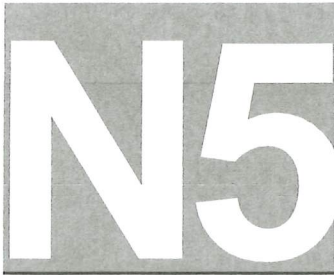


FOR OFFICIAL USE



National Qualifications 2024

Mark

X847/75/01

Mathematics Paper 1 (Non-calculator)

FRIDAY, 3 MAY
9:00 AM – 10:00 AM



Fill in these boxes and read what is printed below.

Full name of centre

Town

WORKED SOLUTIONS

Forename(s)

Surname

Number of seat

Th

Date of birth

Day

Month

Year

Scottish candidate number

Total marks — 40

Attempt ALL questions.

You must NOT use a calculator.

To earn full marks you must show your working in your answers.

State the units for your answer where appropriate.

Write your answers clearly in the spaces provided in this booklet. Additional space for answers is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting.

Use blue or black ink.

Before leaving the examination room you must give this booklet to the Invigilator; if you do not, you may lose all the marks for this paper.



FORMULAE LIST

The roots of $ax^2 + bx + c = 0$ are $x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$

Sine rule $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$ or $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$

Area of a triangle $A = \frac{1}{2}ab \sin C$

Volume of a sphere $V = \frac{4}{3}\pi r^3$

Volume of a cone $V = \frac{1}{3}\pi r^2 h$

Volume of a pyramid $V = \frac{1}{3}Ah$

Standard deviation $s = \sqrt{\frac{\Sigma(x - \bar{x})^2}{n - 1}}$
or $s = \sqrt{\frac{\Sigma x^2 - \frac{(\Sigma x)^2}{n}}{n - 1}}$, where n is the sample size.



* X 8 4 7 7 5 0 1 0 2 *

Total marks — 40
Attempt ALL questions

1. Evaluate $3\frac{2}{3} - 1\frac{1}{4}$.

2

$$3\frac{2}{3} - 1\frac{1}{4}$$

$$2\frac{2}{3} - \frac{1}{4}$$

$$2\frac{8}{12} - \frac{3}{12}$$

$$= \underline{\underline{2\frac{5}{12}}}$$

Alternative method:

$$\frac{11}{3} - \frac{5}{4}$$

$$\frac{44}{12} - \frac{15}{12}$$

$$= \frac{29}{12}$$

2. Given that $f(x) = (x+3)^2$, evaluate $f(7)$.

2

$$f(7) = (7+3)^2$$

$$= 10^2$$

$$\underline{\underline{f(7) = 100}}$$

[Turn over



* X 8 4 7 7 5 0 1 0 3 *

3. Expand and simplify $(x+1)(x^2-4x+5)$.

$$\begin{array}{r|rrr}
 & x^2 & -4x & +5 \\
 \hline
 x & x^3 & -4x^2 & +5x \\
 +1 & +x^2 & -4x & +5
 \end{array}$$

$$= \underline{\underline{x^3 - 3x^2 + x + 5}}$$

4. Given $\mathbf{a} = \begin{pmatrix} 3 \\ 4 \\ -1 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} 5 \\ 3 \\ 2 \end{pmatrix}$, find the resultant vector $3\mathbf{a} + \mathbf{b}$.

Express your answer in component form.

$$\begin{aligned}
 & 3\mathbf{a} + \mathbf{b} \\
 & 3 \begin{pmatrix} 3 \\ 4 \\ -1 \end{pmatrix} + \begin{pmatrix} 5 \\ 3 \\ 2 \end{pmatrix} \\
 & \begin{pmatrix} 9 \\ 12 \\ -3 \end{pmatrix} + \begin{pmatrix} 5 \\ 3 \\ 2 \end{pmatrix} = \underline{\underline{\begin{pmatrix} 14 \\ 15 \\ -1 \end{pmatrix}}}
 \end{aligned}$$



5. The prices, in pounds (£), of the cameras on display in a shop are listed below.

155 Q_1 160 190 | 210 Q_3 230 240
 Q_2

(a) Calculate the median and the interquartile range of these prices.

