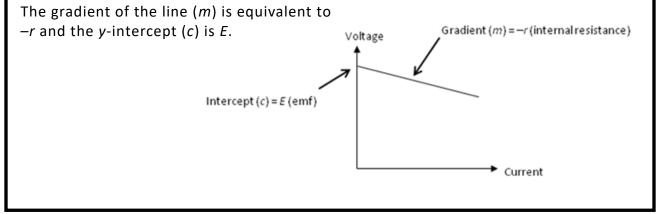
V = E - Ir

Re-arranging,

$$V = (-r) \times I + E$$

Comparing this with the equation of a straight line,

y = mx + c



Second graphical method

When we increase the external resistance (*R*) in a circuit, there will be a decrease in the current flowing. Starting with a low resistance, take reading from ammeter. Then increase resistance and take a further readings from ammeter. Repeat this until several sets of readings have been obtained. If we plot a graph of *R* on the *y*-axis against 1/*I* on the *x*-axis, we get a straight line of positive gradient and negative intercept.

From the internal resistance equation:

$$E = IR + Ir$$

Divide both sides by *I*:

Re-arranging

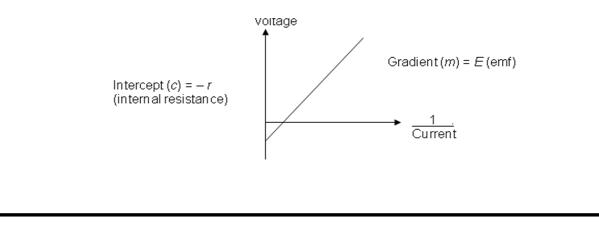
 $R = (E \times 1/I) - r$

E/I = R + r

Comparing this with the equation of a straight line:

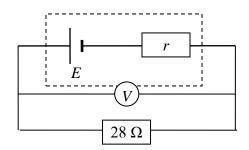
$$y = mx + c$$

The gradient of the line (m) is equivalent to E and the y-intercept (c) is -r.



Worked example

A cell of emf 1.5 V is connected in series with a 28 Ω resistor. A voltmeter measures the voltage across the cell as 1.4 V.



Calculate:

- (a) the internal resistance of the cell
- (b) the current if the cell terminals are short circuited
- (c) the lost volts if the external resistance R is increased to 58 Ω .

Solution:

(a) E = V + Ir

In this case we do not know the current, *I*, but we do know that the voltage across the 28 Ω resistor is 1.4 V, and *I* = V/R, so *I* = 0.05 A.

$$1.5 = 1.4 + 0.05r$$

$$r = \frac{0.1}{0.05} = 2 \Omega$$

(b) Short circuit:

Total resistance= 2 Ω

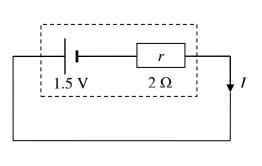
$$I = \frac{E}{r} = \frac{1.5}{2} = 0.75 \text{ A}$$

(c) E = I(R + r)

1.5= /(58 + 2)

I = 1.5<u>/60</u> = <u>0.025 A</u>

lost volts = $Ir = 0.025 \times 2 = 0.05 \text{ V}$

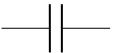


Capacitors

Capacitance

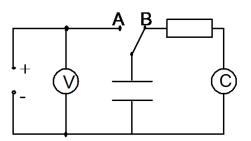
Capacitance is the ability (or capacity) of a component to store charge. A device that stores charge is called a **capacitor**.

Practical capacitors consist of two conducting layers separated by an insulator. The simplest type is two metal plates with an air gap between them. The circuit symbol for a capacitor is based on this:

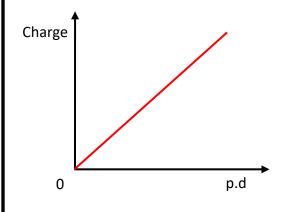


Relationship between charge and pd

A capacitor is charged to a chosen voltage by setting the switch to A. The charge stored can be measured directly by discharging through the coulomb meter by moving the switch to B.



