

CfE Higher Mathematics

Mathematics Department

	How well do I understand?
Straight Line	
Calculate the distance between 2 points using the distance formula $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$	1 2 3 4 5 6 7 8 9 10
Calculate a mid-point $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$	1 2 3 4 5 6 7 8 9 10
Calculate a gradient between 2 given points $m = \frac{y_2 - y_1}{x_2 - x_1}$	1 2 3 4 5 6 7 8 9 10
Calculate the gradient when given the angle that the line makes with the positive direction of the x-axis $m = tan\theta$	1 2 3 4 5 6 7 8 9 10
Gradient of a parallel lines $m_1 = m_2$	1 2 3 4 5 6 7 8 9 10
Gradient of perpendicular lines $m_1 imes m_2 = -1$	1 2 3 4 5 6 7 8 9 10
Calculate the equation of a line when given the gradient and y-intercept $y = mx + c$	1 2 3 4 5 6 7 8 9 10
Calculate the equation of a line when given the gradient and a point on the line $y - b = m(x - a)$	1 2 3 4 5 6 7 8 9 10
Find the point of intersection between lines	1 2 3 4 5 6 7 8 9 10
Calculating the equation of a median	1 2 3 4 5 6 7 8 9 10
Calculating the equation of an altitude	1 2 3 4 5 6 7 8 9 10
Calculating the equation of a perpendicular bisector	1 2 3 4 5 6 7 8 9 10
State if points are collinear	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Functions and Graphs	
Understand function terminology and notation	1 2 3 4 5 6 7 8 9 10
Find a composite function e.g. f (g(x))	1 2 3 4 5 6 7 8 9 10
Find the equation of an inverse function, $f^{-1}(x)$	1 2 3 4 5 6 7 8 9 10
Sketch / assess functions and their transformations e.g. f(x) + a, f(x + a), f(-x), -f(x), kf(x), f(kx)	1 2 3 4 5 6 7 8 9 10
Sketch / assess logarithmic and exponential functions	1 2 3 4 5 6 7 8 9 10
Sketch / assess trigonometric functions in degrees and radians	1 2 3 4 5 6 7 8 9 10

