

SIMULTANEOUS EQUATIONS

We can solve simultaneous equations graphically or algebraically.

GRAPHICALLY

Find the point of intersection between the lines $y = x + 1$ and $y = -2x + 7$.

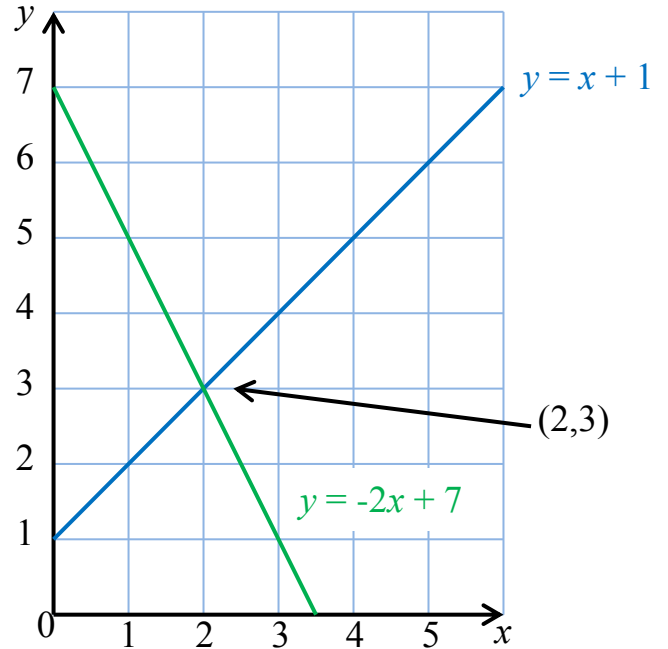
Use a table of values to find points on each line:

$$y = x + 1$$

x	0	1	2	3
y	1	2	3	4

$$y = -2x + 7$$

x	0	1	2	3
y	7	5	3	1



Draw the lines and find the point of intersection.

The point of intersection in this example is (2,3).

ALGEBRAICALLY BY SUBSTITUTION

Solve the equations $y = 3x$ and $y = 2x + 2$ by substitution.

The 1st equation, $y = 3x$, is used to make a substitution into the 2nd equation.

$$y = 2x + 2 \quad \text{Replace the } y \text{ with } 3x \text{ from the 1}^{\text{st}} \text{ equation.}$$

$$3x = 2x + 2 \quad \text{Solve to find } x.$$

$$x = 2 \quad \text{Use either of the original equations to find } y.$$

$$y = 3x = 3 \times 2 = 6$$

The point of intersection is $x = 2, y = 3$

ALGEBRAICALLY BY ELIMINATION

Solve the equations $x + y = 9$ and $x - y = 1$ by elimination.

To solve by elimination we add or subtract the equations to eliminate one of the variables.

$$\begin{array}{r} x + y = 9 \\ \underline{x - y = 1} \quad \text{ADD} \\ 2x \quad = 10 \end{array}$$

So $x = 5$

Substitute into either equation to find y .

$$\begin{array}{r} x + y = 9 \\ 5 + y = 9 \\ y = 4 \end{array}$$

Solve the equations $5x + 2y = 9$ and $2x + 3y = 8$ by elimination.

In this case a variable is not eliminated by adding or subtracting. We must first multiple the equations to give either the same number of x or y terms.

$$\begin{array}{r} 5x + 2y = 9 \quad \text{multiply by 3} \quad 15x + 6y = 27 \\ 2x + 3y = 8 \quad \text{multiply by 2} \quad \underline{4x + 6y = 16} \quad \text{SUBTRACT} \\ 11x \quad = 11 \\ x = 1 \end{array}$$

Substitute into either equation to find y .

$$\begin{array}{r} 5x + 2y = 9 \\ 5 \times 1 + 2y = 9 \\ 2y = 4 \\ y = 2 \end{array}$$

Simultaneous Equations Practice

<http://www.bbc.co.uk/schools/gcsebitesize/maths/algebra/simultaneoushirev1.shtml>

Revise Simultaneous Equations.

http://www.cimt.plymouth.ac.uk/projects/mepres/book9/bk9i5/bk9_5i5.html

Revise Simultaneous Equations.

<http://www.supermathsworld.com/> Ask your teacher for the login details.

Select ALGEBRA from the menu. Select SIMULTANEOUS EQUATIONS. Try on EASY, MEDIUM and HARD level.