In this way pairs of readings of voltage and charge are obtained. When a graph of charge stored on the capacitor is plotted against the pd (voltage), it is found that the charge is directly proportional to the pd (voltage) across it:



From the graph:

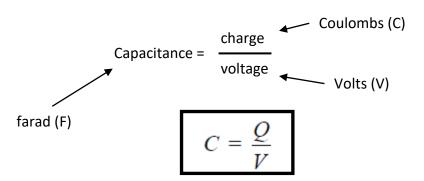
V = a constant

This constant is defined as the capacitance, C:

$$C = \frac{Q}{V}$$
 or $Q = CV$

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Notice that this means that capacitance is the *gradient* of the above graph. For any capacitor, the ration Q/V is a constant and is called the capacitance



Therefore, the formal definition of capacitance is the charge stored per unit voltage.

The unit of capacitance is the farad (F).

From the above formula: 1 farad = 1 coulomb per volt.

The farad is too large a unit for practical purposes and the following submultiples are used:

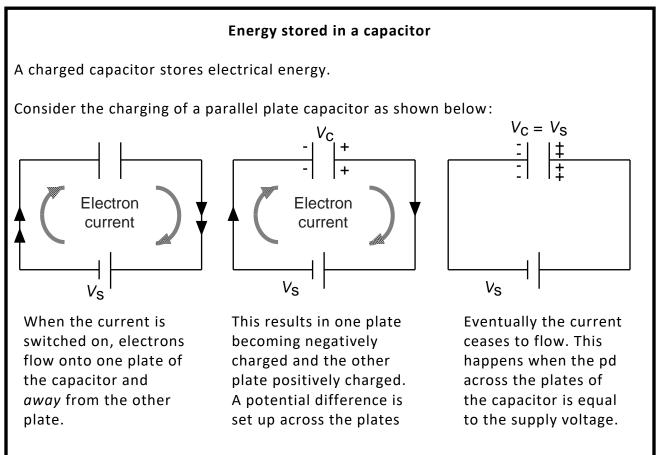
1 mF (microfarad) = 1 \times 10⁻⁶ F and 1 nF (nanofarad) = 1 \times 10⁻⁹ F

Note: When a capacitor is charging and there is a constant charging current then the equation Q=It can be used. If the current is not constant this equation cannot be used.

Example: A capacitor stores 4×10^{-4} C of charge when the potential difference across it is 100 V. Calculate the capacitance.

If the charging current is constant then the following formula can be used to work out the charging time

$$Q = It$$



When charging a capacitor, the negatively charged plate will tend to repel the electrons approaching it.

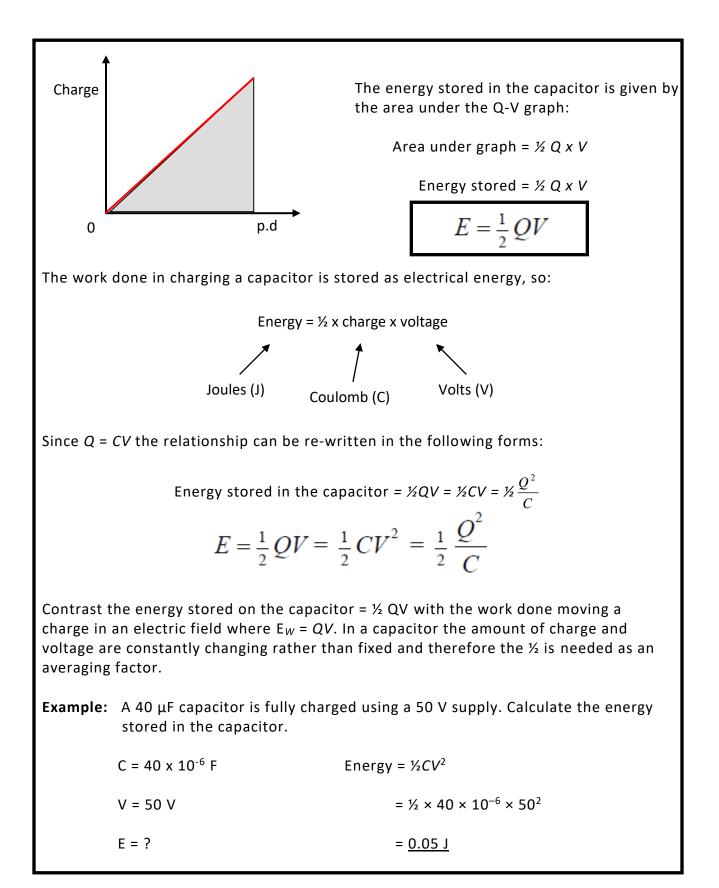
In order to overcome this repulsion work has to be done in charging the capacitor. This energy is supplied by the battery.