	How well do I understand?
Recurrence Relations	
Construct a recurrence relation when given relevant information	1 2 3 4 5 6 7 8 9 10
Calculate a and b when given three consecutive terms in a sequence	1 2 3 4 5 6 7 8 9 10
Find the limit, where it exists, for a recurrence relation	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Differentiation	
Differentiate a function of the form $f(x) = ax^n$	1 2 3 4 5 6 7 8 9 10
Know how to prepare to differentiate e.g. functions with negative and fractional powers	1 2 3 4 5 6 7 8 9 10
Calculate the gradient of a tangent to a function	1 2 3 4 5 6 7 8 9 10
Calculate the equation of a tangent to a function	1 2 3 4 5 6 7 8 9 10
Find an expression for velocity ($v = \frac{dx}{dt}$) when given the displacement, x	1 2 3 4 5 6 7 8 9 10
Find an expression for acceleration ($s = \frac{dv}{dt}$) when given the velocity, v	1 2 3 4 5 6 7 8 9 10
Sketch the graph of a derived function	1 2 3 4 5 6 7 8 9 10
Find stationary points and their nature	1 2 3 4 5 6 7 8 9 10
Identify when a function is increasing/decreasing	1 2 3 4 5 6 7 8 9 10
Use the stationary points and points to intersection of the axes to sketch the graph of a curve	1 2 3 4 5 6 7 8 9 10
Find the maximum/minimum values in a closed interval	1 2 3 4 5 6 7 8 9 10
Solve optimization problems	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Quadratics and Polynomials	
Complete the square for a quadratic expression	1 2 3 4 5 6 7 8 9 10
State the max/min value of a function completed square form	1 2 3 4 5 6 7 8 9 10
Sketch the graph of a quadratic function	1 2 3 4 5 6 7 8 9 10
Solve a quadratic equation through factorising or quadratic formula	1 2 3 4 5 6 7 8 9 10
Use the discriminant to determine the nature of the roots	1 2 3 4 5 6 7 8 9 10
Use the discriminant to prove tangency	1 2 3 4 5 6 7 8 9 10
Solve quadratic inequalities	1 2 3 4 5 6 7 8 9 10
Use synthetic division to factorise a polynomial	1 2 3 4 5 6 7 8 9 10
Use the remainder and factor theorems	1 2 3 4 5 6 7 8 9 10
Find the roots of polynomials	1 2 3 4 5 6 7 8 9 10
State the equation of a polynomial given the graph of the function	1 2 3 4 5 6 7 8 9 10
Use iteration to find approximate roots of polynomials	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Integration	
Integrate a function of the form f (x) = axn.	1 2 3 4 5 6 7 8 9 10
Know how to prepare to integrate e.g. functions with negative and fractional powers	1 2 3 4 5 6 7 8 9 10
Solve differential equations to find a general or particular solution	1 2 3 4 5 6 7 8 9 10
Evaluate a definite integral	1 2 3 4 5 6 7 8 9 10
Find the area between a curve and the x-axis	1 2 3 4 5 6 7 8 9 10
Find the area between a line and a curve or 2 curves	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Circle	
Find the equation of a circle with centre O and radius $r x^2 + y^2 = r^2$	1 2 3 4 5 6 7 8 9 10
Find the equation of a circle with centre (<i>a</i> , <i>b</i>) and radius $r (x - a)^2 + (y - b)^2 = r^2$	1 2 3 4 5 6 7 8 9 10
Find the equation of a circle in general form $x^2 + y^2 + 2gx + 2fy + c = 0$	1 2 3 4 5 6 7 8 9 10
Find the centre and radius of a circle in any form	1 2 3 4 5 6 7 8 9 10
Find the equation of a tangent to a circle	1 2 3 4 5 6 7 8 9 10
Use the discriminant to determine the number of points of contact between a line and circle	1 2 3 4 5 6 7 8 9 10
Find the point/points of intersection between a line and a circle	1 2 3 4 5 6 7 8 9 10
Know if two circles never touch, touch once internally / externally or touch twice	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Trigonometry	
State the exact values of sin/cos/tan for angles: 0°, 30°, 45°, 60° & 90°	1 2 3 4 5 6 7 8 9 10
Convert between degrees and radians	1 2 3 4 5 6 7 8 9 10
Solve simple linear trigonometric equations	1 2 3 4 5 6 7 8 9 10
Solve trigonometric equations with multiple angles	1 2 3 4 5 6 7 8 9 10
Solve trigonometric equations involving squared functions	1 2 3 4 5 6 7 8 9 10
Solve quadratic trigonometric equations	1 2 3 4 5 6 7 8 9 10
Solve trigonometric equations with phase angles	1 2 3 4 5 6 7 8 9 10
Use trigonometric identities to simplify and solve trigonometric equations	1 2 3 4 5 6 7 8 9 10
Use the addition formulae to solve problems	1 2 3 4 5 6 7 8 9 10
Use the additional formulae to find the related angle formulae	1 2 3 4 5 6 7 8 9 10
Use the double angle formulae to solve problems	1 2 3 4 5 6 7 8 9 10
Use the addition & double angle formulae to simplify and solve trigonometric equations	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Vectors	
Use vectors to prove collinearity of points	1 2 3 4 5 6 7 8 9 10
Write column vectors in terms of the unit vectors <u>i</u> , <u>i</u> and <u>k</u>	1 2 3 4 5 6 7 8 9 10
Use vectors to divide a line in a given ratio	1 2 3 4 5 6 7 8 9 10
Use the scalar product to show that vectors are perpendicular	1 2 3 4 5 6 7 8 9 10
Use the scalar product to find the angle between vectors	1 2 3 4 5 6 7 8 9 10

	How well do I understand?
Further Calculus	
Differentiate $\sin x$ and $\cos x$	1 2 3 4 5 6 7 8 9 10
Integrate $\sin x$ and $\cos x$	1 2 3 4 5 6 7 8 9 10
Use the Chain Rule to differentiate a function of the form $f(x) = (ax + b)^n$	1 2 3 4 5 6 7 8 9 10
Integrate a function of the form $f(x) = (ax + b)^n$	1 2 3 4 5 6 7 8 9 10



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	How well do I understand?
Logarithms and Exponentials	
Convert between logarithmic and exponential forms $y = a^x \leftrightarrow x = \log_a y$	1 2 3 4 5 6 7 8 9 10
Use the rules of logs $\log_a 1 = 0$, $\log_a a = 1$, $\log_a x + \log_a y = \log_a xy$, $\log_a x - \log_a y = \log_a \frac{x}{y}$, $\log_a x^n = n \log_a x$	1 2 3 4 5 6 7 8 9 10
Solve logarithmic equations	1 2 3 4 5 6 7 8 9 10
Solve exponential problems	1 2 3 4 5 6 7 8 9 10
Use the graph of $\log_a y$ against x to find the equation connecting x and y in the form $y = ab^x$	1 2 3 4 5 6 7 8 9 10
Use the graph of $\log_a y$ against $\log_a x$ to find the equation connecting x and y in the form $y = ax^n$	1 2 3 4 5 6 7 8 9 10