## The Circle

- 1. Find the equation of the circle centre (-4,7) which has the x-axis as a tangent.
- 2. Find the equation of the circle which has the lines x = -4, x = 8, y = -2 and y = 10 as tangents.
- 3. A circle has equation  $x^2 + y^2 4x 8y 5 = 0$ . Write down the equation of the tangent to this circle at the point (-3,4).
- 4. A circle has equation  $(x + 5)^2 + (y 1)^2 = 16$ . Write down the equation of the tangent to this circle at the point A(-5,-3).
- 5. A circle has equation  $x^2 + y^2 + 6x + 4 = 0$ . Find the equation of the tangent to this circle at the point P(-5,-1).

6. Find the equation of the tangent to the circle  $x^2 + y^2 - 8x + 2y - 3 = 0$ at the point A(2,3).





P(-5,-1

A(2,3

8. P is the point (-5,3) and Q is (5,-21). Find the equation of the circle which has PQ as diameter.

9. Two congruent circles with centres A and B touch at G. The equations of the circles are

$$x^{2} + y^{2} + 8x - 4y - 5 = 0$$
 and  $x^{2} + y^{2} - 4x - 20y + 79 = 0$ 

- (a) Find the coordinates of G.
- (b) Find the length of AB.



10. Two circles have equations

$$(x + 1)^{2} + (y + 3)^{2} = 20$$
 and  $x^{2} + y^{2} - 10x - 18y + 26 = 0$ 

- (a) Write down the centre and radius of each circle.
- (b) Show that the circles touch at a single point.
- (c) Find P, the point of contact of the circles.
- 11. Two circles have equations

$$x^{2} + y^{2} + 4x + 16y - 60 = 0$$
 and  $x^{2} + y^{2} - 8x + 4y + 12 = 0$ 

Show that these circles touch at a single point.

12. Three circles touch externally as shown. The centres of the circles are collinear and the equations of the two smaller circles are

$$(x+2)^2 + (y-8)^2 = 9$$
 and

$$x^2 + y^2 - 20x + 16y + 155 = 0$$

Find the equation of the larger circle.



- 13. The circle  $x^2 + y^2 + 4x 7y 8 = 0$  cuts the y-axis at two points. Find the coordinates of these points.
- 14. The circle  $x^2 + y^2 2x + 10y 24 = 0$  cuts the x-axis at the points A and B. Find the length of AB.
- 15. (a) A circle has equation  $(x + 3)^2 + (y 6)^2 = 61$ . Find the equation of the tangent to this circle at the point A(3,3).
  - (b) Show that this tangent is also a tangent to the circle with equation  $x^2 + y^2 + 6x 7y 10 = 0$  and find the point of contact.



- 16. Show that the line y = -3x 10 is a tangent to the circle with equation  $x^2 + y^2 8x + 4y 20 = 0$  and find the point of contact.
- 17. (a) Find the equation of the tangent to the curve  $y = 2x^3 4x^2 7x + 12$ at the point where x = 2.
  - (b) Show that this tangent is also a tangent to the circle  $x^2 + y^2 6x + 2y + 10 = 0$  and find the point of contact.
- 18. Show that the line y = 2x + 1 does not intersect the circle with equation  $x^2 + y^2 2x + 4y + 1 = 0$ .
- 19. For what range of values of p does the equation  $x^2 + y^2 + 2px + 2py + 6p + 8 = 0$  represent a circle.
- 20. For what range of values of k does the equation  $x^2 + y^2 2kx + 4ky + 4 k = 0$  represent a circle.
- 21. (a) A circle has centre (a,0), a > 0 and radius 4 units. Write down the equation of this circle.
  - (b) Show that if y = x is a tangent to this circle then  $a = 4\sqrt{2}$ .



- 22. The diagram shows six identical circles. Circle A has equation  $x^2 + y^2 - 6x - 6y + 9 = 0.$ 
  - (a) Write down the equation of circle F.
  - (b) Find the point of contact between the the circles C and D.
- 23. (a) Find the equation of AB, the perpendicular bisector of the line joining the points P(-3,1) and Q(1,9).
  - (b) C is the centre of a circle passing through P and Q. Given that QC is parallel to the y-axis, determine the equation of the circle.
  - (c) The tangents at P and Q intersect at T.

Write down

(i) the equation of the tangent at Q

(ii) the coordinates of T.

24. The diagram shows a tangent kite ABCD and a circle centre C.A is the point (-8,0) and B is (4,9).The radius CD is parallel to the y-axis.

- (a) Find the coordinates of D and write down the equation of CD.
- (b) Find the equation of the line BC.
- (c) Find the coordinates of C and hence determine the equation of the circle.