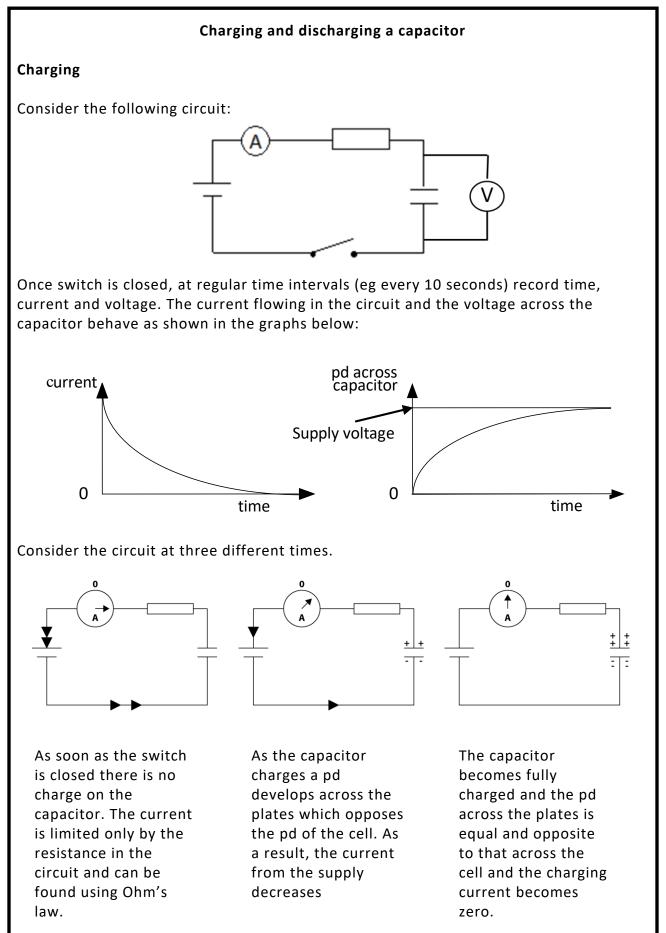
Note that current does not flow through the capacitor, electrons flow *onto* one plate and *away from* the other plate.

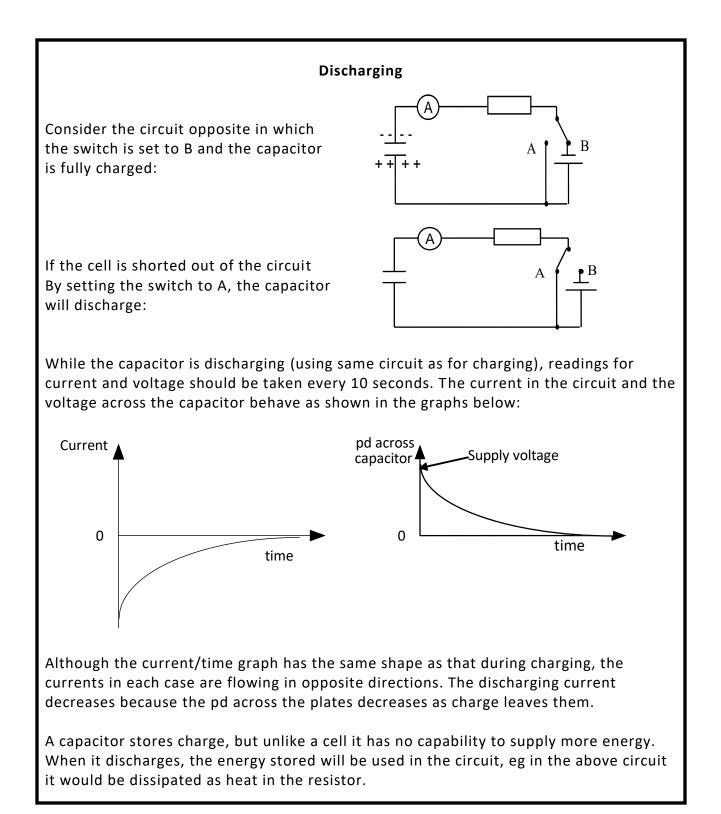
For a given capacitor the pd across the plates is directly proportional to the charge stored.

Consider a capacitor being charged to a pd of V and holding a charge Q.

The work done is stored as energy in the capacitor.