3

Median, $Q_2 = £200$

$Q_1 = 160$

$IQR = Q_3 - Q_1$

$Q_3 = 230$

$= 230 - 160$

$IQR = £70$

On a website, a sample of camera prices have a median of £195 and an interquartile range of £73.

(b) Make two valid comments comparing the prices of the cameras in the shop and on the website.

2

On average, the camera prices are cheaper on the website, than in the shop.

The camera prices on the website [Turn over] are more variable than they are in the shop.

	median	IQR
Shop	200	70
Website	195	73



6. Simplify $\sqrt{75} - \sqrt{3}$.

2

$$\begin{aligned} & \sqrt{25}\sqrt{3} - \sqrt{3} \\ & 5\sqrt{3} - \sqrt{3} \\ & = \underline{\underline{4\sqrt{3}}} \end{aligned}$$

7. Solve, algebraically, the system of equations

$$2p - 7r = 11 \quad (\times 2)$$

$$3p + 2r = 4 \quad (\times 7)$$

3

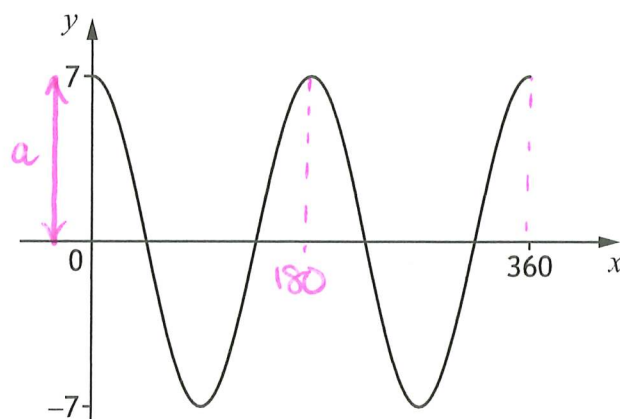
$$\begin{aligned} & 4p - 14r = 22 \\ (+) & 21p + 14r = 28 \\ \hline & 25p = 50 \\ & p = 2 \end{aligned}$$

$$\begin{aligned} & 3p + 2r = 4 \\ & 3(2) + 2r = 4 \\ & 6 + 2r = 4 \\ & 2r = -2 \\ & r = -1. \end{aligned}$$

Solution: $p=2$ and $r=-1$



8. The graph of $y = a \cos bx^\circ$, $0 \leq x \leq 360$, is shown.



(a) State the value of a .

1

$$\underline{\underline{a = 7}}$$

(b) State the value of b .

1

2 cosine waves in 360°

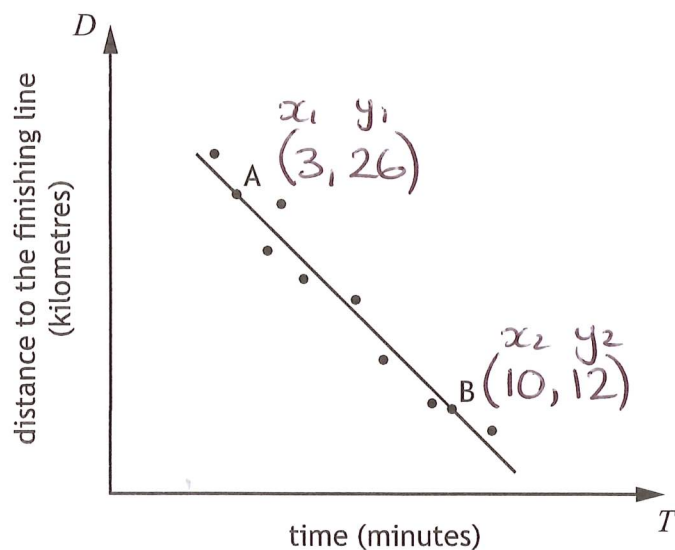
$$\therefore \underline{\underline{b = 2}}$$

[Turn over



9. In a car rally, competitors start at different times.

The scattergraph shows the relationship between the length of time they have been driving, T minutes, and the distance to the finishing line, D kilometres.



A line of best fit has been drawn.

Point A represents a competitor who has been driving for 3 minutes and is 26 kilometres from the finishing line.