Factors affecting the rate of charge and discharge

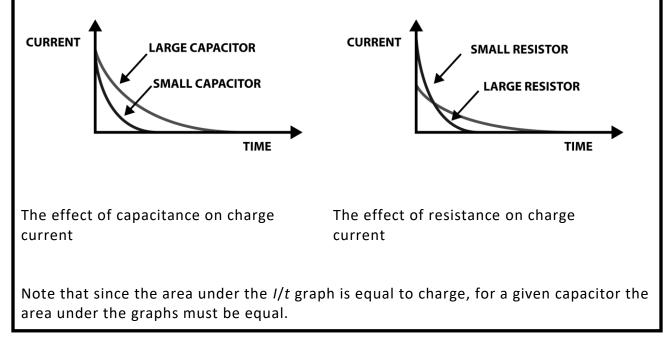
The time taken for a capacitor to charge is controlled by the resistance of the resistor *R* (because it controls the size of the current, ie the charge flow rate) and the capacitance of the capacitor (since a larger capacitor will take longer to fill and empty).

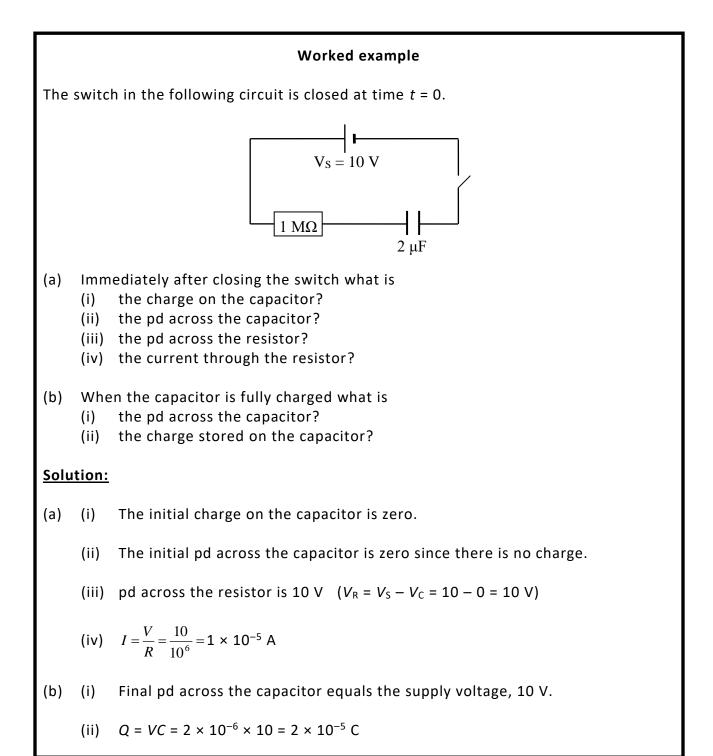
As an analogy, consider charging a capacitor is like filling a jug with water. The size of the jug is like the capacitance and the resistor is like the tap you use to control the rate of flow.

The values of R and C can be multiplied together to form what is known as the time constant. Can you prove that $R \times C$ has units of time, seconds? The time taken for the capacitor to charge or discharge is related to the time constant.

Large capacitance and large resistance both increase the charge or discharge time.

The I/t graphs for capacitors of different value during charging are shown below:

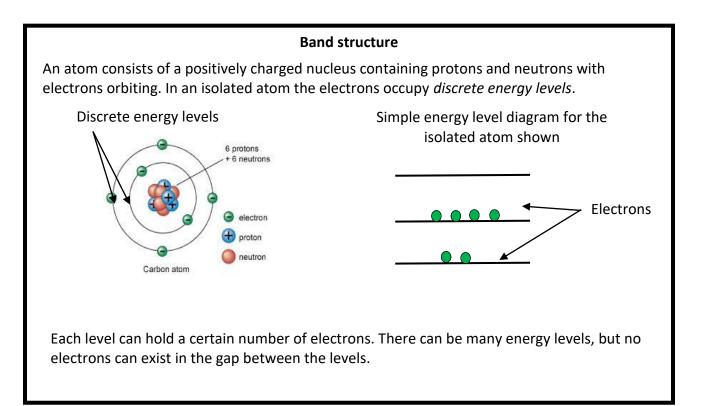




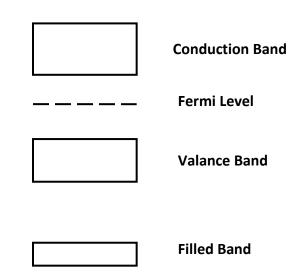
3.2 Electrons at Work

Conductors, Semi conductors and Insulators

	ical properties of materials, we can divide them into three groups:
Material	Electrical properties
Conductor	Materials with many free electrons. These electrons can easily be made to flow through the material.
	Examples: all metals, semi-metals like carbon- graphite, antimony and arsenic.
Insulator	Materials that have very few free electrons.
	Examples: plastic, glass and wood.
Semi -conductor	Materials that behave like insulators when pure, but will conduct when an impurity is added and/ or in response to light, heat, voltage etc.
	Examples: Elements: silicon, germanium, selenium
	Compounds: gallium arsenide and indium antimonide.



When atoms are close to each other the electrons can use the energy levels of their neighbours. However, when the atoms are arranged in a crystalline lattice of a solid, the electrons in adjacent atoms cannot occupy the same energy levels, so the energy levels of the isolated atoms are split into many levels of slightly different energy. These energy levels are so closely spaced that they form a continuous band of permitted energy levels. Thus, in a solid, the electrons occupy a continuous range of allowed energy levels rather than a single level for an isolated atom.



There will also be a group of energy level that are not allowed. These occur between the bands in what is known as the *band gap*.

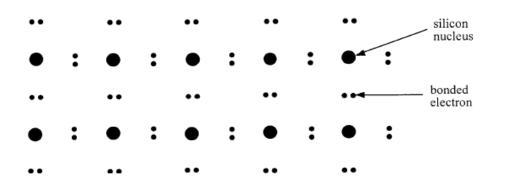
Similar to the energy levels of an individual atom, the electrons in a solid will fill the lower bands first. The Fermi level gives a rough idea of the energy level which electrons will generally fill up to, but there will always be some electrons with individual energies above this.

Elect	trical conduction in conductors, insulators and semiconductors	
Band theory allows us to understand the electrical properties of conductors, insulators and emiconductors.		
	Electron Energy Conduction band Conduction band Conduction band Conduction band Band Fermi level Band Gap Valence Band	
Material	Band Structure Conductor Semiconductor Insulator	
Conductor	In a conductor the highest occupied energy band is only partially filled. This is known as the Conduction Band. There are many empty energy levels available close to the occupied levels for the electrons to move into. Therefore, electrons can flow easily from one atom to another when a potential difference is applied. Some metals have overlapping conduction and valance bands which makes them highly conductive.	
Insulator	In an insulator, the highest occupied band is completely full of electrons. This is known as the valance band. There are no electrons in the band above this, i.e. the conduction band. There is a large gap between the bands called the <i>band gap</i> . The band gap is so large that electrons almost never cross it and the solid never conducts. If we supply enough energy the solid will conduct but often the large amount of energy needed ends up destroying the solid.	
Semiconductor	Semiconductors are like insulators in that the highest occupied band is completely full, i.e. the valence band. However, the gap between the two bands is small and at room temperature some electrons have enough energy to jump the gap. At warm temperatures the solid will conduct to a small extent. As the temperature increases, the number of electrons in the conduction band	
	increases and so the semiconductor conducts better.	

Bonding in Semiconductors

Intrinsic semiconductors

The most commonly used semiconductors are silicon and germanium. Both these materials have a *valency of four* (they have four outer electrons available for bonding). In a pure crystal, each atom is bonded covalently to another four atoms. All of its outer electrons are bonded and therefore there are few free electrons available to conduct. These semiconductors have a very large resistance.



Imperfections in the crystal lattice and thermal ionisation due to heating can cause a few electrons to become free. A higher temperature will result in more free electrons, increasing conductivity and thus decreasing the resistance e.g. as in a thermistor.

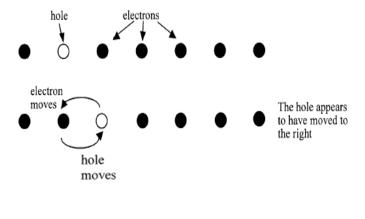
Holes

When an electron leaves its position in the crystal lattice, there is a space left behind that is positively charged. This lack of an electron is called a *positive hole*.

This hole may be filled by an electron from a neighbouring atom, which will in turn leave a hole there. Although it is technically the electron that moves, the effect is the same as if it was the hole that moved through the crystal lattice. The hole can then be thought of as a positive charge carrier.

In an intrinsic (undoped) semiconductor, the number of holes is equal to the number of electrons.

The generally small currents consist of drifting electrons in one direction and holes in the other.



p – n junctions

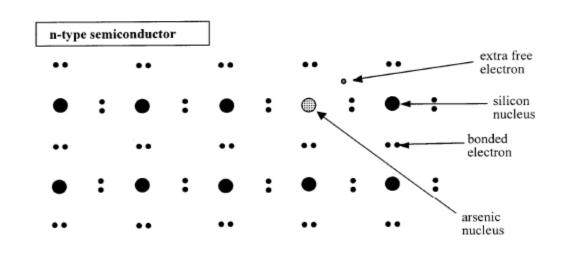
Doping

The electrical properties of semiconductors make them very important in electronic devices such as transistors, diodes and light dependant resistors (LDRs).

Doping is the addition of a very small amount of impurity e.g. arsenic, to a pure semiconductor. This action dramatically changes the electrical properties of a material, i.e. **allows a semiconductor to conduct**. Once doped these materials are known as *extrinsic semiconductors*.

n -type semiconductors

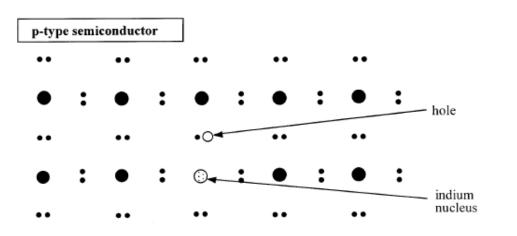
If an impurity such as arsenic (As), which has five outer electrons, is present in the crystal lattice, then four of its electrons will be used in bonding with the silicon. The fifth will be free to move about and conduct. Since the ability of the crystal to conduct is increased, the resistance of the semiconductor is therefore reduced.



This type of semiconductor is called *n*-type, since most conduction is by the movement of free electrons, which are negatively charged.

p -type semiconductors

A semiconductor may also be doped with an element like indium (In), which has only three outer electrons. This produces a hole in the crystal lattice, where an electron is 'missing'.



An electron from the next atom can move into the hole created as described previously. Conduction can thus take place by the movement of positive holes. This is called a *p*-type semiconductor, as most conduction takes place by the movement of positively charged 'holes'.

Additional notes on doping

To dope a material the impurity can be grown into the crystal's lattice, in order that it becomes part of the atomic lattice. Alternatively, the impurity can be added later by a process called indiffusion at higher temperatures.

The quantity of impure atoms added is extremely small when compared with the number of atoms in the whole lattice.

p-type and n-type semiconductors remain **overall neutral** (just as a metal can conduct but is normally neutral).

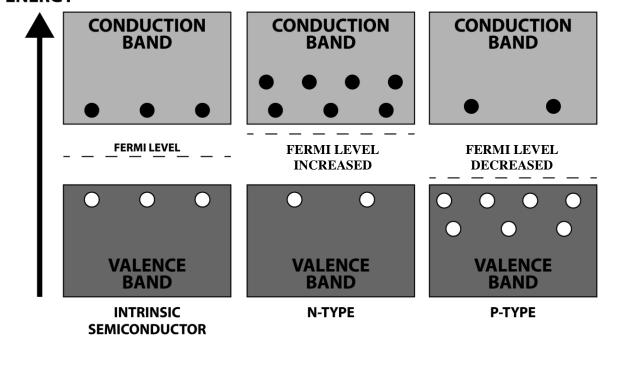
Each type of semiconductor will still have small amounts of additional free electrons due to thermal ionisation.

How doping affects Band Structure

In terms of band structure, we can represent the electrons as dots in the conduction band, and holes as circles in the valance band, as shown in the diagram below.

The diagram also illustrates how the additional energy levels produced by the addition of the impure atoms changes the **Fermi level** (the top of the collection of electron energy levels at absolute zero) and make it easier for electrons to move up to the conduction band in n-type semiconductors and for holes to be created in the valance band of the p-type.

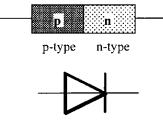
ELECTRON ENERGY



n –type semiconductor: extra electrons present, the Fermi level is closer to the conduction band. p – type semiconductor: fewer electrons present.

p –n junctions

When a semiconductor is grown so that one half is p-type and the other half is n-type, the product is called a p-n junction and it functions as a diode. There is an electric field in the p-n junction.