Point B represents a competitor who has been driving for 10 minutes and is 12 kilometres from the finishing line.

- (a) Find the equation of the line of best fit in terms of D and T .

Give the equation in its simplest form.

3

Gradient

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{12 - 26}{10 - 3}$$

$$m = -\frac{14}{7}$$

$$m = -2$$

Equation of line

$$y - b = m(x - a)$$

$$y - 12 = -2(x - 10)$$

$$y - 12 = -2x + 20$$

$$y = -2x + 32$$

$$\hookrightarrow \underline{\underline{D = -2T + 32}}$$



9. (continued)

Another competitor has been driving for 7 minutes.

- (b) Use your equation from part (a) to estimate the distance the competitor is from the finishing line.

1

$$\text{Let } T = 7$$

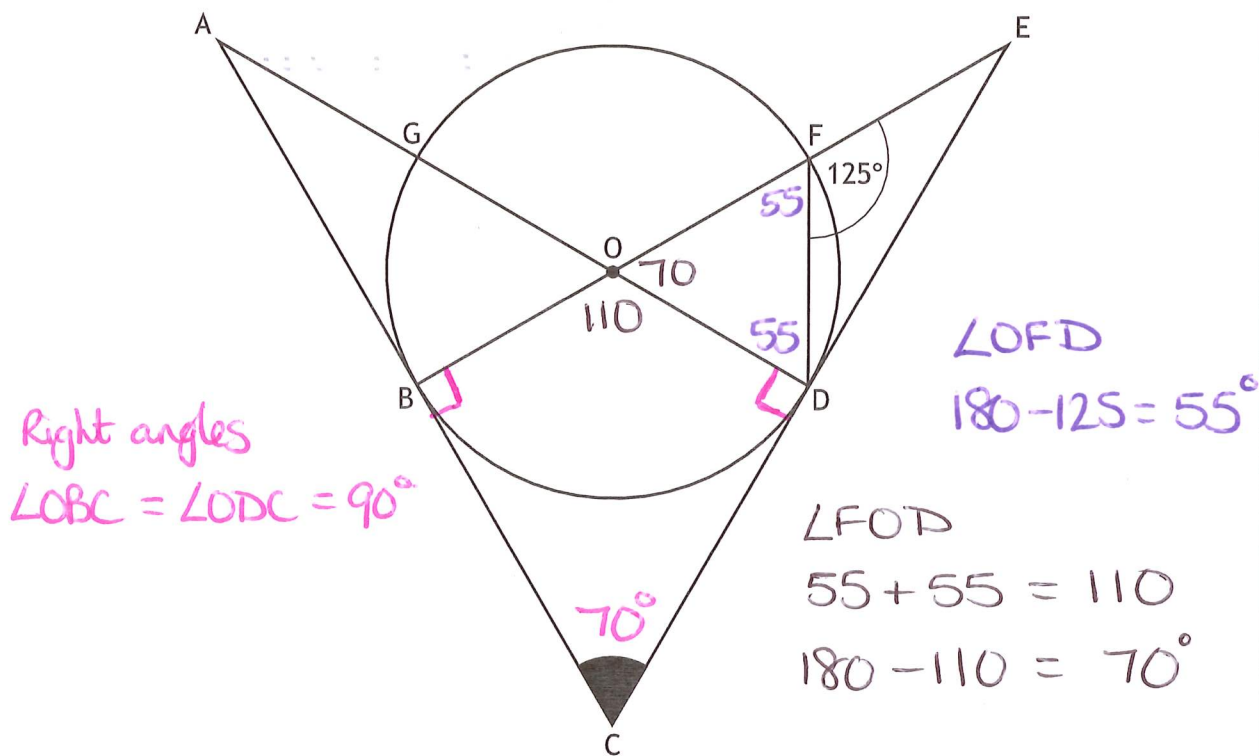
$$\begin{aligned}\therefore D &= -2(7) + 32 \\ &= -14 + 32\end{aligned}$$

$$\underline{\underline{D = 18 \text{ kilometres.}}}$$

[Turn over



10. The diagram below shows a circle centre O.
- AC is a tangent to the circle at the point B.
 - CE is a tangent to the circle at the point D.
 - DG and BF are diameters of the circle.
 - Angle DFE is 125° .