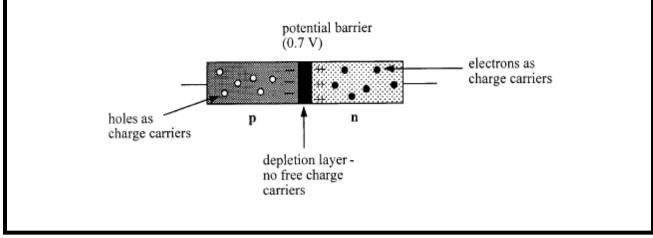
circuit symbol

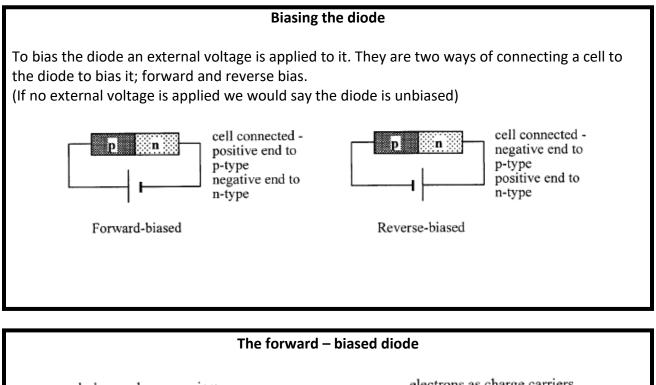
At temperatures above absolute zero, the electrons in the n-type material and the holes in the ptype material will constantly diffuse. The charge carriers near the junction will be able to diffuse across it in opposite directions. (Diffusion is the spread of any particles through random motion from high concentration regions to low concentration regions)

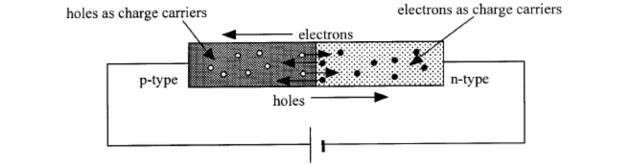
Some of the free electrons from the n- type material diffuse across the junction and fill some of the holes in the p- type material. This can also be thought of as holes moving in the opposite direction to be filled with electrons.

Since the n-type has lost electrons, it becomes positively charged near the junction. The p-type having gained electrons becomes negatively charged.

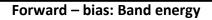
There will be a small voltage, a potential barrier (about 0.7V in silicon), across the junction due to this charge separation. This voltage will tend to oppose any further movement of charge. The region around the junction has lost virtually all its free charge carriers. This region is called the *depletion layer*.



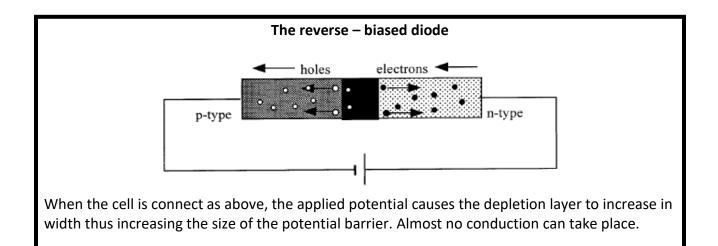




When the cell is connect as above, the electrons from the n-type will be given enough energy from the battery to overcome the depletion layer p.d (the potential barrier) and flow through the junction and round the circuit in an anti-clockwise direction. This movement will result in a similar movement of holes in the clockwise direction. The diode conducts because the depletion layer has been removed.

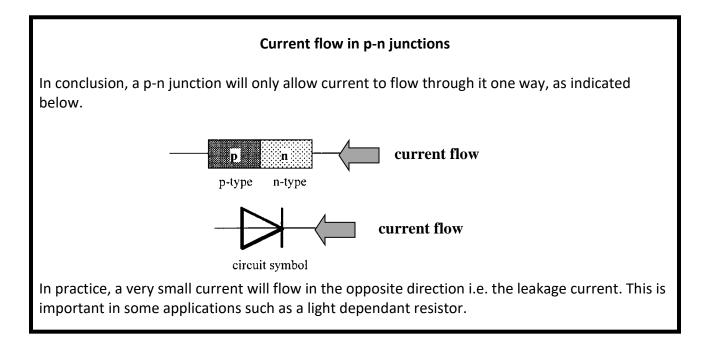


Applying forward bias has the effect of lowering the bands on the p-side from where they were originally. This reduces the electric field in the p-n junction. As the applied voltage approaches the built in voltage, more electrons will have sufficient energy to flow up the now smaller barrier and an appreciable current will be detected. Once the applied voltage reaches the in-built voltage there is no potential barrier and the p-n junction presents almost no resistance, like a conductor. The holes are similarly able to flow in the opposite direction across the junction towards the negative side of the battery.



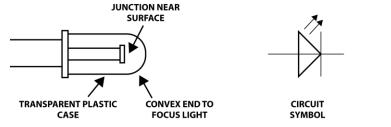
Reverse – bias: Band energy

Applying a reverse bias has the effect of raising the bands on the p-side from where they were originally. This increases the electric field in the p-n junction. Almost no conduction can take place since the battery is trying to make electrons flow 'up the slope' of the difference in the conduction bands. The holes face a similar problem in flowing in the opposite direction. The tiny current that does flow is termed reverse **leakage current** and comes from the few electrons which have enough energy from thermal ionisation to make it up the barrier.



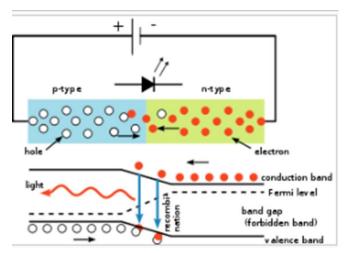
The light emitting diode (LED)

One application of the p-n junction is the LED. An LED consists of a p-n junction diode connected to a positive and negative terminal. The junction is encased in a transparent plastic as shown below.



How does an LED work?

When the p-n junction is connected in forward bias, electrons and holes pass through the junction in opposite directions. The electrons move from the conduction band of the n-type semiconductor towards the conduction band of the p-type semiconductor. Photons are emitted when electrons 'fall' from the conduction band into the valence band either side of the junction.



For each recombination of electron and hole, one photon of radiation is emitted.

Depending on the type of semiconductor used the radiation may be in the form of heat resulting in a temperature increase. However, in some semiconductors such as gallium arsenic phosphide, the energy is emitted as photons of light. The colour of the emitted light depends on the relative amounts of gallium, arsenic and phosphorous used to produce the semiconductor.

The frequency of light from the LED's is controlled by the size of the energy gap between the conduction and valence bands. A bigger gap will result in a larger energy change and a higher frequency of light will be emitted.

The recombination energy can be calculated using $\mathbf{E} = \mathbf{h} \mathbf{f}$, if the frequency is known. [As discussed previously, the diode does not conduct in reverse bias, therefore an LED will not work when connect in reverse bias.]

LED: worked example

An LED emits photons of light with a frequency of 5 x 10^{14} Hz.

Calculate:

- (a) The wavelength of the photons of light.
- (b) What colour of light is emitted by this LED?
- (c) What factor about the construction of the LED determines the colour of the emitted light?

Solution:

(a) $v = f x \lambda$

 $3 \times 10^8 = 5 \times 10^{14} \times \lambda$

λ = 600 nm

- (b) Orange (selected from the data sheet)
- (c) The type of materials used to construct the semiconductor.

The Photodiode

A p-n junction in a transparent coating will react to light due to the *photoelectric effect*.

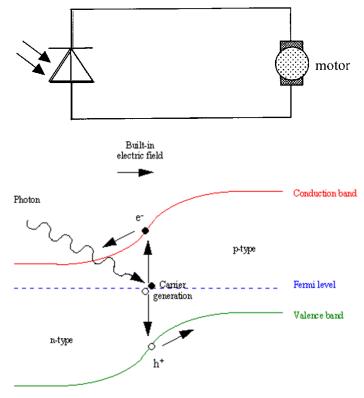


circuit symbol

The photodiode can be used in two modes; *photovoltaic mode* and *photoconductive mode*.

Solar-cell - Photovoltaic Mode

In this mode the diode has no bias voltage applied as shown in the diagram below. The load may be a component other than a motor.



The absorption of photons provides energy to 'raise' electrons from the valence band of the semiconductors to the conduction band. The p-n junction causes the electrons in the conduction band to move towards the n-type semiconductor and a potential difference is produced across the solar cell, a voltage being generated by the separation of the electron and hole.

Using more *intense light* (more photons incident per second) will lead to more electron-hole pairs being produced and therefore a higher voltage will be generated by the diode. The voltage generated is proportional to the light intensity.

In this mode, the photodiode will supply a voltage to the load, e.g. motor. Many photodiode's connected together form the basis of solar cells.