Calculate the size of shaded angle BCD.

$\angle BOD = 110^\circ$ 3

Tangent kite

$360 - (90 + 90 + 110)$

$\angle BCD = 70^\circ$



* X 8 4 7 7 5 0 1 1 0 *

11. A straight line has equation $x + 4y - 24 = 0$.
Find the gradient of this line.

2

$$\begin{aligned}x + 4y - 24 &= 0 \\4y &= -x + 24 \\y &= -\frac{1}{4}x + 6 \\y &= mx + c\end{aligned}$$

Gradient, $m = -\frac{1}{4}$.

[Turn over]



12. (a) Express $x^2 - 6x + 8$ in the form $(x-a)^2 + b$.

2

$$\begin{aligned} & [(x-3)^2 - 3^2] + 8 \\ & (x-3)^2 - 9 + 8 \\ & = \underline{(x-3)^2 - 1} \end{aligned}$$

- (b) Hence, or otherwise, state the coordinates of the turning point of the graph of $y = x^2 - 6x + 8$.

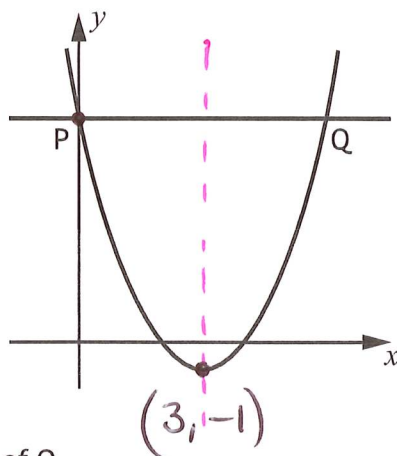
1

Minimum TP (3, -1)

The diagram shows the graph of $y = x^2 - 6x + 8$.

A line PQ has been drawn parallel to the x -axis, where:

- P lies on the y -axis
- P and Q lie on the graph of $y = x^2 - 6x + 8$.



P and Q have
same y -coord.

- (c) Find the coordinates of Q.

2

Using axis of symmetry $x_a = 6$

Using y -intercept at $x=0$, $y = 0^2 - 6(0) + 8$
 $y_e = 8$

Point Q (6, 8)



13. Expand and simplify fully $x\left(x^{\frac{1}{2}} + x^{-1}\right)$.

$$\begin{aligned}
 & x^1 \times x^{\frac{1}{2}} + x^1 \times x^{-1} \\
 & x^{\frac{3}{2}} + x^0 \\
 & = \underline{\underline{x^{\frac{3}{2}} + 1}}
 \end{aligned}$$

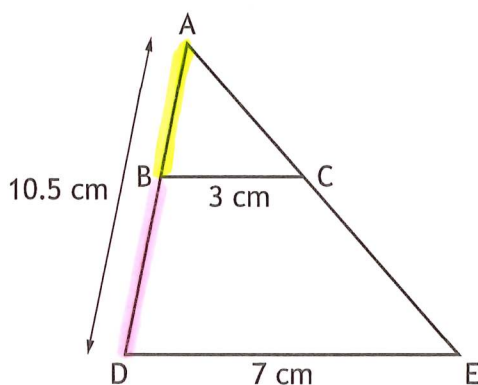
[Turn over

OR $\sqrt{x^3} + 1$ also correct.



14. In the diagram, triangles ABC and ADE are mathematically similar.

- $BC = 3$ centimetres
- $DE = 7$ centimetres
- $AD = 10.5$ centimetres



Calculate the length of BD.

3

To find BD, we must find AB first.

$$\text{Linear SFR} = \frac{\text{wee}}{\text{big}} = \frac{3}{7}$$

$$AB = \frac{3}{7} \text{ of } 10.5 = 4.5 \text{ cm}$$

$$7 \overline{) 31.5}$$

$$BD = 10.5 - 4.5$$

$$BD = 6 \text{ cm.}$$

[END OF QUESTION PAPER]



* X 8 4 7 7 5 0 1 1 4 *